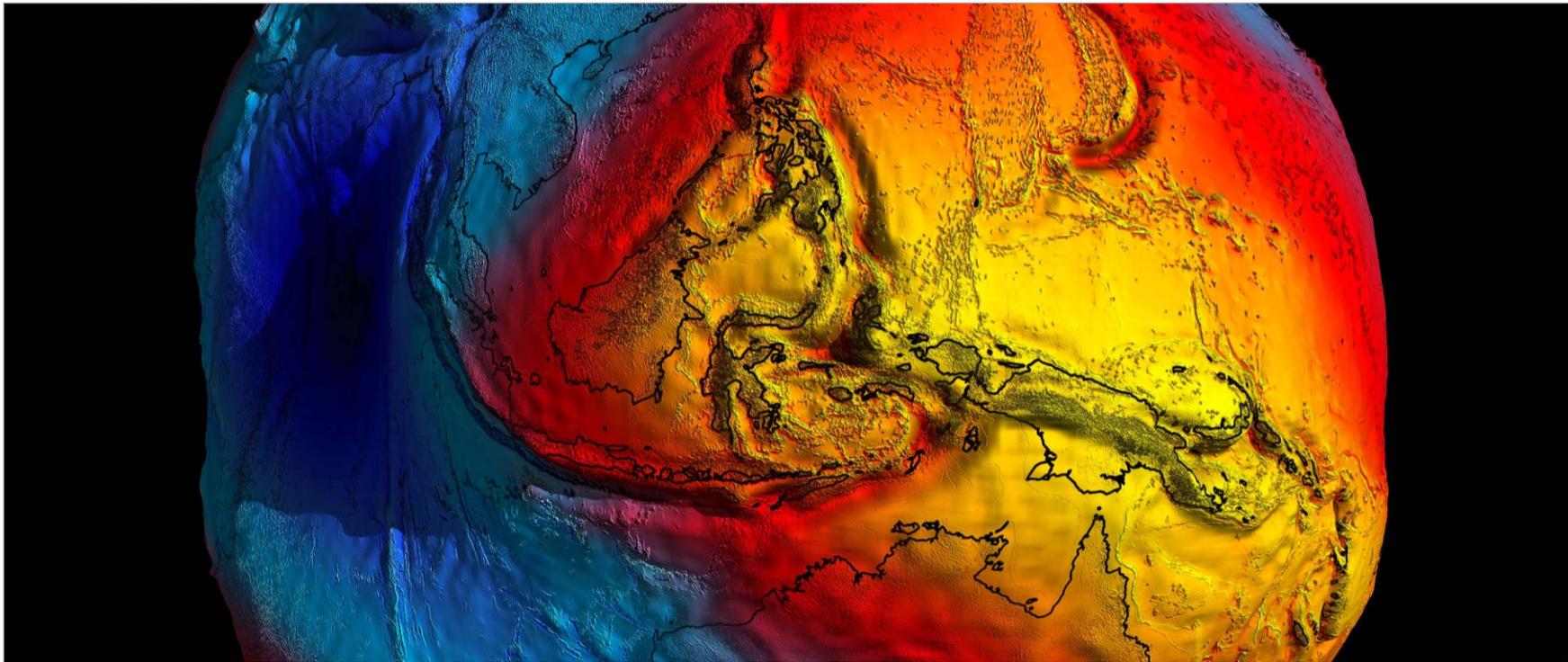
