

Colloque G2

Gravimetry for the LNE Watt balance

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http://synte.obspm.fr/tfc/capteurs_inertiels/

Lecture

Kilogram in the SI

actual situation and evolution

LNE Watt balance

SYRTE participation: Gravimetry

Lecture

Kilogram in the SI

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The kilogram

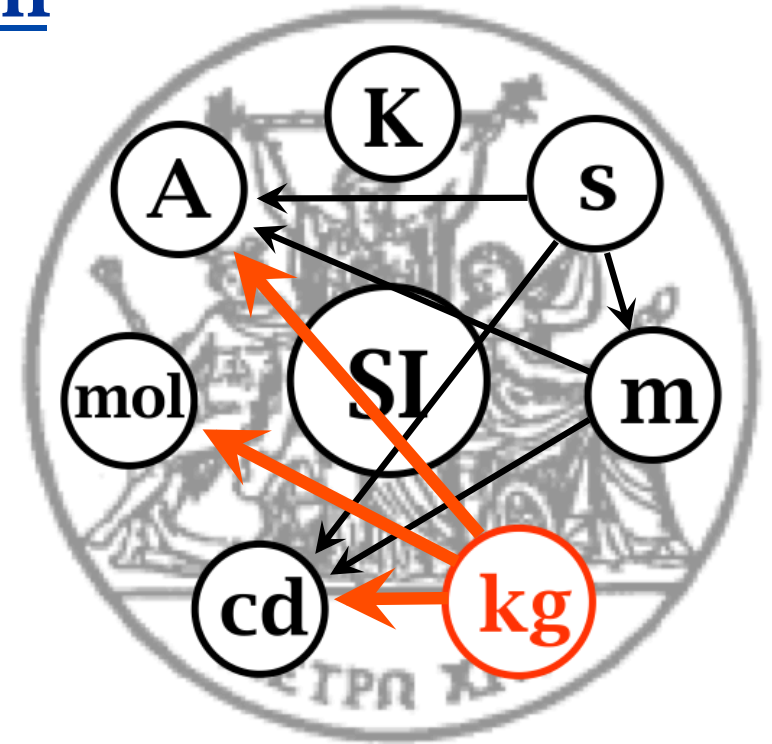
*Le kilogramme est l'unité de masse ;
il est égal à la masse
du prototype international du
kilogramme*

1^{ère} CGPM - 1889 / 3^{ème} CGPM - 1901



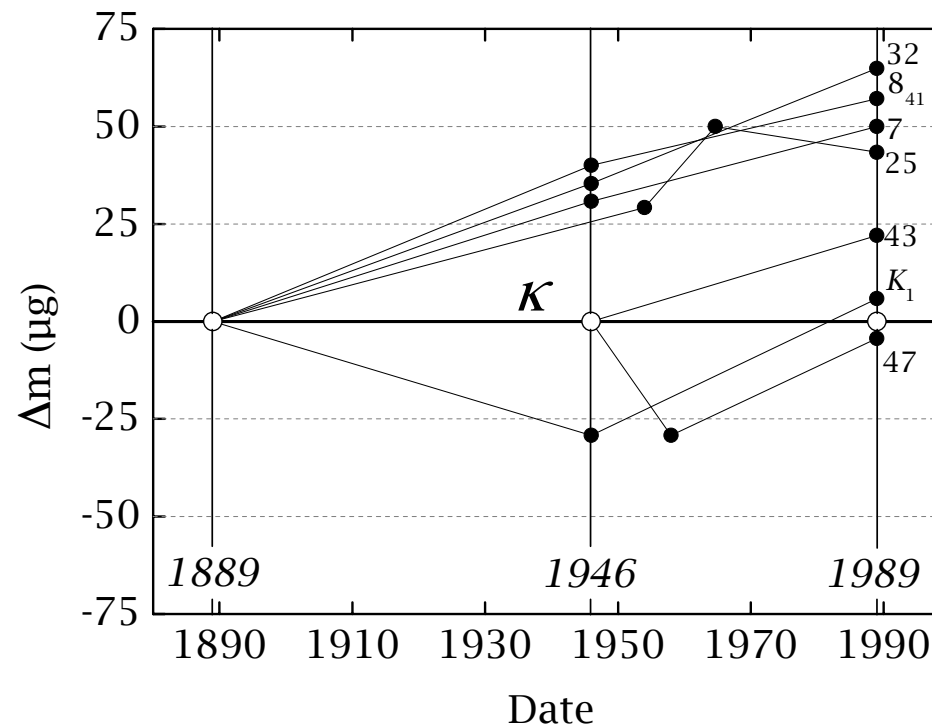
International prototype
of kilogram (κ)