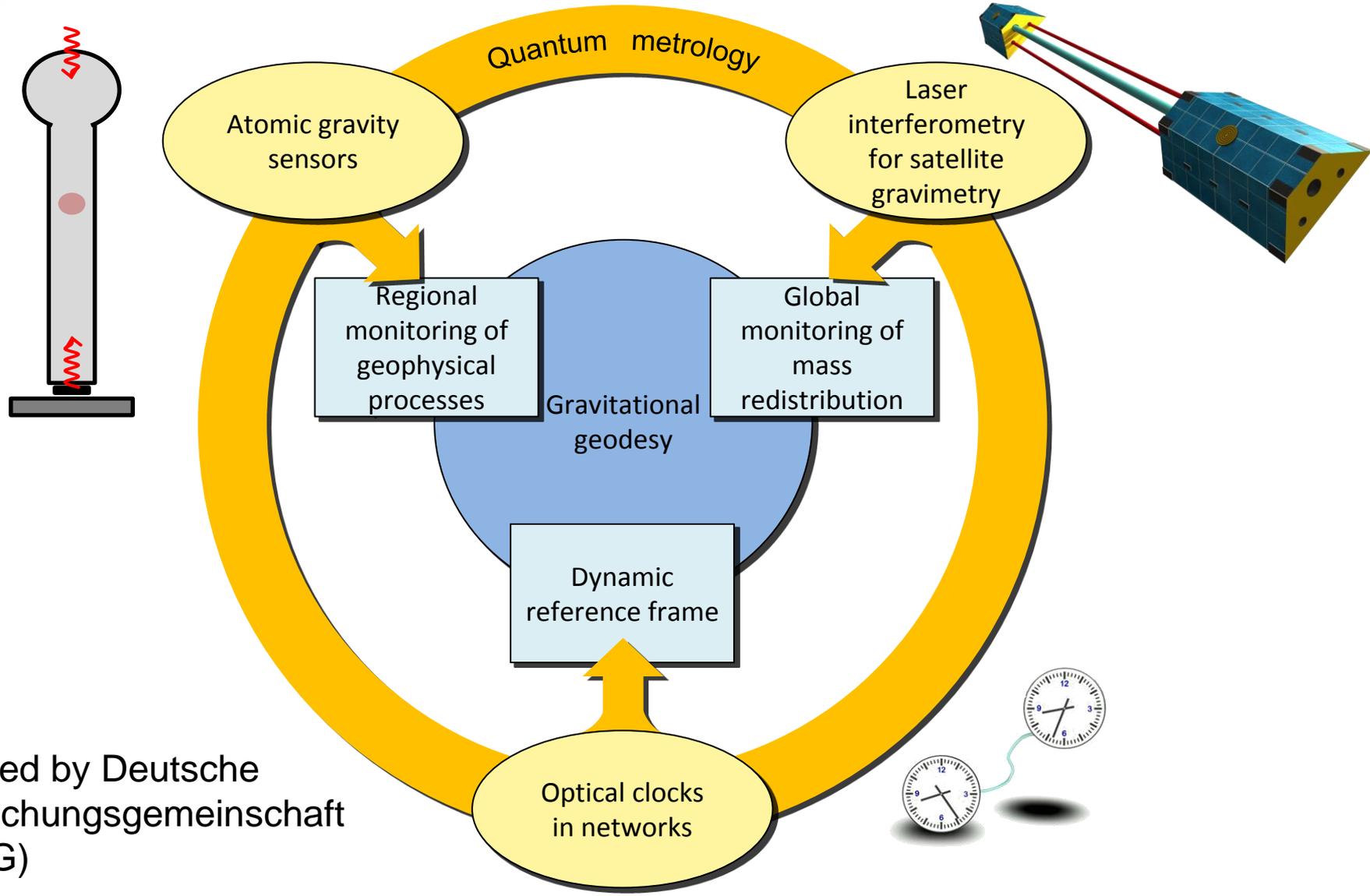