- 1 kg exactly
- Cylindre PtIr
- diameter = height



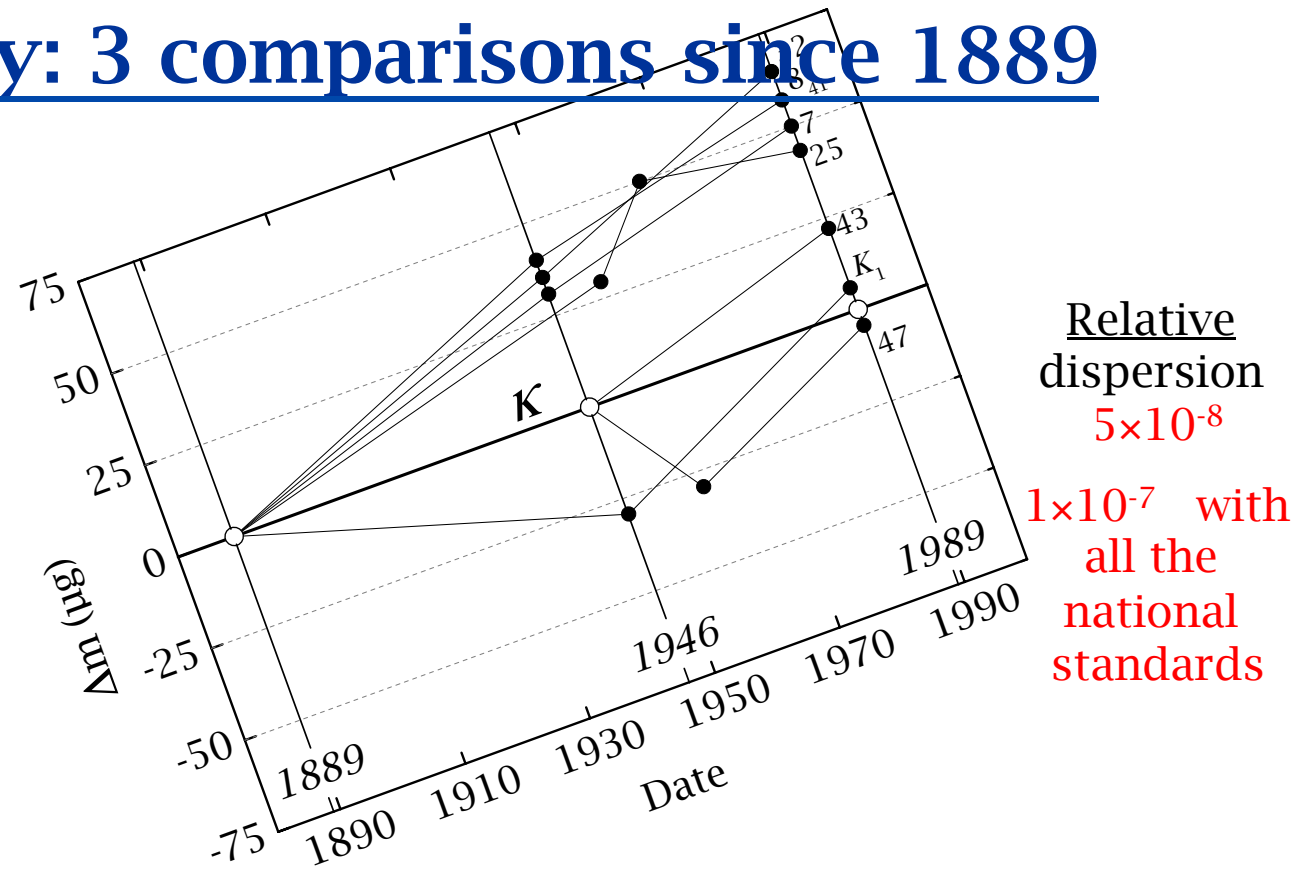
Other units
depends of kg

K stability: 3 comparisons since 1889

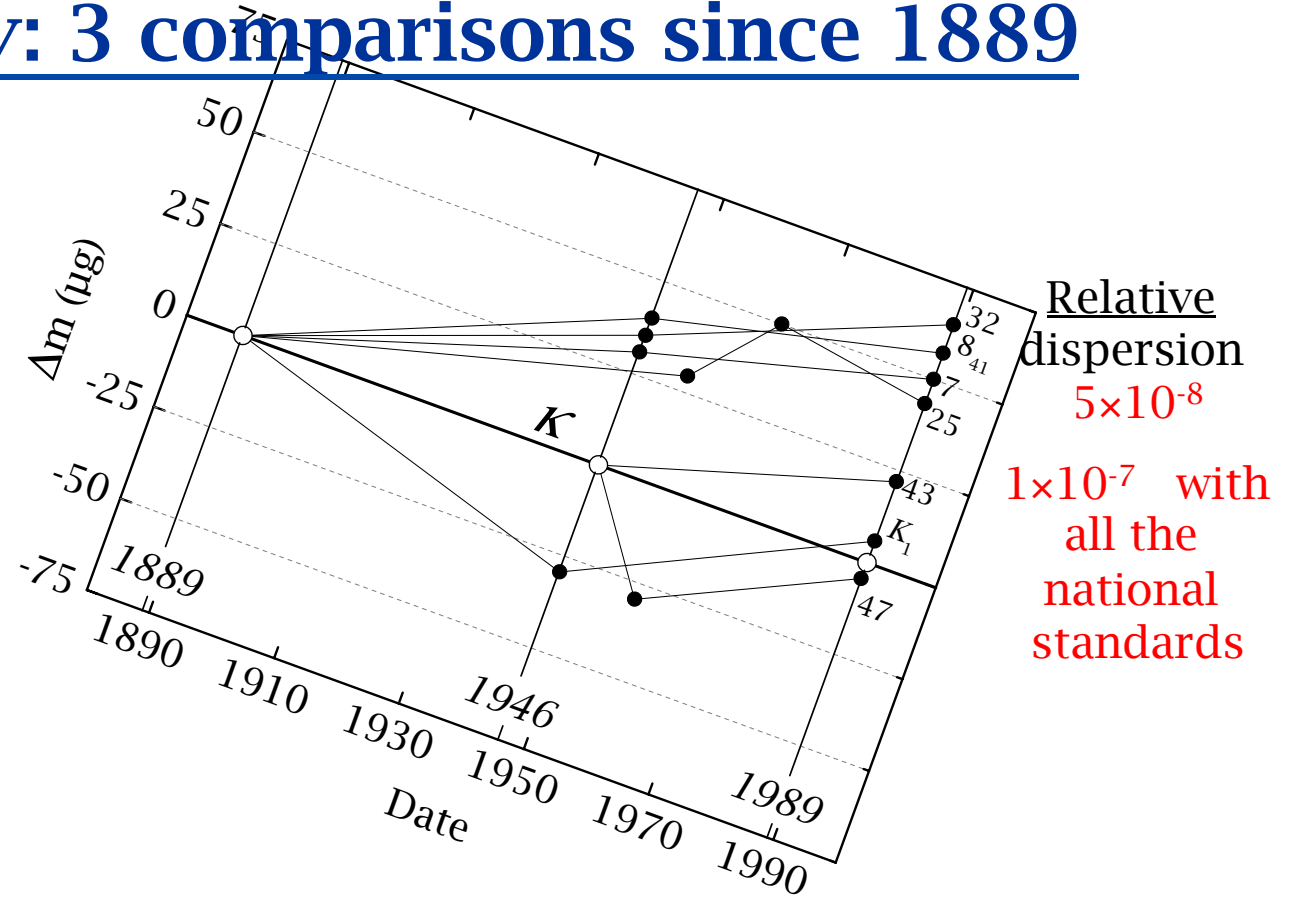


Relative dispersion
 5×10^{-8}
 1×10^{-7} with
all the
national
standards

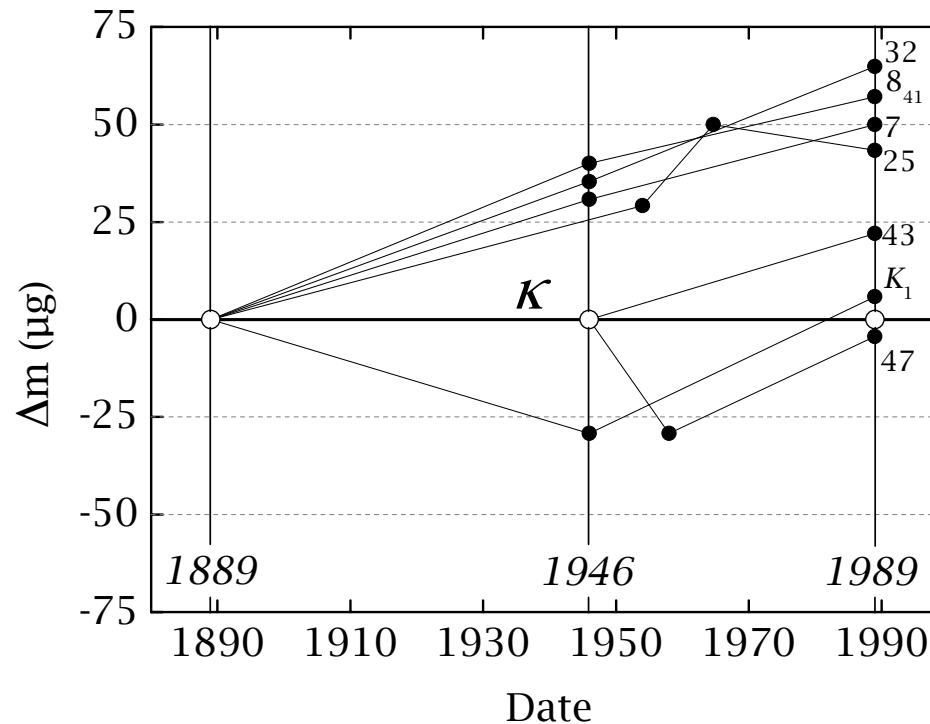
A photograph of a museum display case containing several mechanical devices, likely early computers or calculators, arranged on shelves. The devices are dark, possibly metal, and some have white labels with numbers like 11, 12, 13, 14, 15, 16, 17, 18, and 19.



K stability: 3 comparisons since 1889



K stability: 3 comparisons since 1889



Relative dispersion

$$5 \times 10^{-8}$$

1×10^{-7} with
all the
national
standards

→ Requirement: SI have to evolve, to be improved, especially the kilogram

Many CGPM resolutions encouraging NMI to investigate, study new possibilities

Résolution 5, 20^{ème} CGPM, 1995

Résolution 7, 21^{ème} CGPM, 1999

Résolution 12, 23^{ème} CGPM, 2007

Résolution 1, 24^{ème} CGPM, 2011

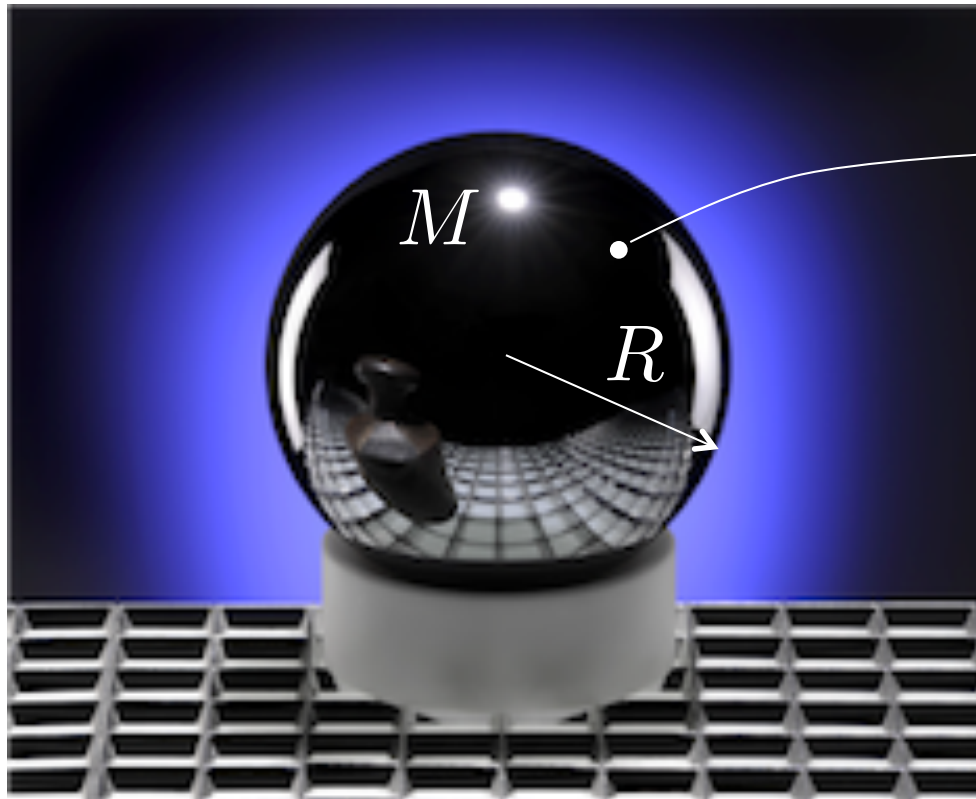
Avogadro project, N_A

Mesure the mass of a microscopic, macroscopic particule ?

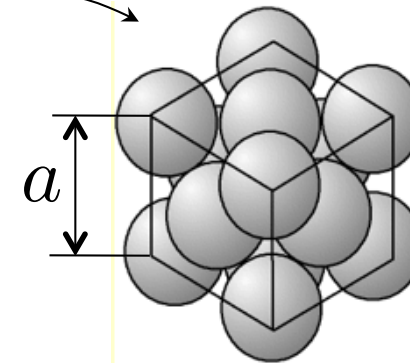
➡ *Link to the macroscopic domain ?*

Realisation of a massive object of know atoms

N_A realisation which define the mole



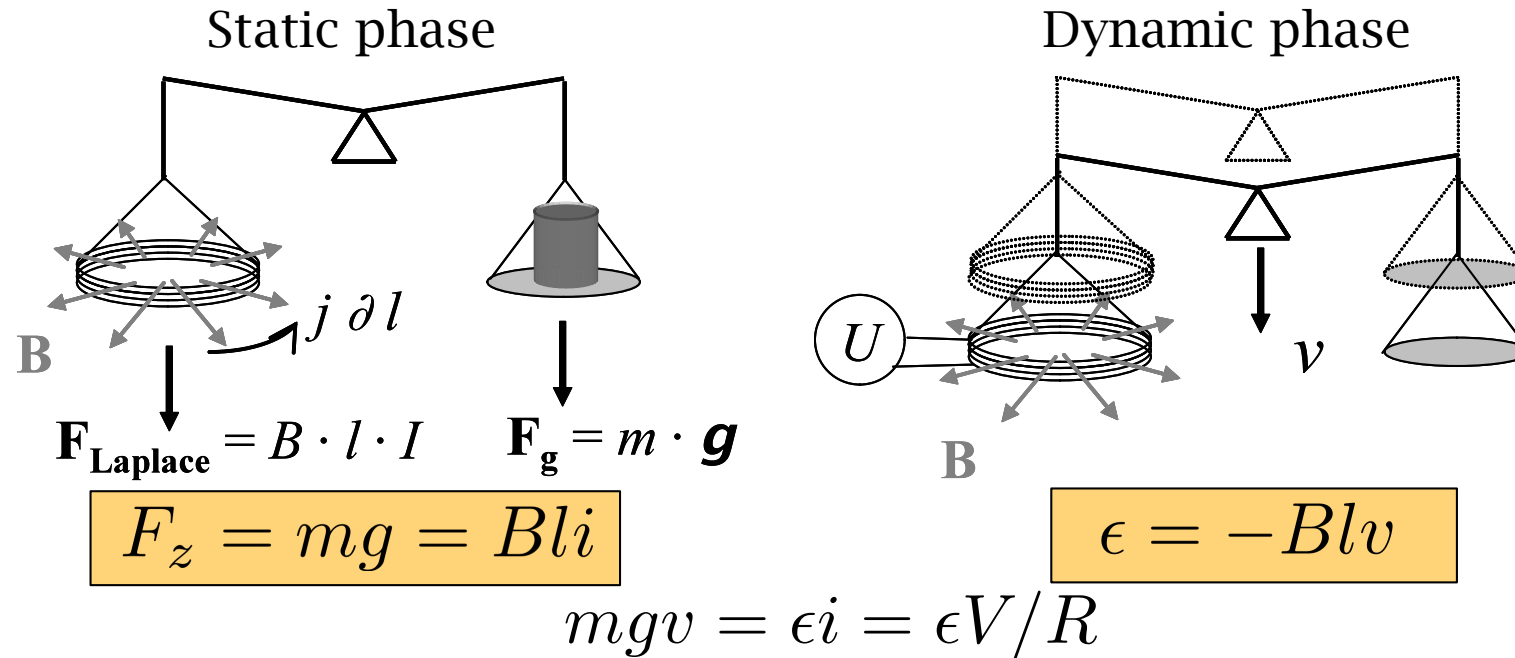
Determine the number of atoms
in a 1 kg silicium



$$\rho = \frac{M}{V} = \frac{n \, m_{\text{Si}}}{a^3 \, N_A}$$

Watt balance

Principle proposed by Brian Kibble in 1975



Electrical measurements: Josephson E ($K_J = 2e/h$) and Q Hall E ($R_K = h/e^2$)

$$R = k R_K / i$$

$$V = n_1 f_1 / K_J$$

$$\epsilon = n_2 f_2 / K_J$$

$$A = \frac{n_1 f_1 n_2 f_2 i}{k}$$

$$mgv = \frac{A}{K_J^2 R_K}$$

$$\frac{m}{h} = \frac{A}{4gv}$$

Absolute value of g needed

Lecture

Kilogram in the SI

actual situation and evolution

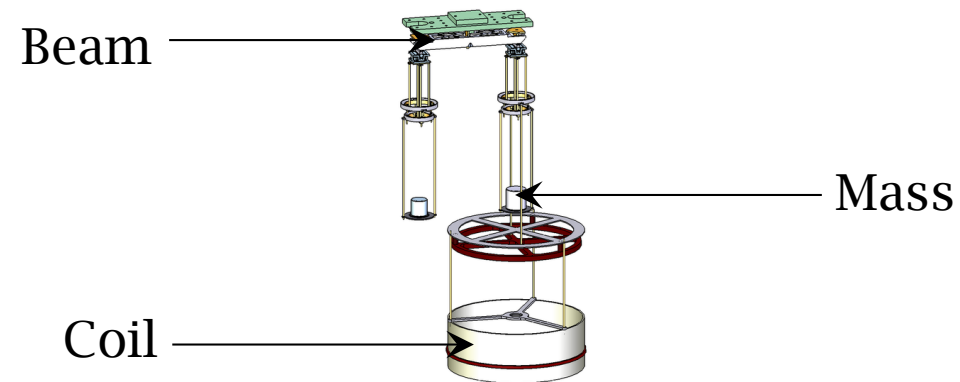
LNE Watt balance

SYRTE participation: Gravimetry

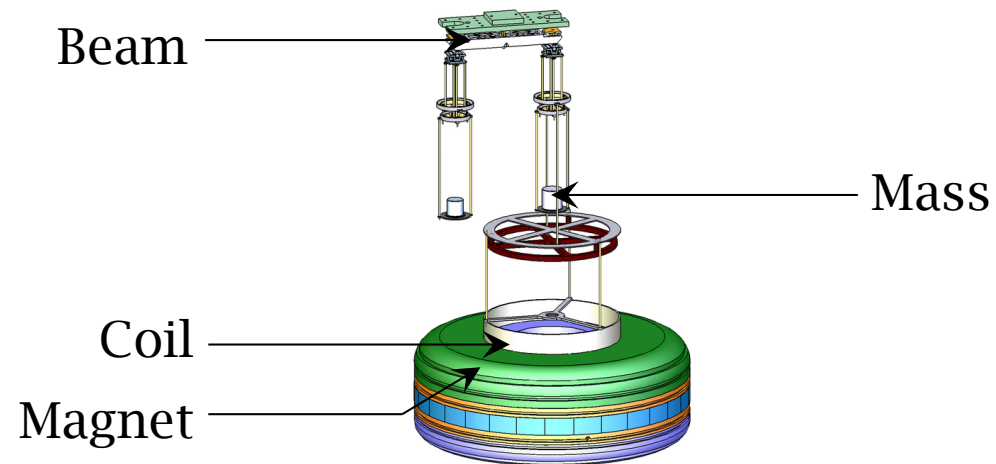
M. Thomas¹, P. Espel¹, D. Ziane¹, P. Pinot², P. Juncar², F. Piquemal¹ and G. Genevès¹

¹LNE, ²LNE-LCM/Cnam

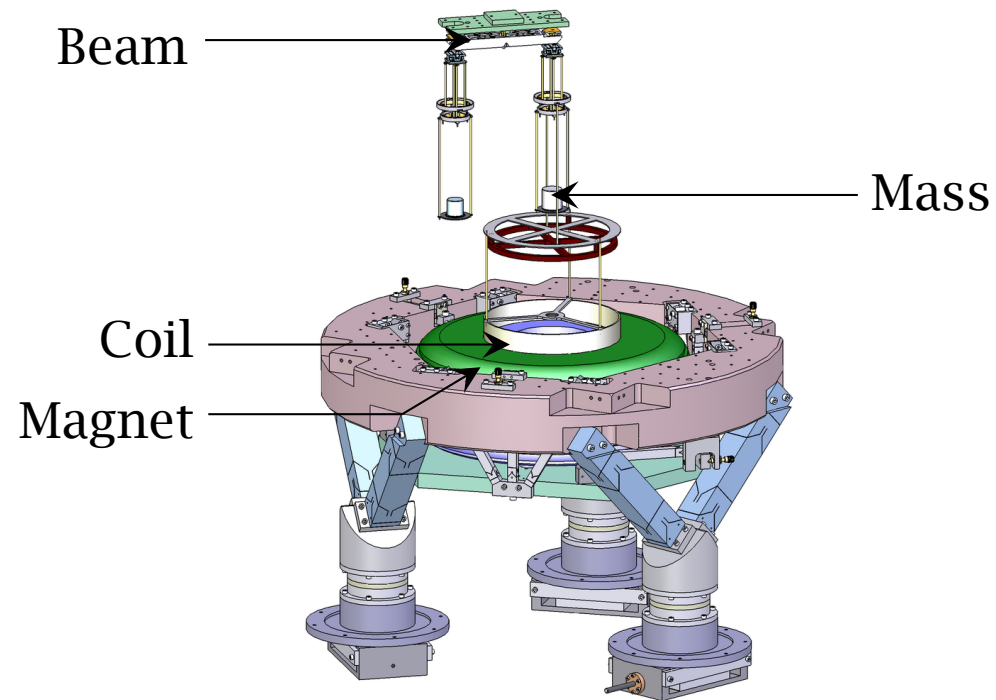
Parts of the LNE Watt balance



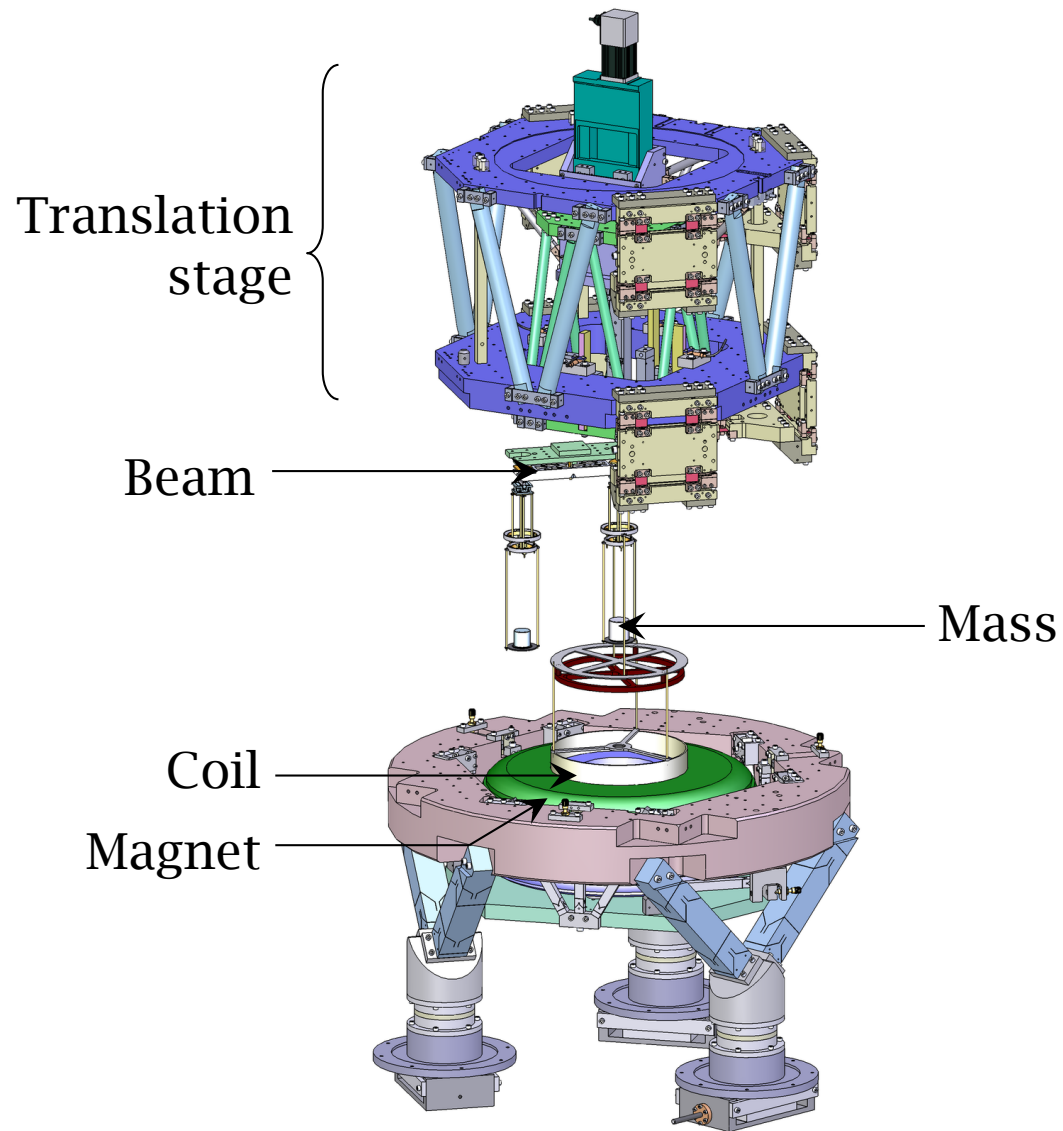
Parts of the LNE Watt balance



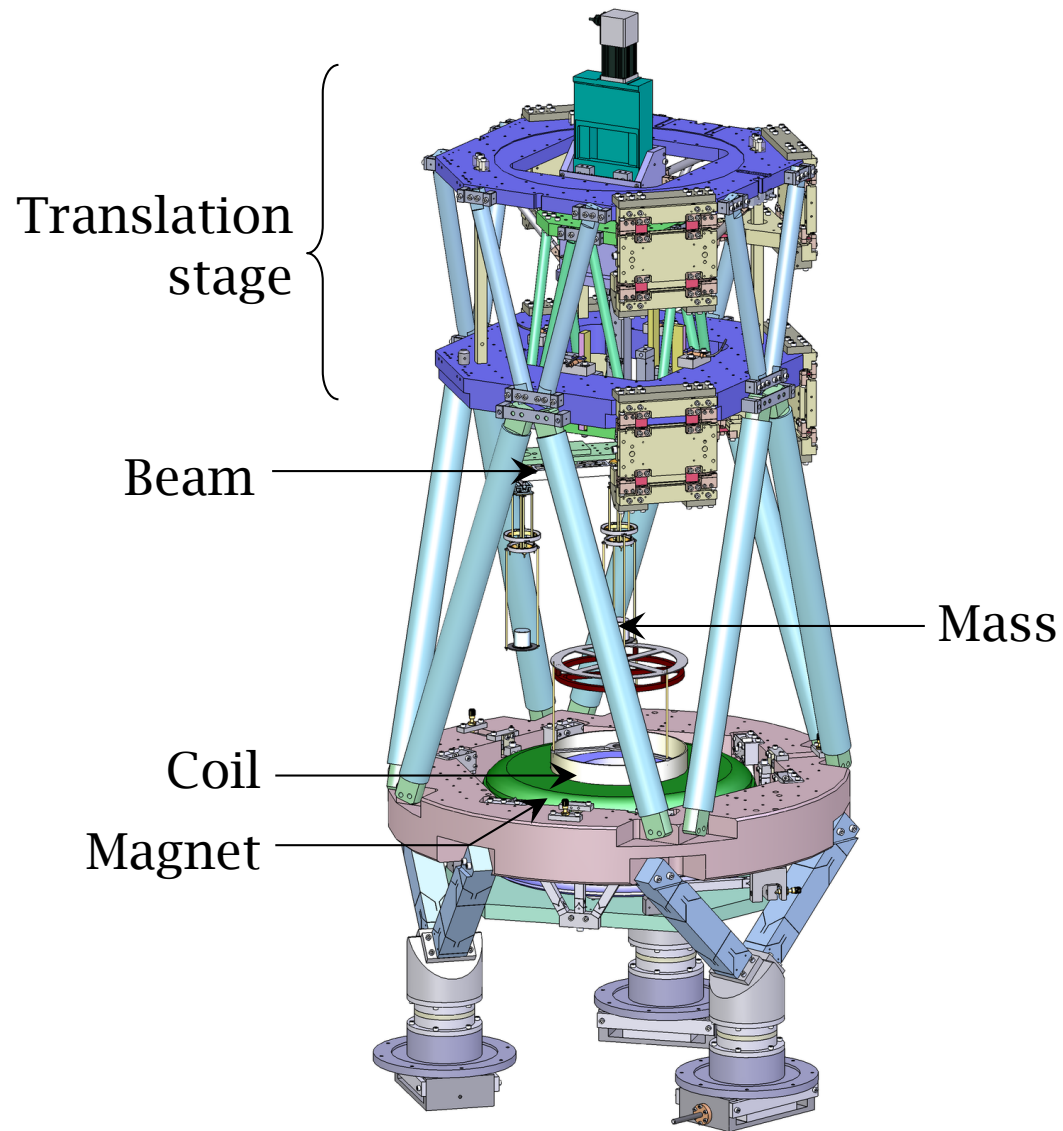
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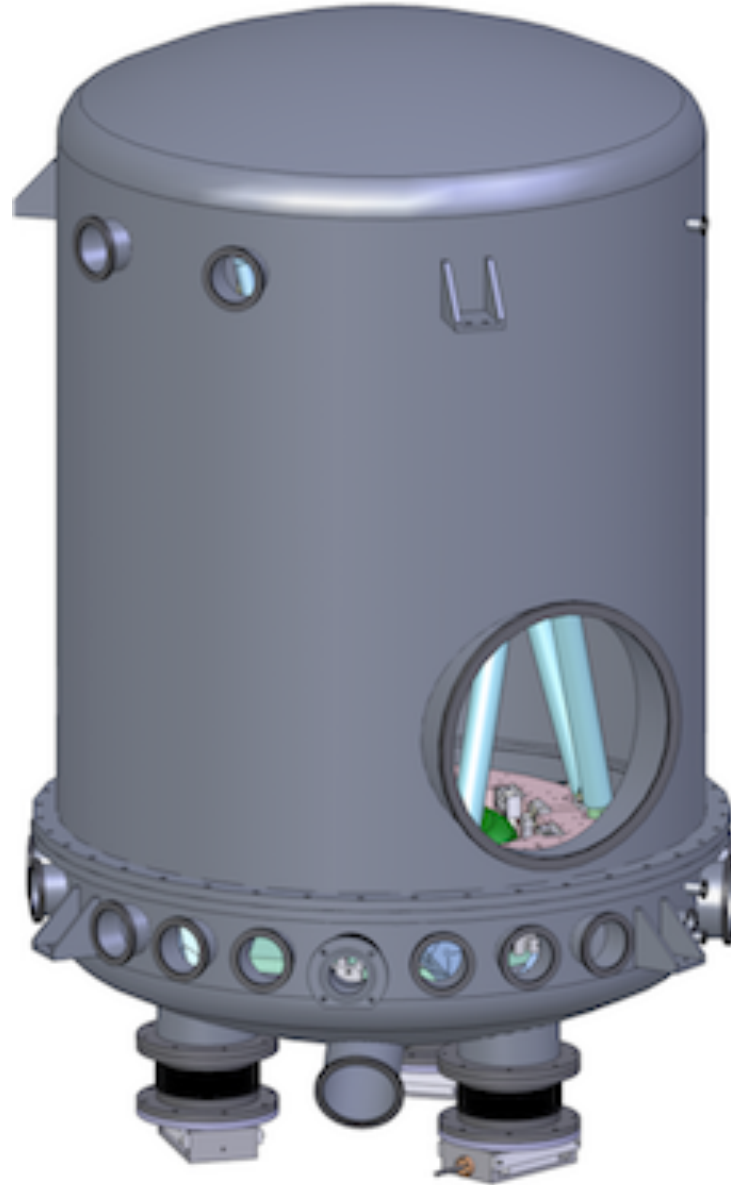
Parts of the LNE Watt balance