Relativistic Geodesy and Gravimetry with Quantum Sensors

Jakob Flury, Institut für Erdmessung (IfE) / Centre for Quantum Engineering and Space-Time Research (QUEST), Leibniz Universität Hannover

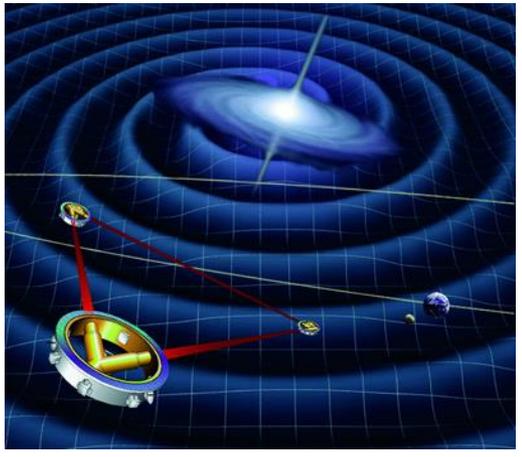
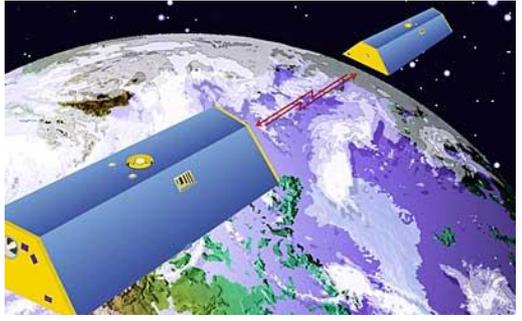
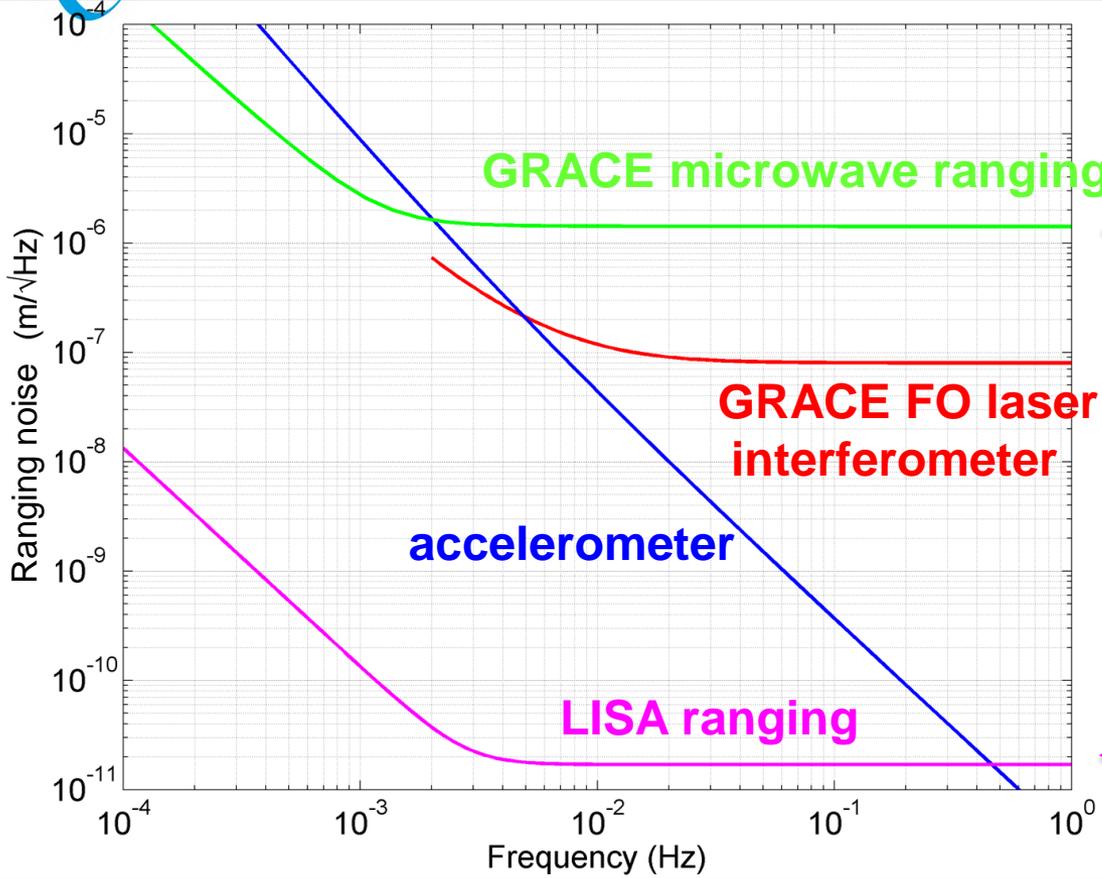




funded by Deutsche
Forschungsgemeinschaft
(DFG)