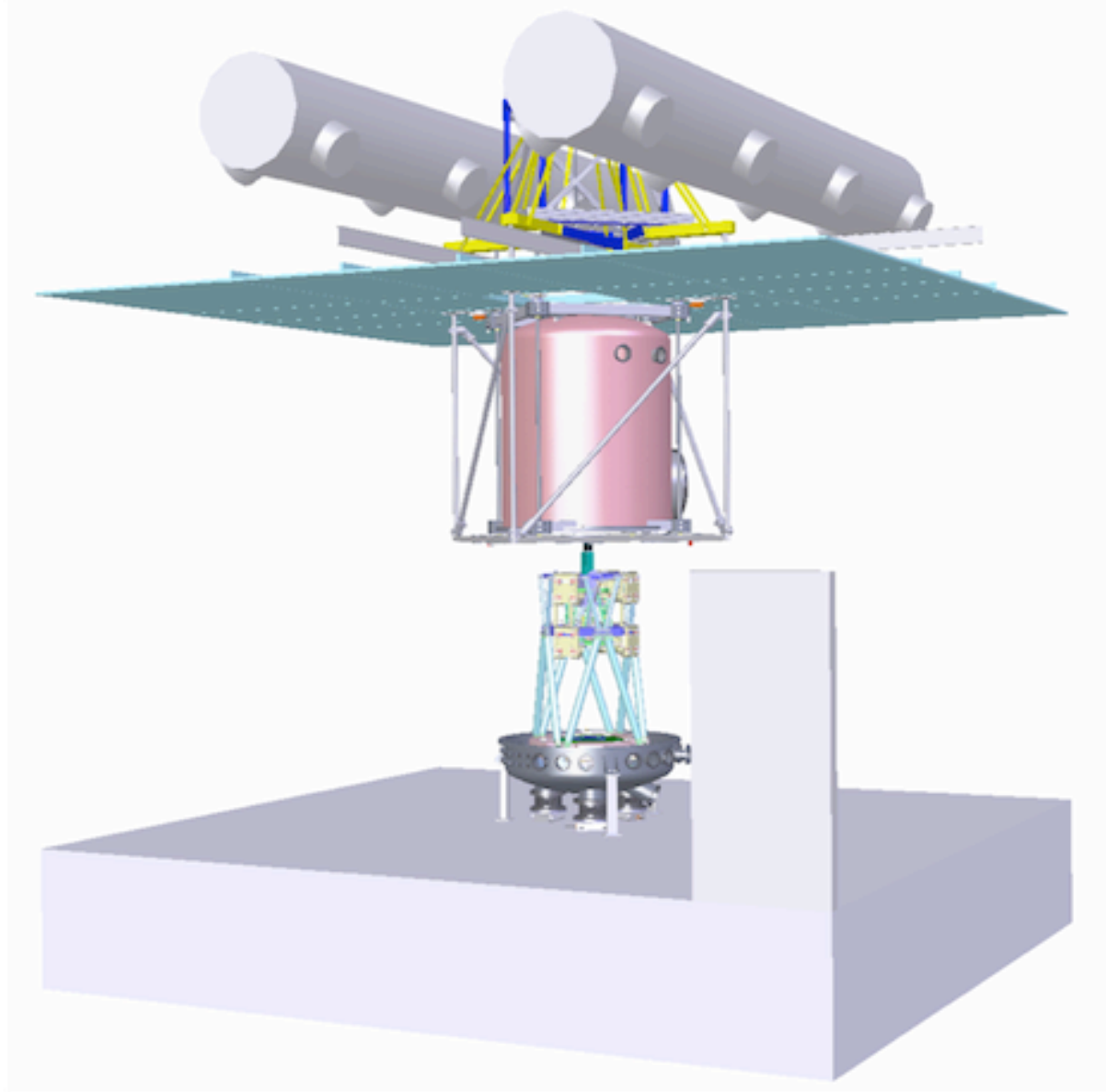
Parts of the LNE Watt balance



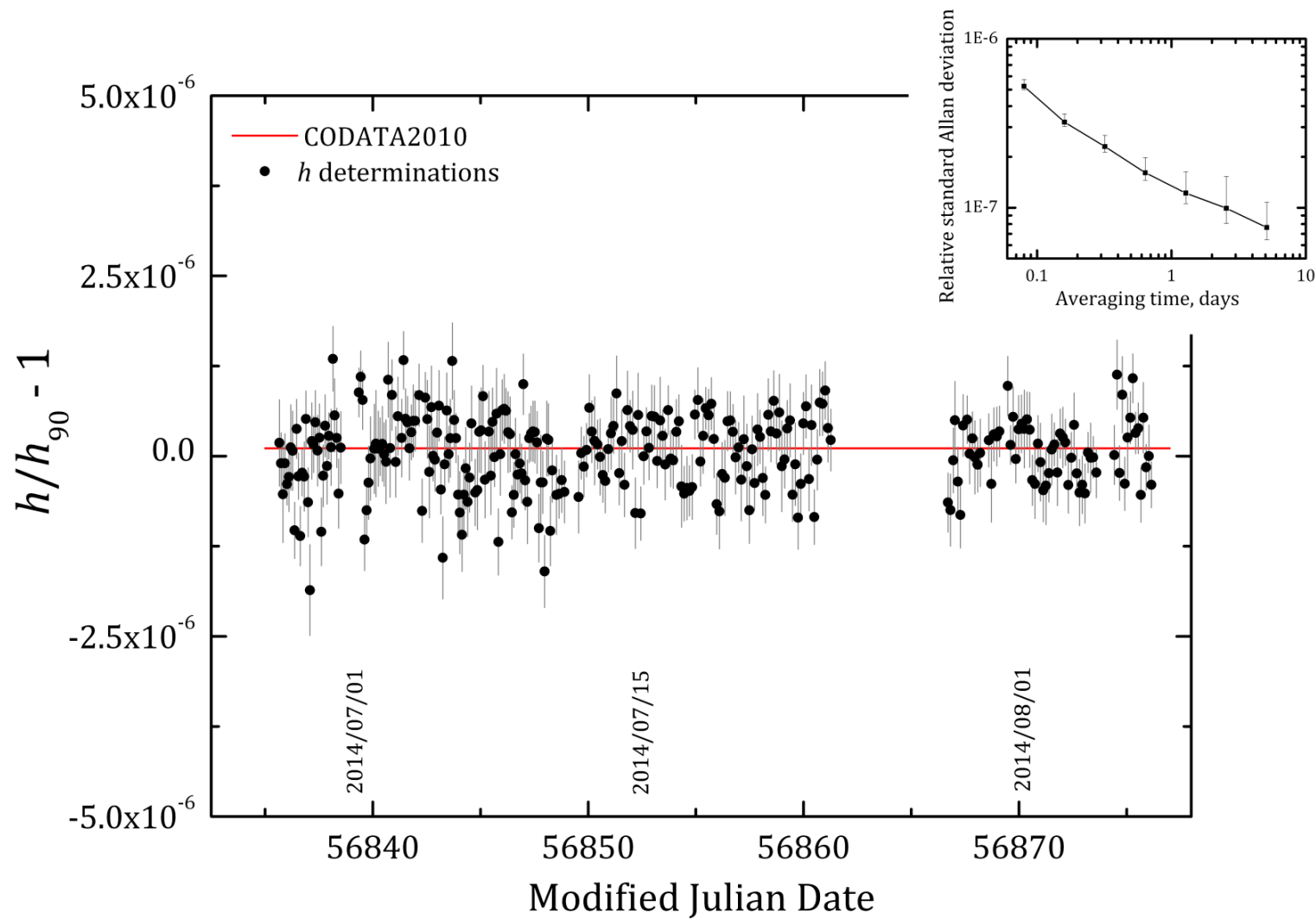
Parts of the LNE Watt balance



LNE Watt balance in its laboratory

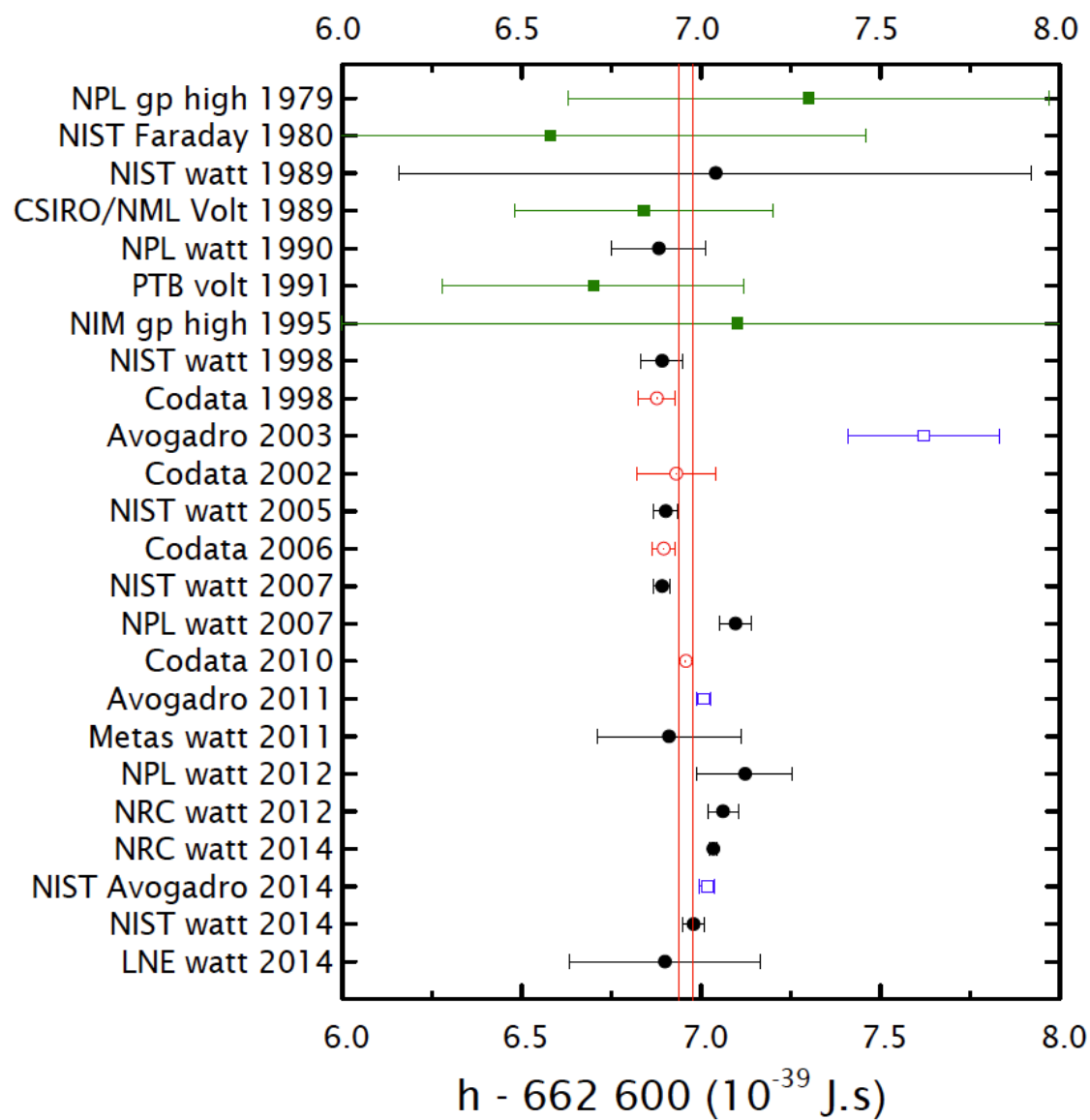


Results summer 2014



Involved Institutes and results

NPL, NIST, METAS, LNE, BIPM,
NIM, MSL, NRC



Involved Institutes and results

NPL, NIST, METAS, LNE, BIPM,

NIM, MSL, NRC

$h_{\text{NIST 2007}} : 3.6 \times 10^{-8}$ (1.2×10^{-8} for g)

$h_{\text{NPL 2007}} : 6.6 \times 10^{-8}$ (1.5×10^{-8} for g)
(0.7×10^{-8} for g)

$h_{\text{METAS 2011}} : 25 \times 10^{-8}$ (0.25×10^{-8} for g)

$h_{\text{NRC 2012}} : 4.3 \times 10^{-8}$ (? for g)

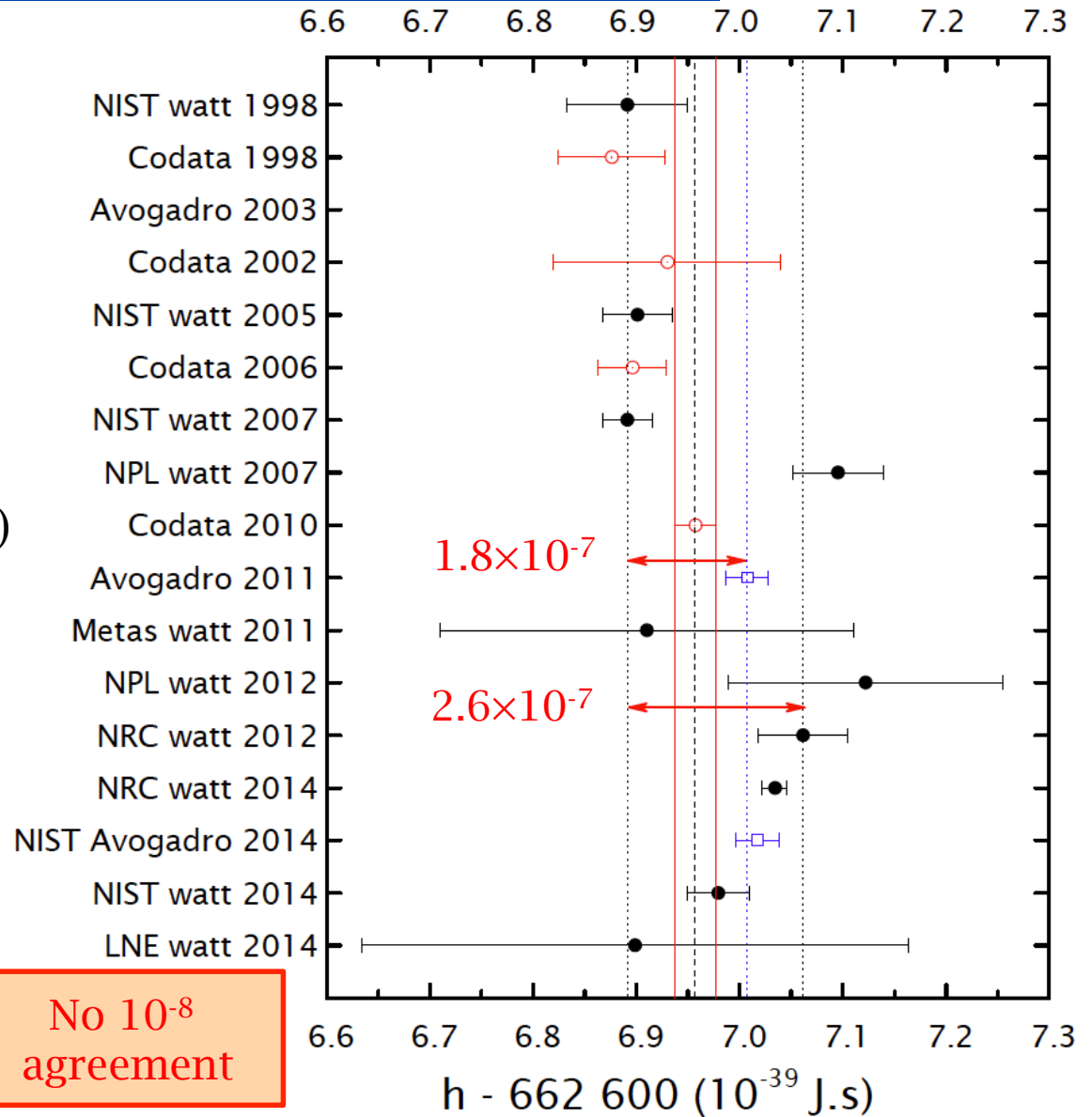
$h_{\text{NRC 2014}} : 1.8 \times 10^{-8}$ (0.57×10^{-8} for g)

$h_{\text{NIST 2014}} : 4.5 \times 10^{-8}$ (0.7×10^{-8} for g)

$h_{\text{LNE 2014}} : 40 \times 10^{-8}$ (0.5×10^{-8} for g)

↓
Last part of
the talk

No 10^{-8}
agreement



Lecture

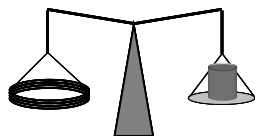
Kilogram in the SI

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SYRTE participation: Gravimetry

LNE Watt balance objective

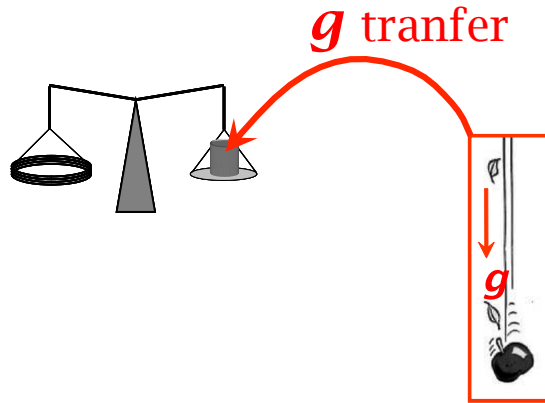


$$\frac{m}{h} = \frac{A}{4gv}$$

Determine h with a relative uncertainty of

$$2 \times 10^{-8}$$

LNE-SYRTE objective



$$\frac{m}{h} = \frac{A}{4gv}$$

Determine h with a relative uncertainty of

$$2 \times 10^{-8}$$

Determine g with an uncertainty of 10 nm.s^{-2} ($1 \text{ } \mu\text{Gal} \sim 10^{-9} g$)

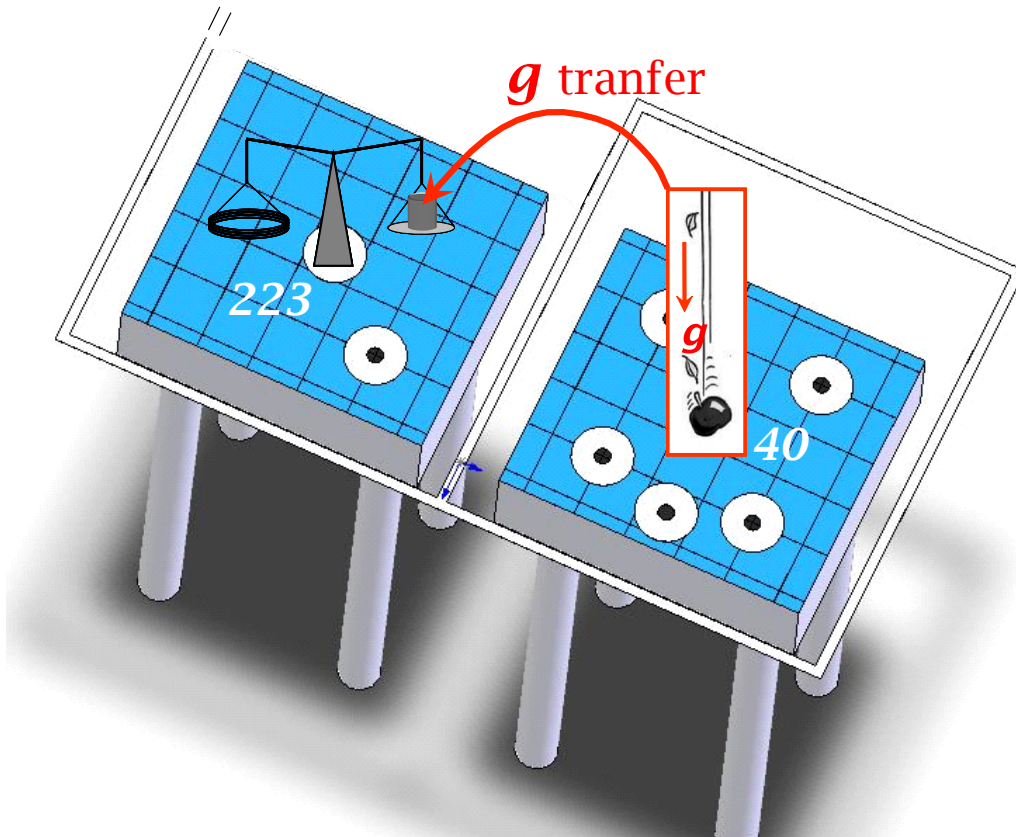
$$1 \times 10^{-9}$$

Two tasks:

→ determine g

→ insure the g transfer at the gravity center of the involved Watt balance mass

LNE-SYRTE objective



$$\frac{m}{h} = \frac{A}{4gv}$$

Determine h with a relative uncertainty of

$$2 \times 10^{-8}$$

Determine g with an uncertainty of 10 nm.s^{-2} ($1 \text{ } \mu\text{Gal} \sim 10^{-9} g$)

$$1 \times 10^{-9}$$

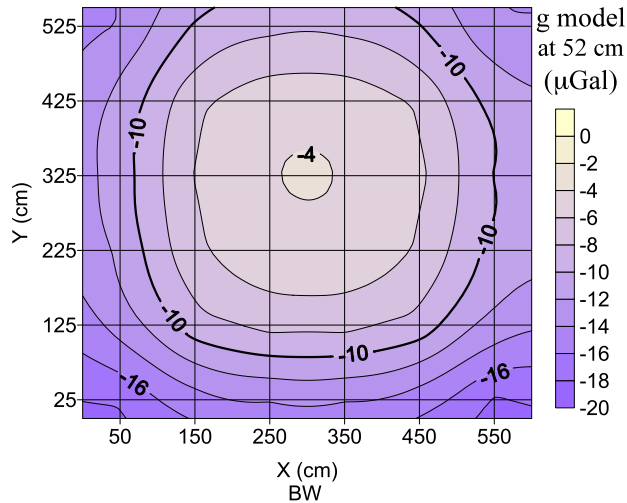
Two tasks:

- determine $g \Rightarrow$ absolute gravimeter
- insure the g transfer at the gravity center of the involved Watt balance mass $\Rightarrow$ laboratory gravity mapping

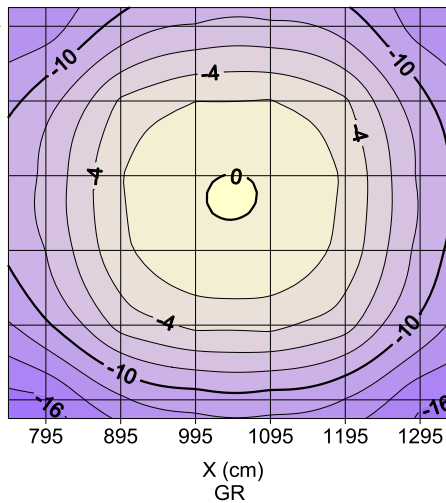
Model, g transfer

- Laboratories*

BW



GR



$U_{\text{model}} < 3 \mu\text{Gal}$ in a 50 m^3 volume

$U_{\text{centres}} = 1.0 \mu\text{Gal} \Rightarrow g$ transfer in the Watt balance
uncertainty budget : 10^{-9}

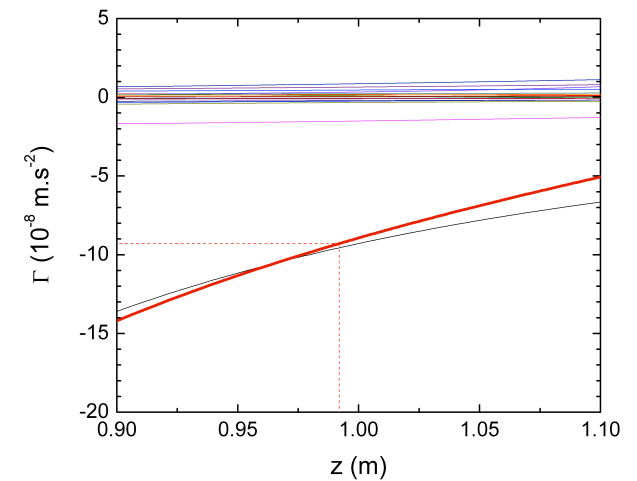
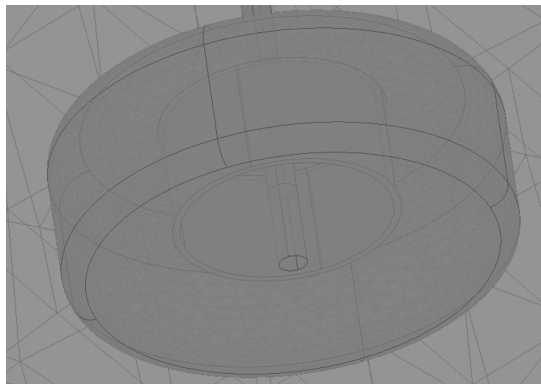
S. Merlet et al. *Metrologia* **45** (2008) 265-274