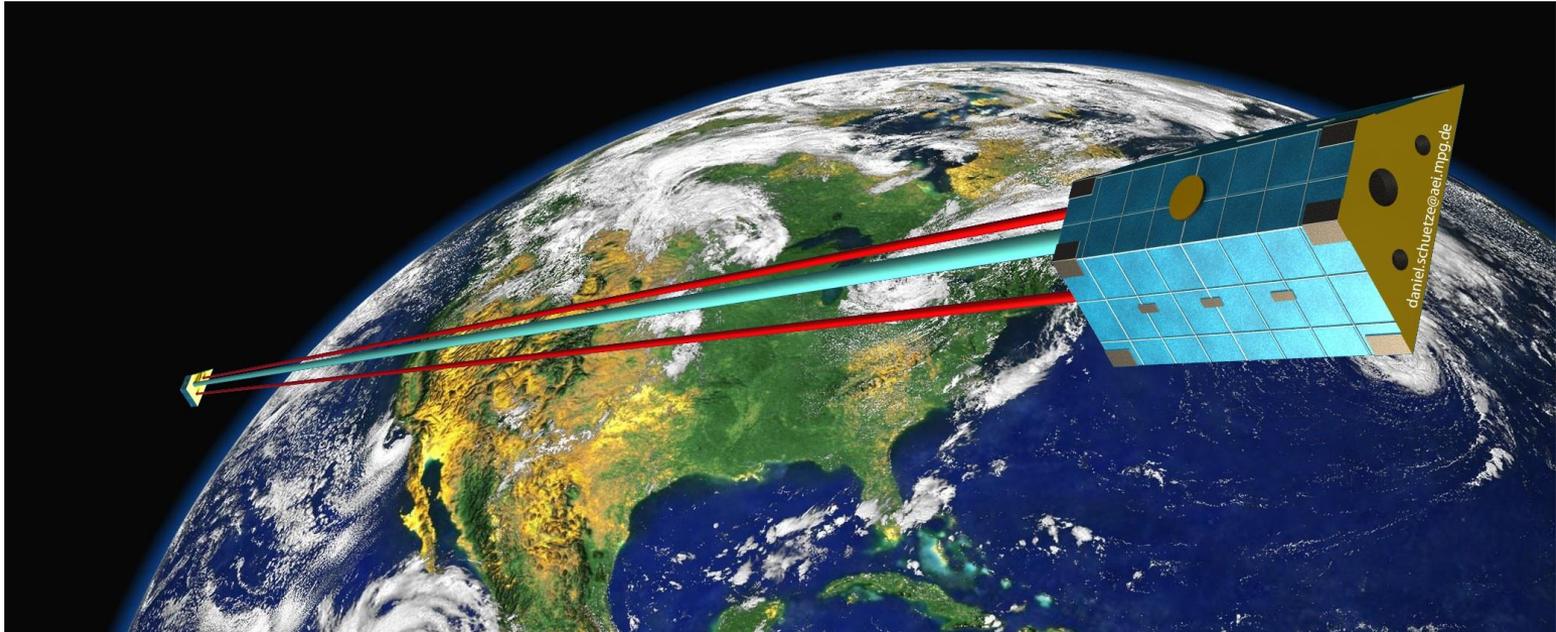


Laser interferometric ranging



- very **low ranging noise** levels achievable in outer space
- **challenge: laser interferometry in Earth orbit**
- different environmental conditions, different target quantity: the **Earth gravitational field!**