- Balance (self gravity effect)*

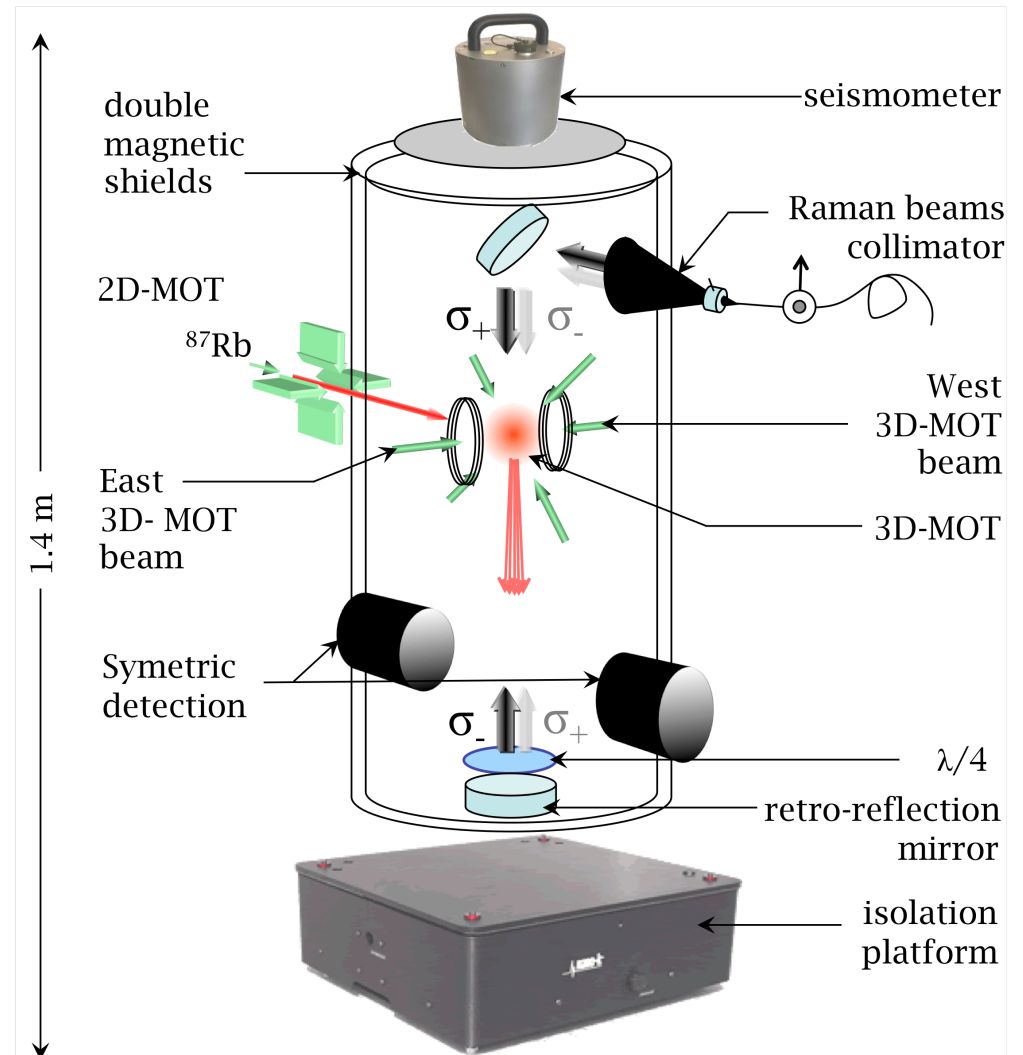
Calculation based on the one developed to determine the CAG SGE :

FEM

G. D'Agostino et al *Metrologia* **48** (2011)



Absolute gravimeter



Movable set up

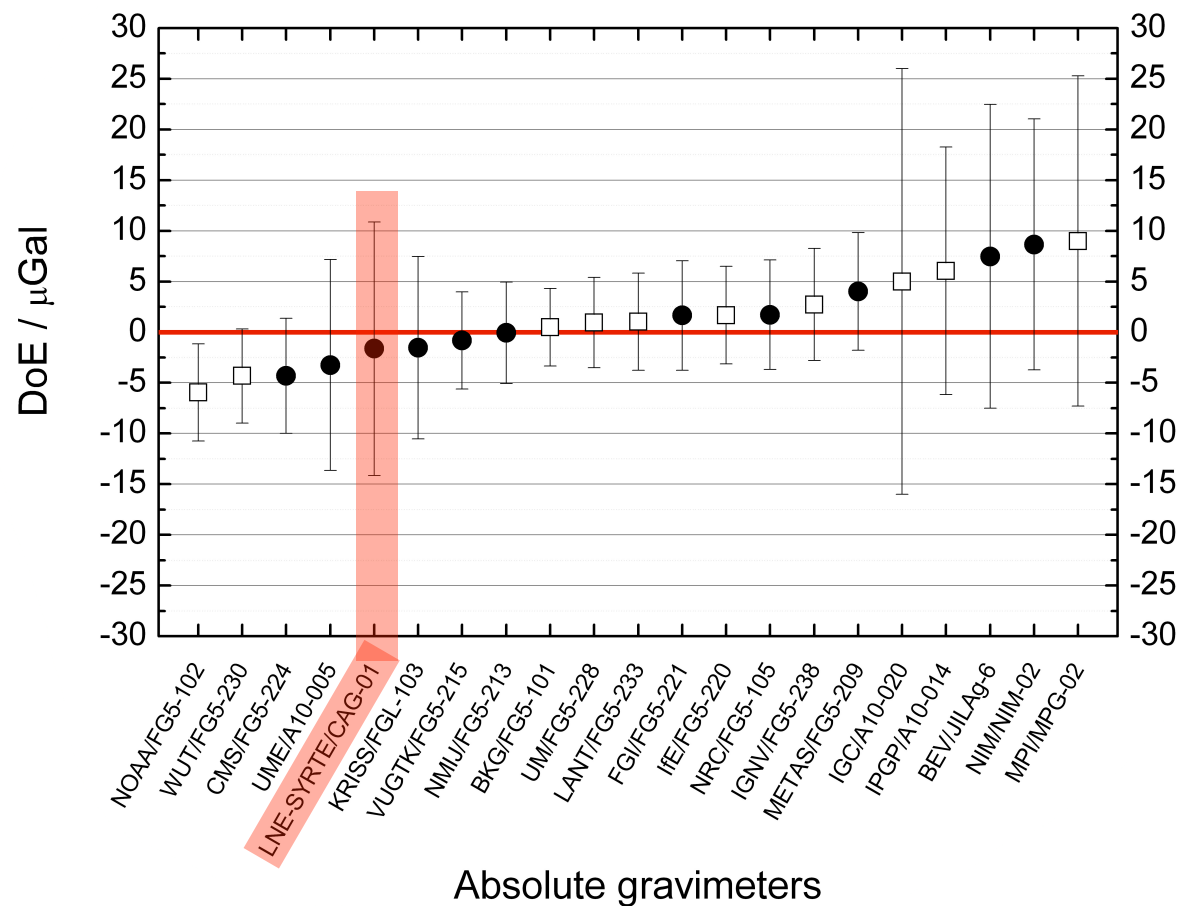


- Participation to international key comparisons: ICAG'09 (BIPM), ECAG'11(Lux), ICAG'13(Lux)



8 comparisons: 4 @ LNE; 7 with CAG

ICAG'09 (BIPM)



Z. Jiang et al *Metrologia* **49** (2012)
 S. Merlet et al *Metrologia* **47** (2010)
 A. Chauvet-Louchet et al *IEEE Trans. Instrum. Meas.* **60** (2011)
 O. Francis et al *Metrologia* **50** (2013)
 P. Gillot et al *Metrologia* **51** (2014)

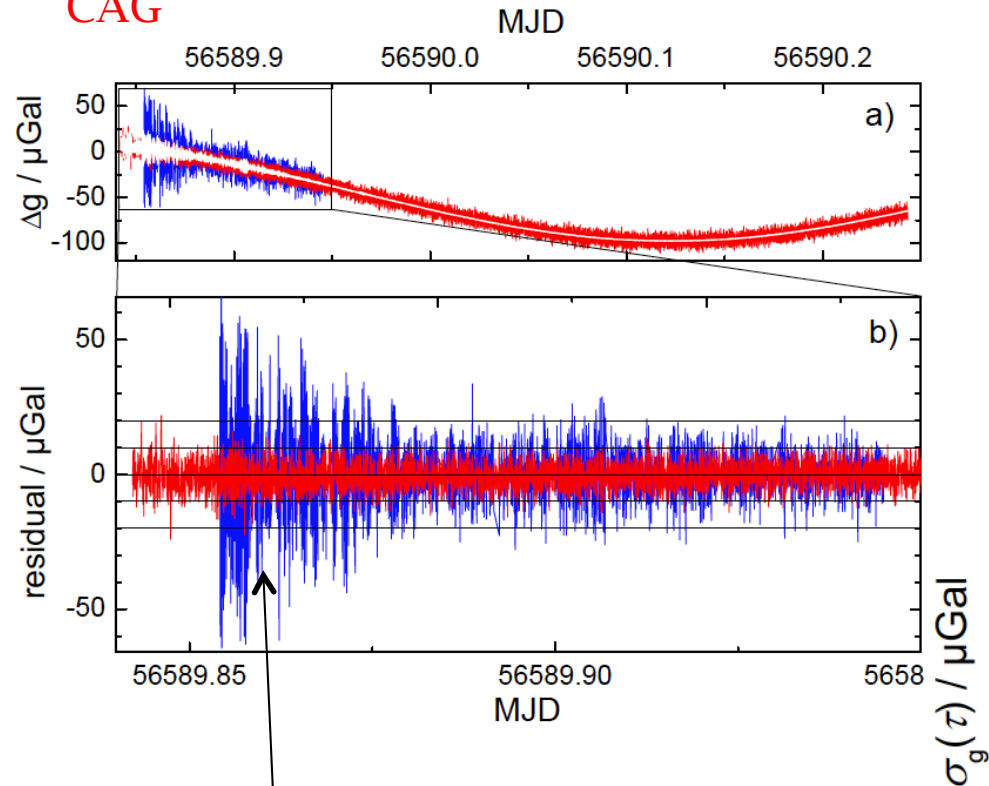
ECAG'11 (Walferdange Lux)

Effect	Bias μGal	u μGal
Alignments	2.4	0.5
Frequency reference	-4.6	<0.1
RF phase shift	0.0	<0.1
<i>vgg</i>	-10.3	<0.1
Self gravity effect	-1.3	0.1
Coriolis	1.3	0.8
Wavefront aberrations	0.0	4.0
LS1	0.0	<0.1
Zeeman	0.0	<0.1
LS2	-7.7	0.5
Detection offset	0.0	0.5
Optical power	0.0	1.0
Cloud indice	0.4	<0.1
Cold collisions	<0.1	<0.1
TOTAL	-19.8	4.3

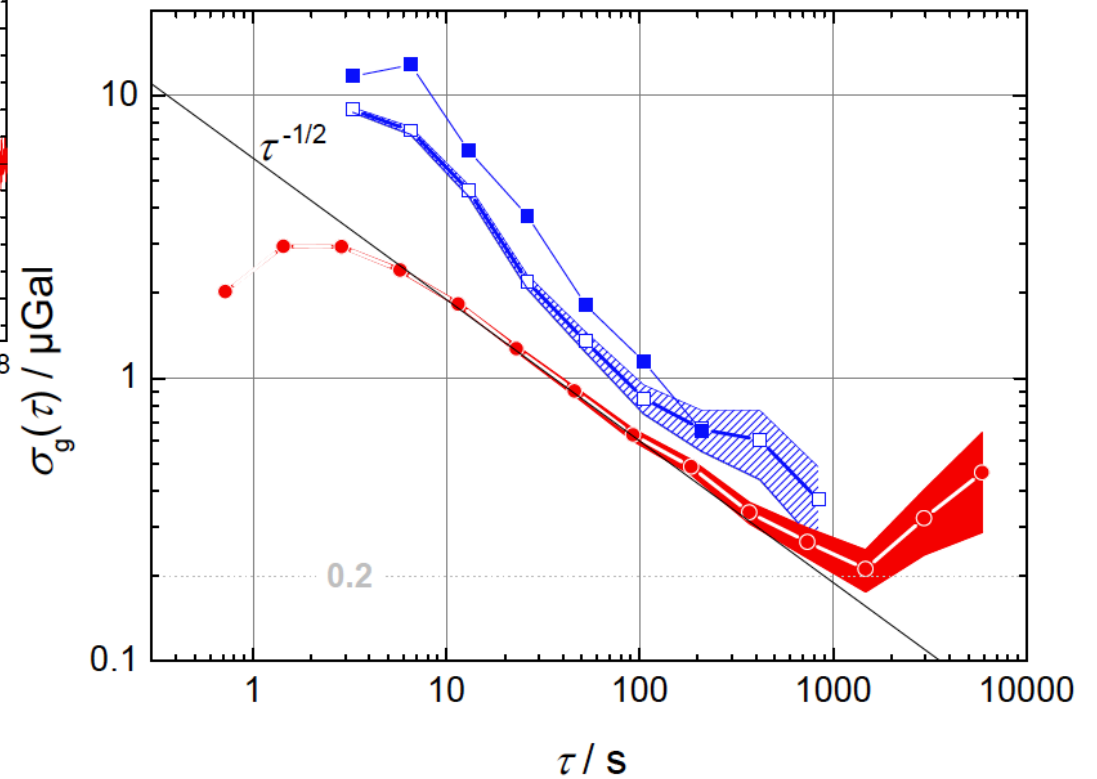
CAG sensitivity

FG5X#216

CAG



P. Gillot et al Metrologia **51** (2014)



Superconducting gravimeter iGrav-005

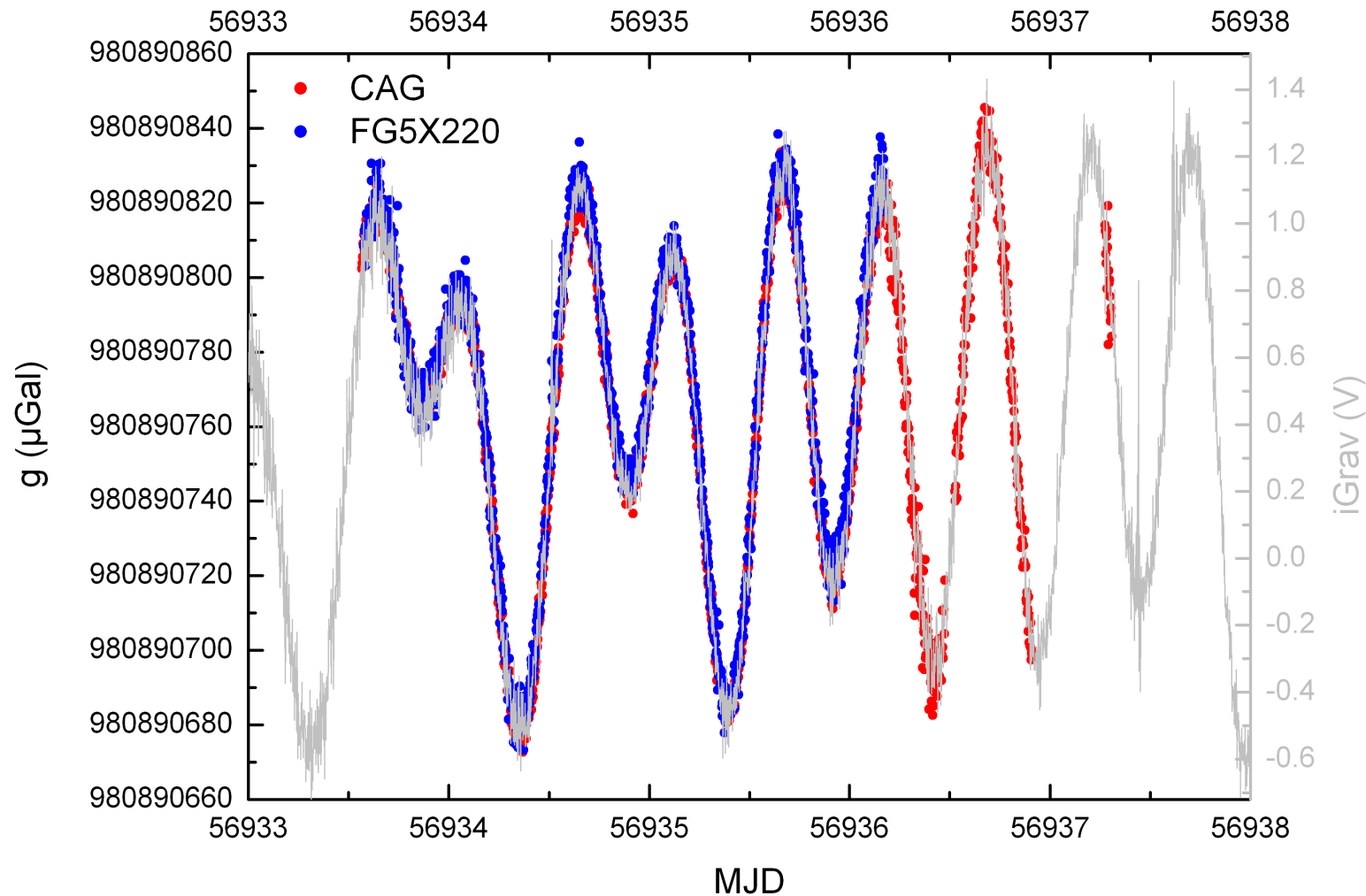
Operating since beginning of 2013

Installed on the same GR pillar than CAG

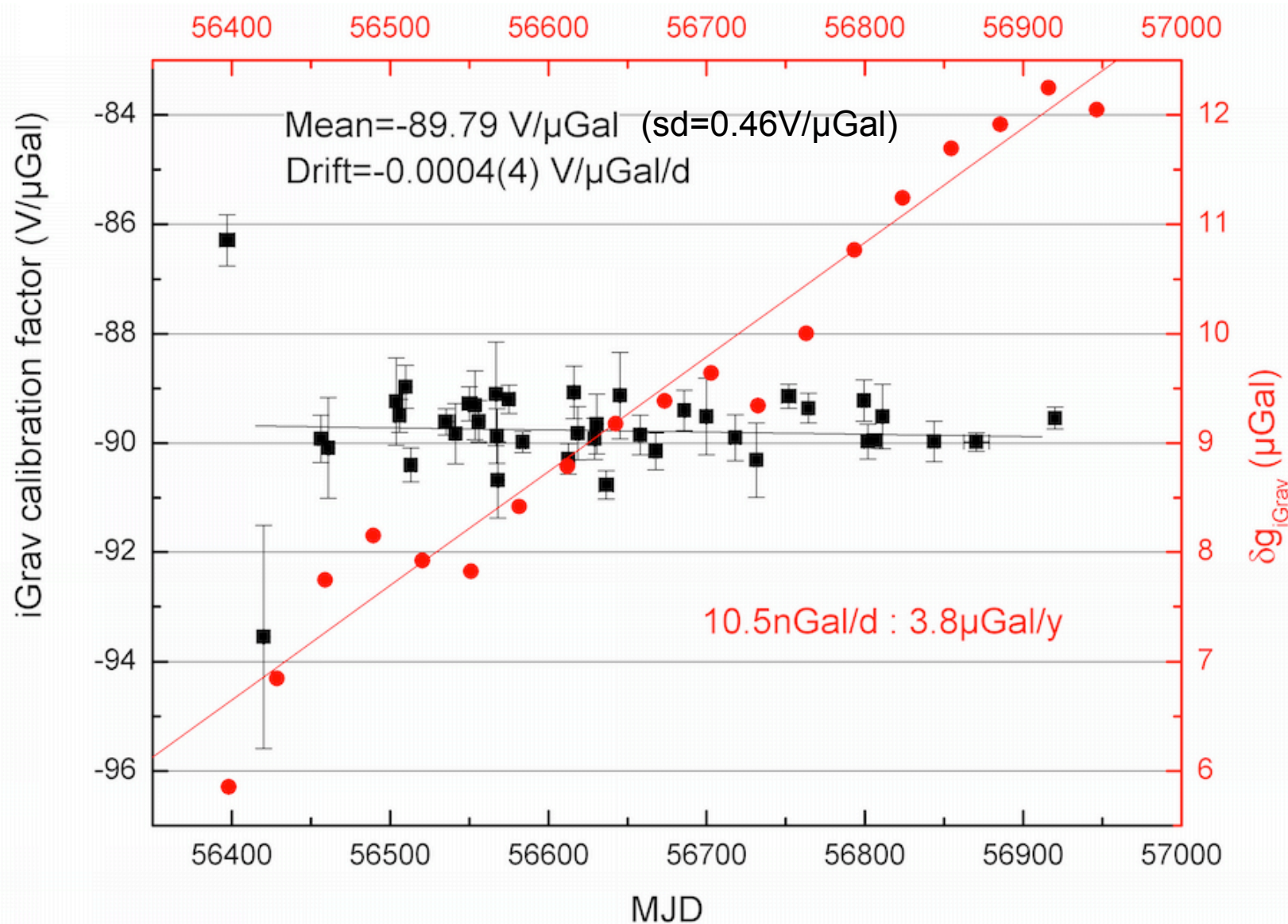


- *Study of long term stability of CAG*
- *Continuous g recording, back up for CAG*
- *No g variation model needed for WB (tides, pressure, ground water...)*