First laser interferometer between Earth orbiters



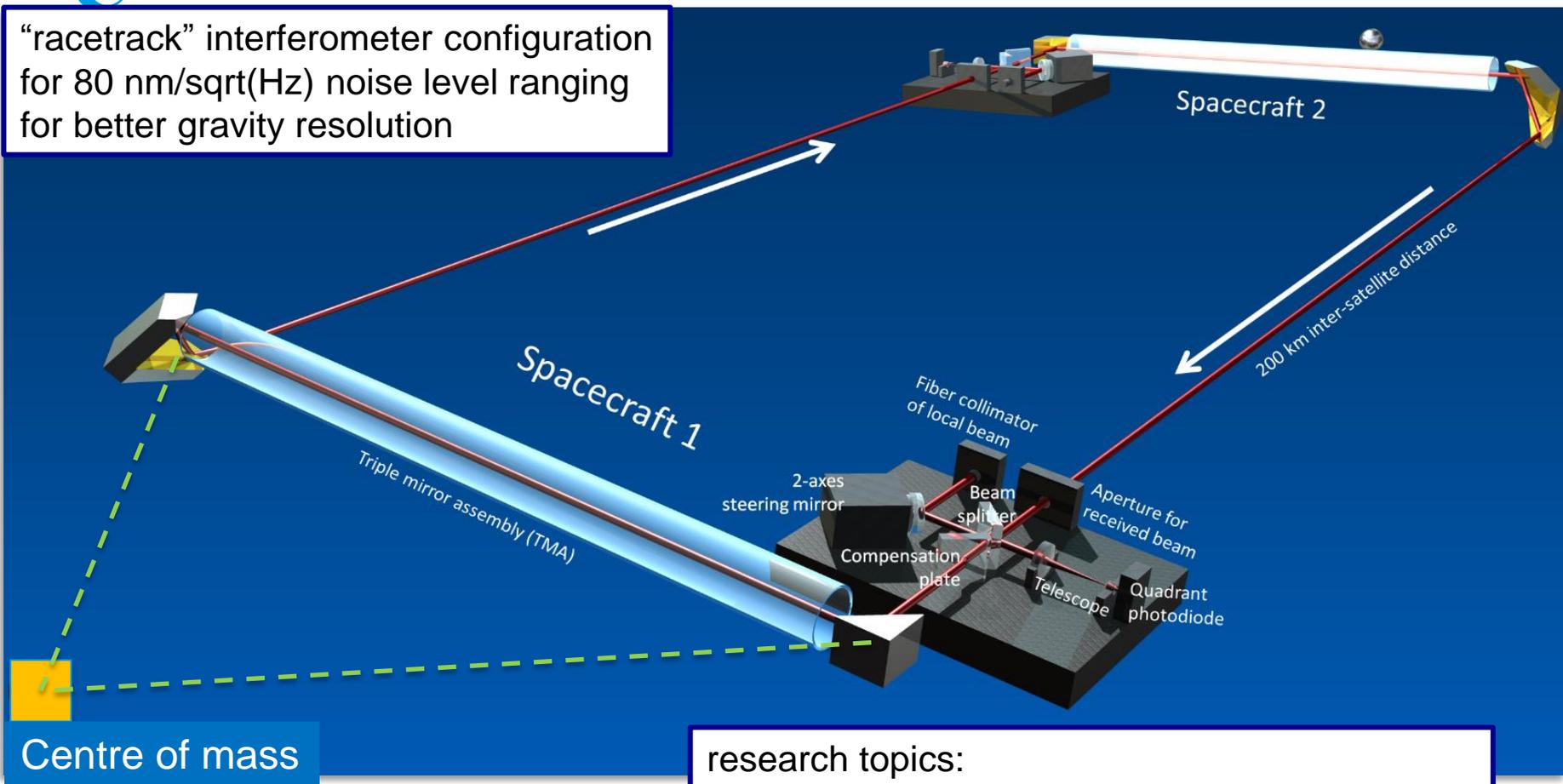
GRACE Follow-On mission 2017-2022

- experimental **demonstrator** on GRACE reflight
- design completed (NASA-JPL / AEI Hannover, group of Karsten Danzmann, Gerhard Heinzel)
- construction started
- **test case for exploring and understanding optical gravimetry in Earth orbit**

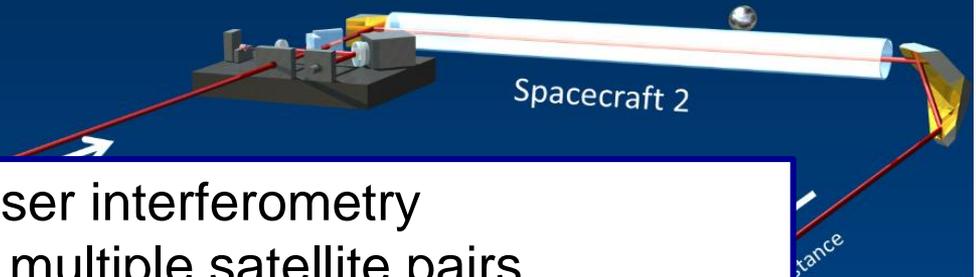


GRACE-FO Laser Ranging Interferometer (LRI)

“racetrack” interferometer configuration for 80 nm/sqrt(Hz) noise level ranging for better gravity resolution



- research topics:
- initial signal acquisition,
 - differential waveform sensing,
 - beam steering for better pointing control
 - pointing jitter, optical pathlength
 - combining μ wave with LRI
 - sensor fusion, data analysis



- future missions will use laser interferometry
- dramatic improvement by multiple satellite pairs
- long lead time of space missions