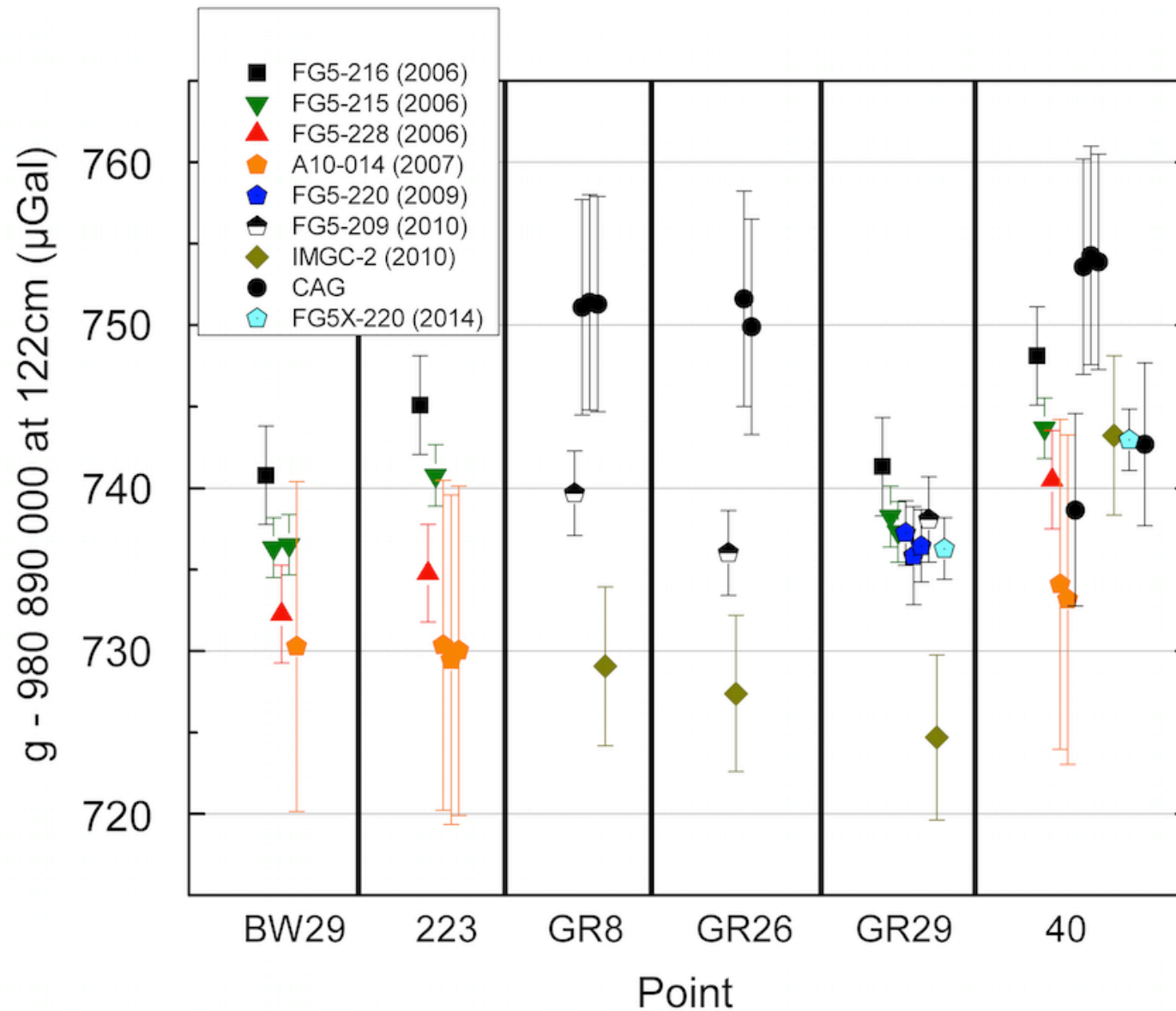
Comparison FG5X#220 and CAG Vs iGrav005



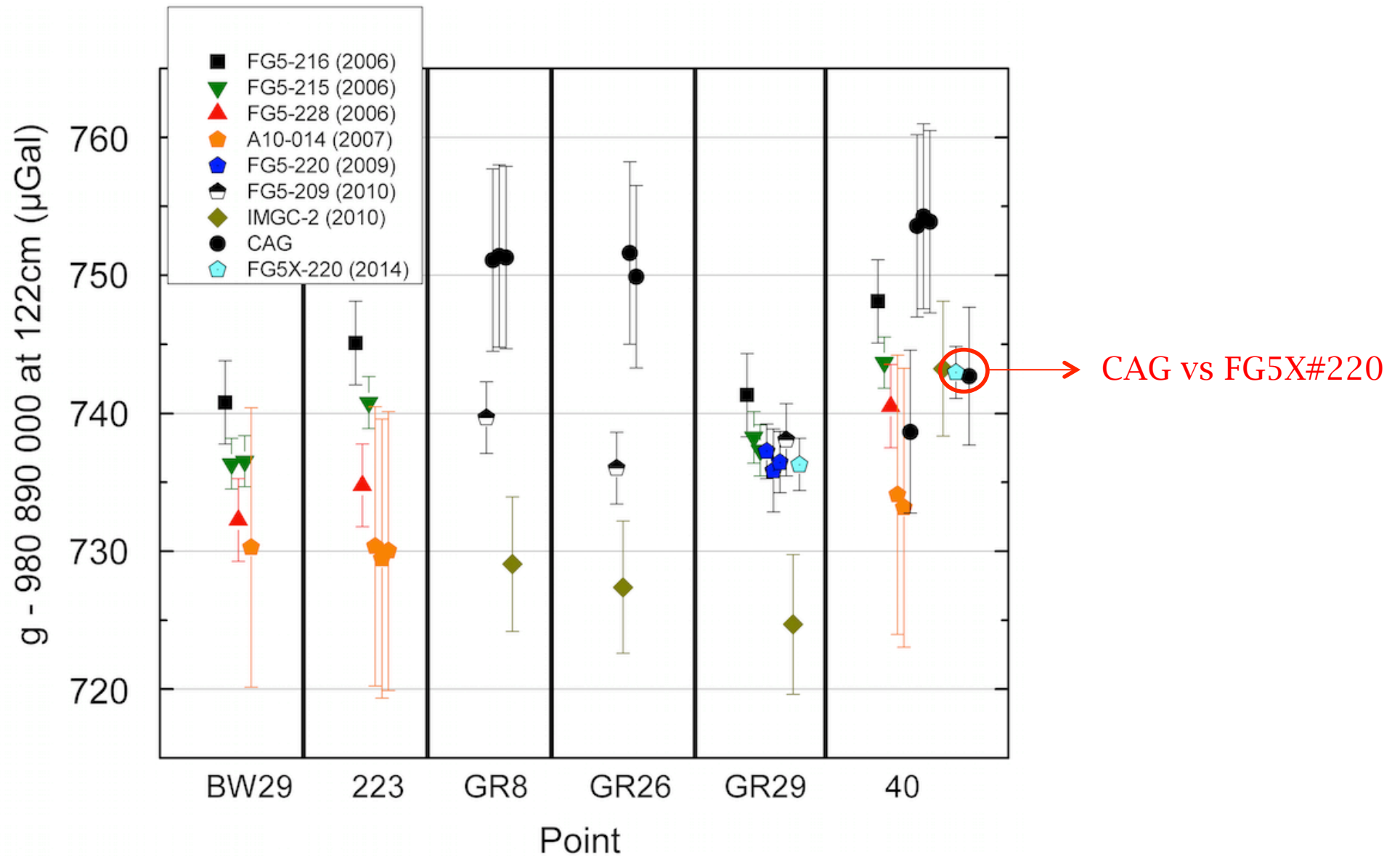
iGrav005 calibration factor and drift



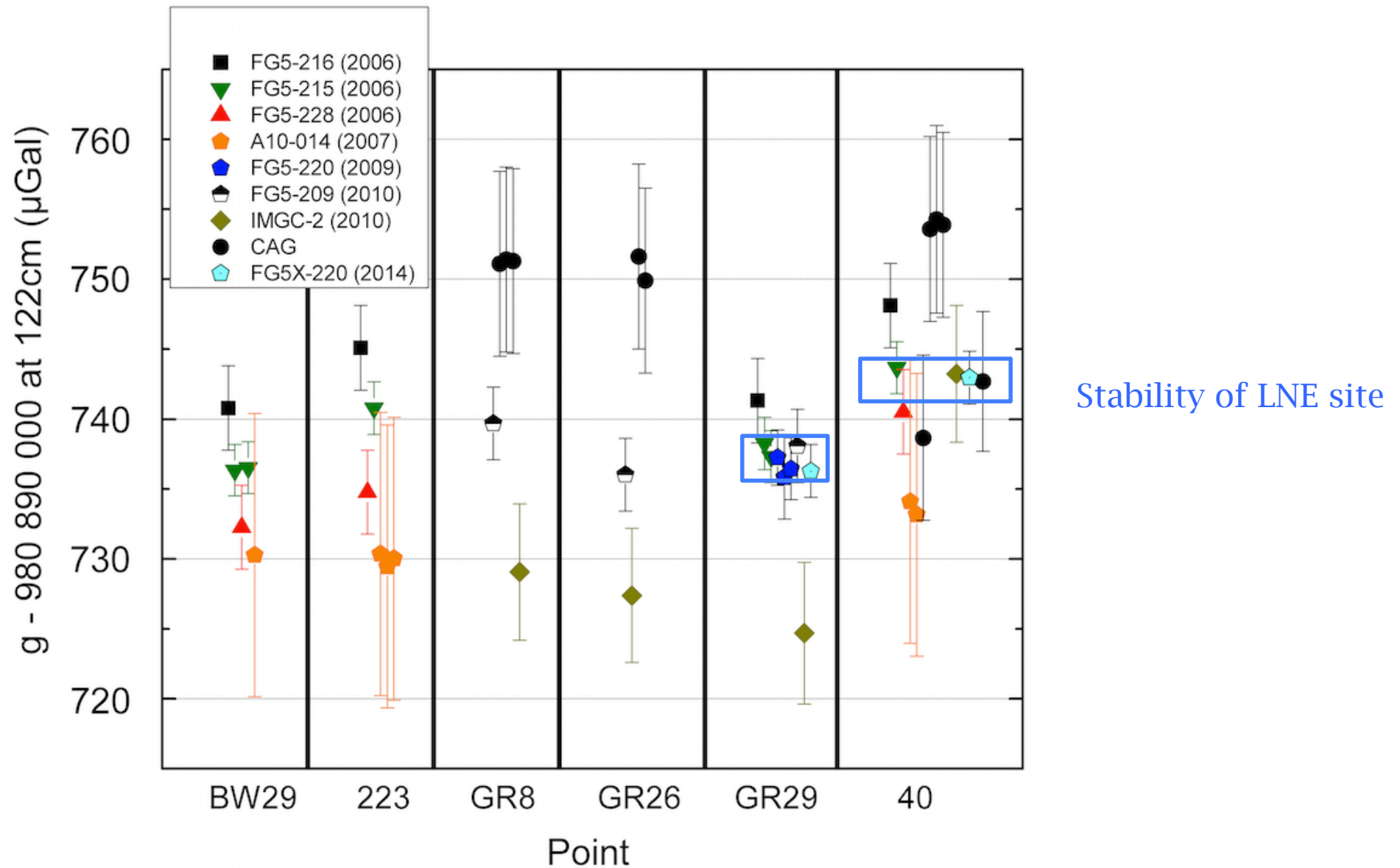
Absolute measurements @ LNE



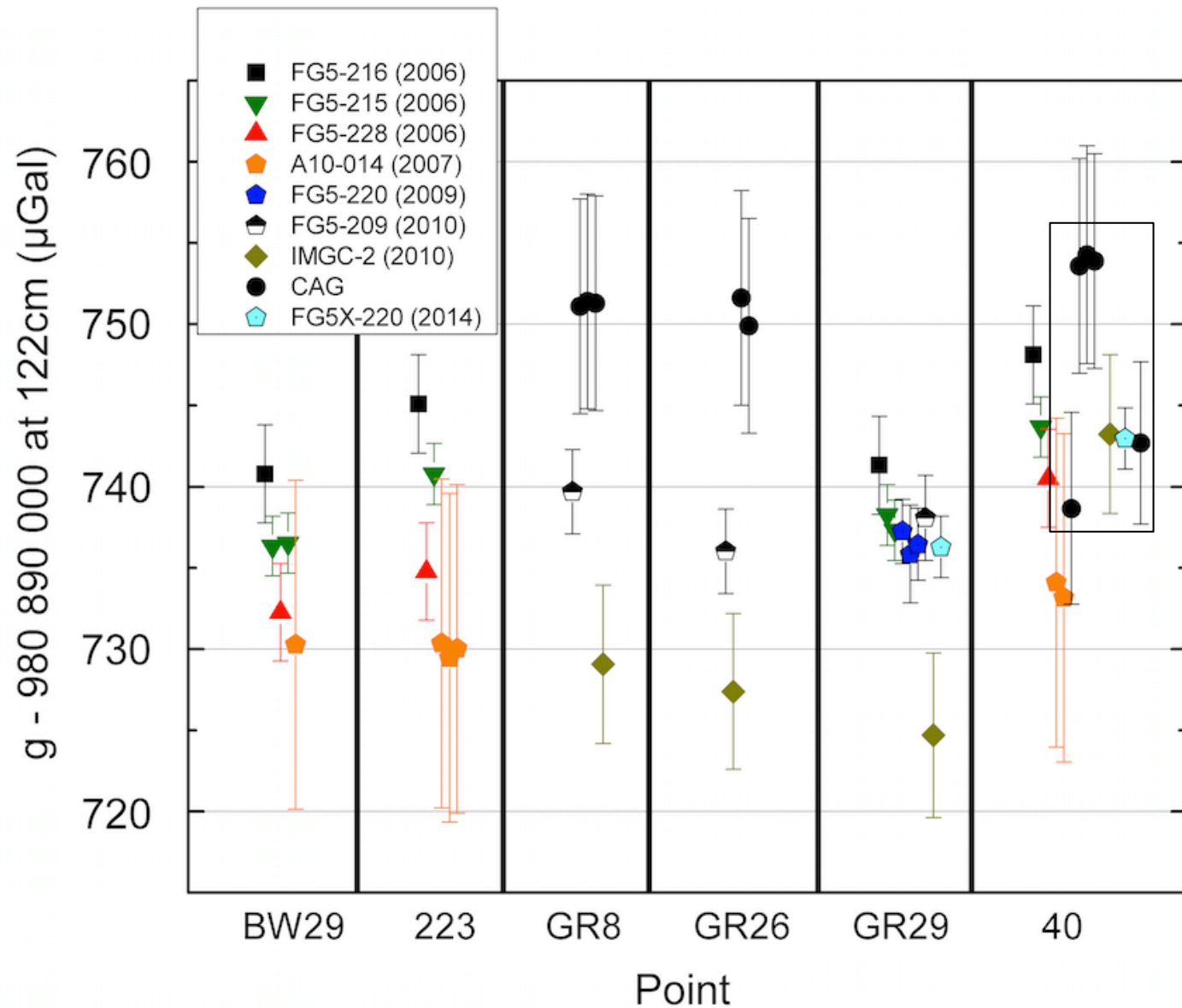
Absolute measurements @ LNE



Absolute measurements @ LNE



Absolute measurements @ LNE



Improvement of CAG

Prospects

Kilogram: a definition to change, when ? CGPM 2018 ?

h with BW ? with N_A ? With both ? → *solve the discrepancies*

LNE Watt balance → *international comparison with IPK in 2015*

→ *in air : 1×10^{-7} in 2015*

→ *in vacuum : $< 1 \times 10^{-7}$ in 2016-2017*

→ *participation to the kilogram redefinition ?*

CAG improvement: → *decrease uncertainty to $1 \times 10^{-9}g$*

→ *improve the sensitivity with the iGrav*

Provide a continuous absolute g value for the LNE Planck constant determinations

Continue to compare the CAG with other AG (CC and AI)

Continuous g measurements for years



Thank you for your attention



http://synte.obspm.fr/tfc/capteurs_inertiels/