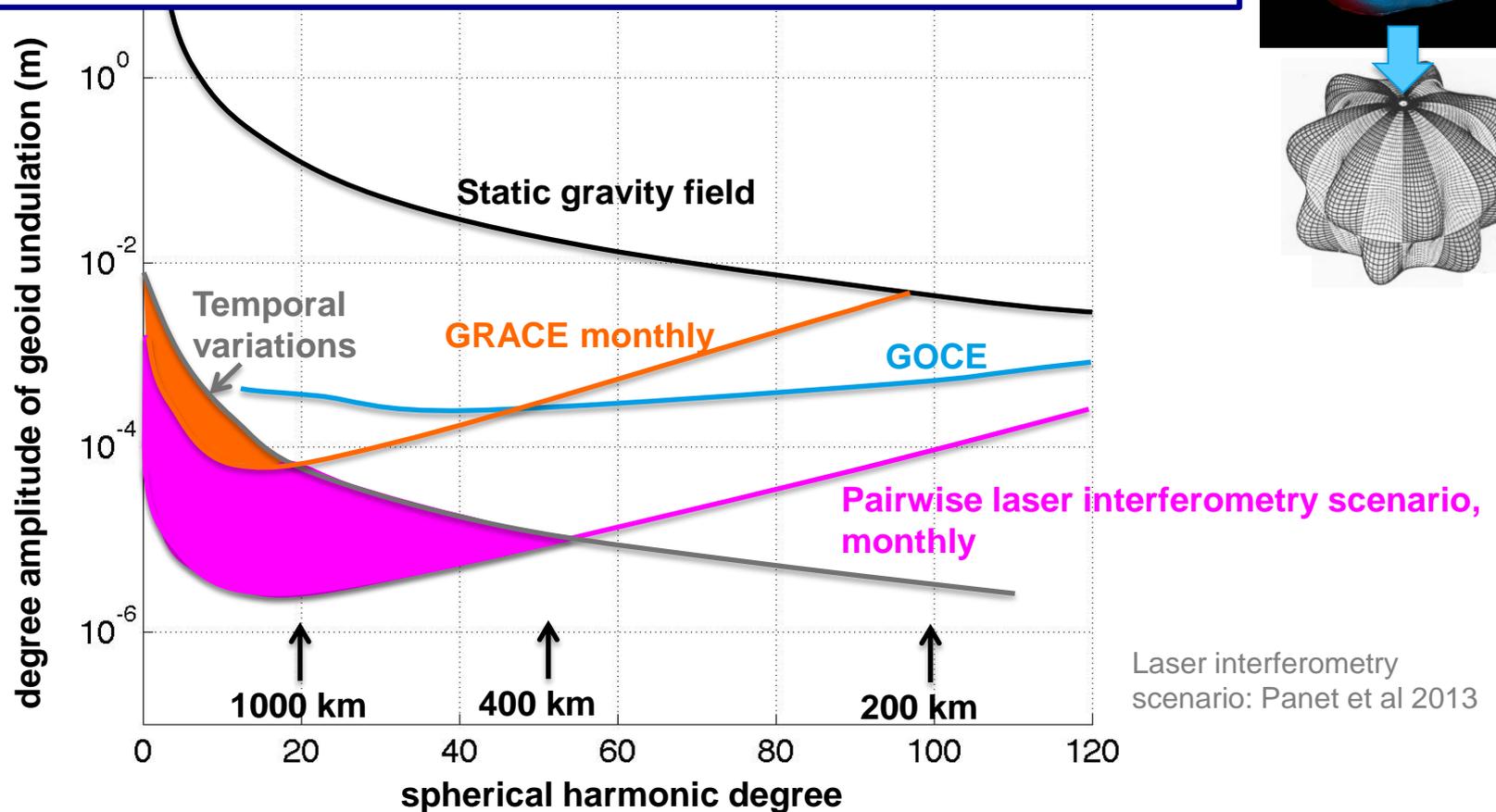
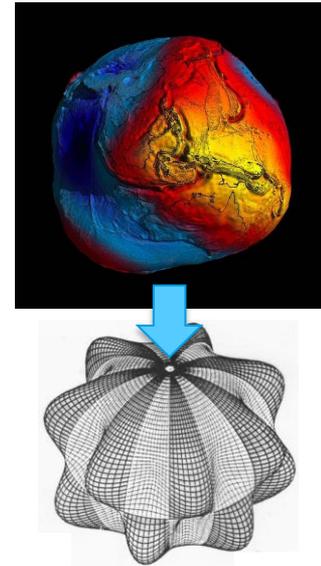
science challenges:

- optical testmass readout
- interferometer configuration
- phase meters
- pointing jitter
- straylight
- system modeling
- environmental and platform effects
- ...

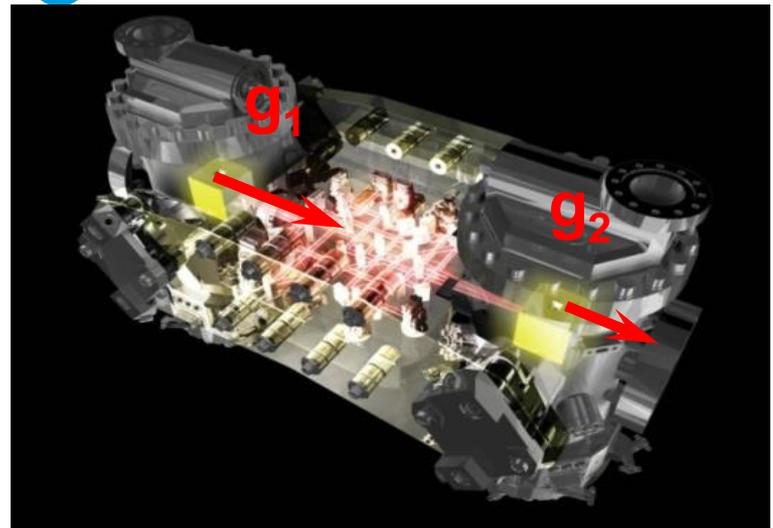


Enhanced resolution in gravity modeling

- **laser interferometry between satellites** is capable to recover temporal gravity and mass variations with significantly higher **spatial resolution**
- allows quantifying highly **relevant geophysical processes**



Optical gradiometry



LISA Pathfinder



GOCE

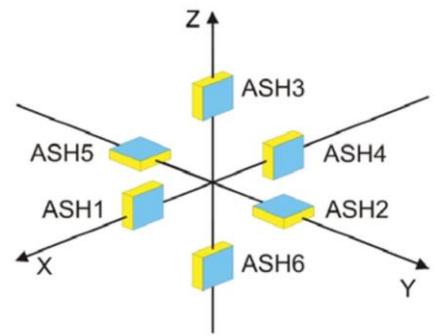
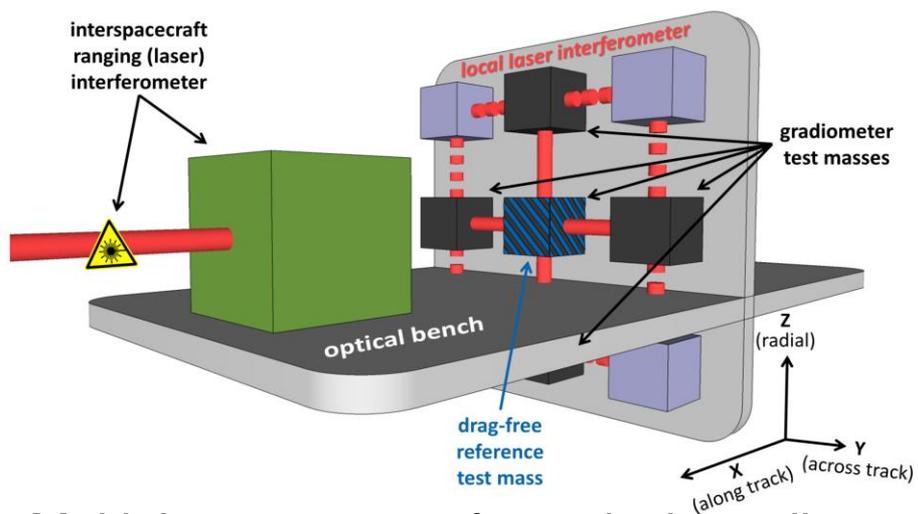
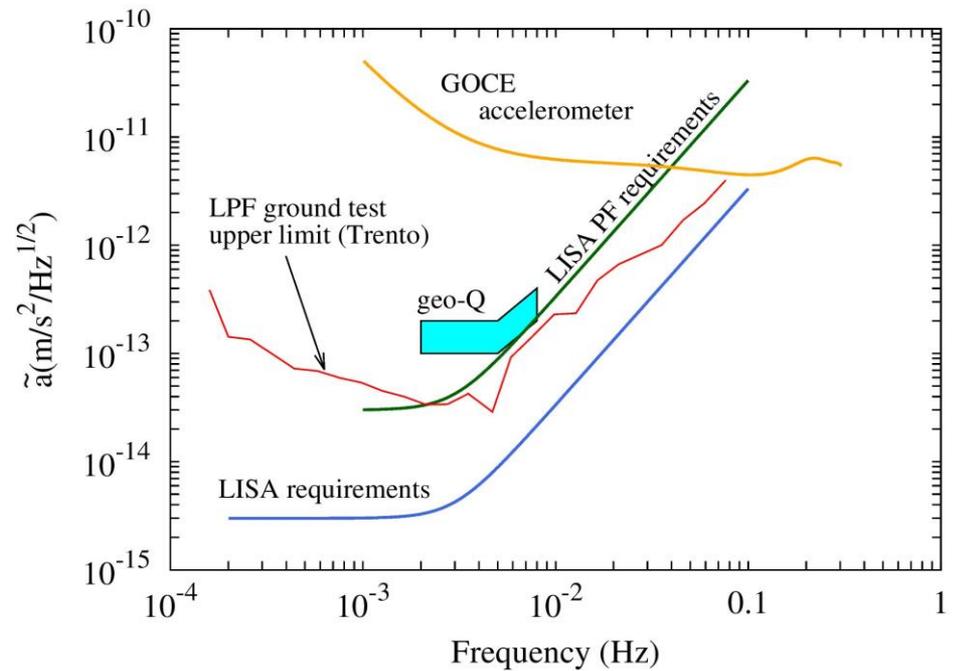


Image credit: ESA

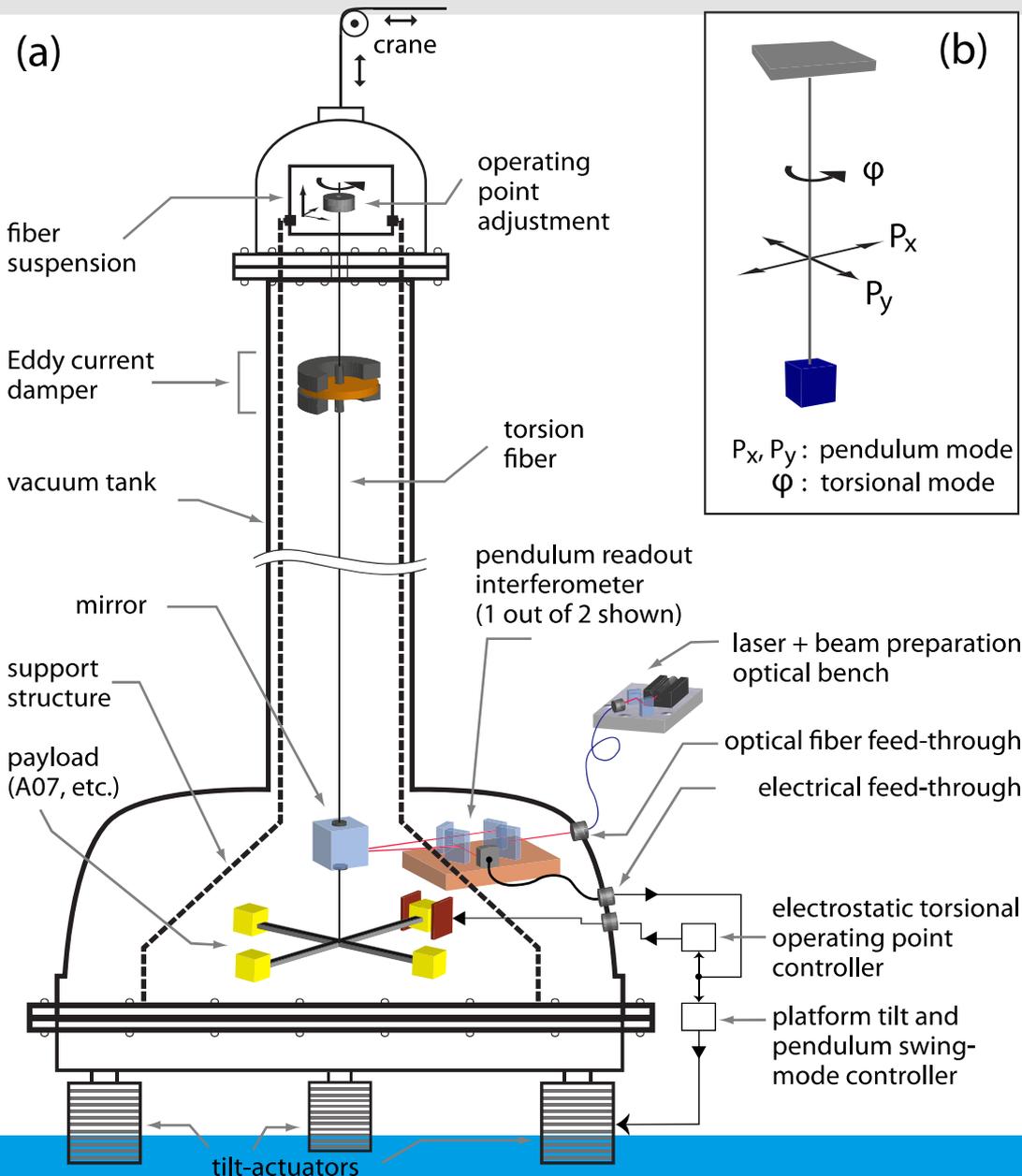


Multiple testmasses for optical gradiometry

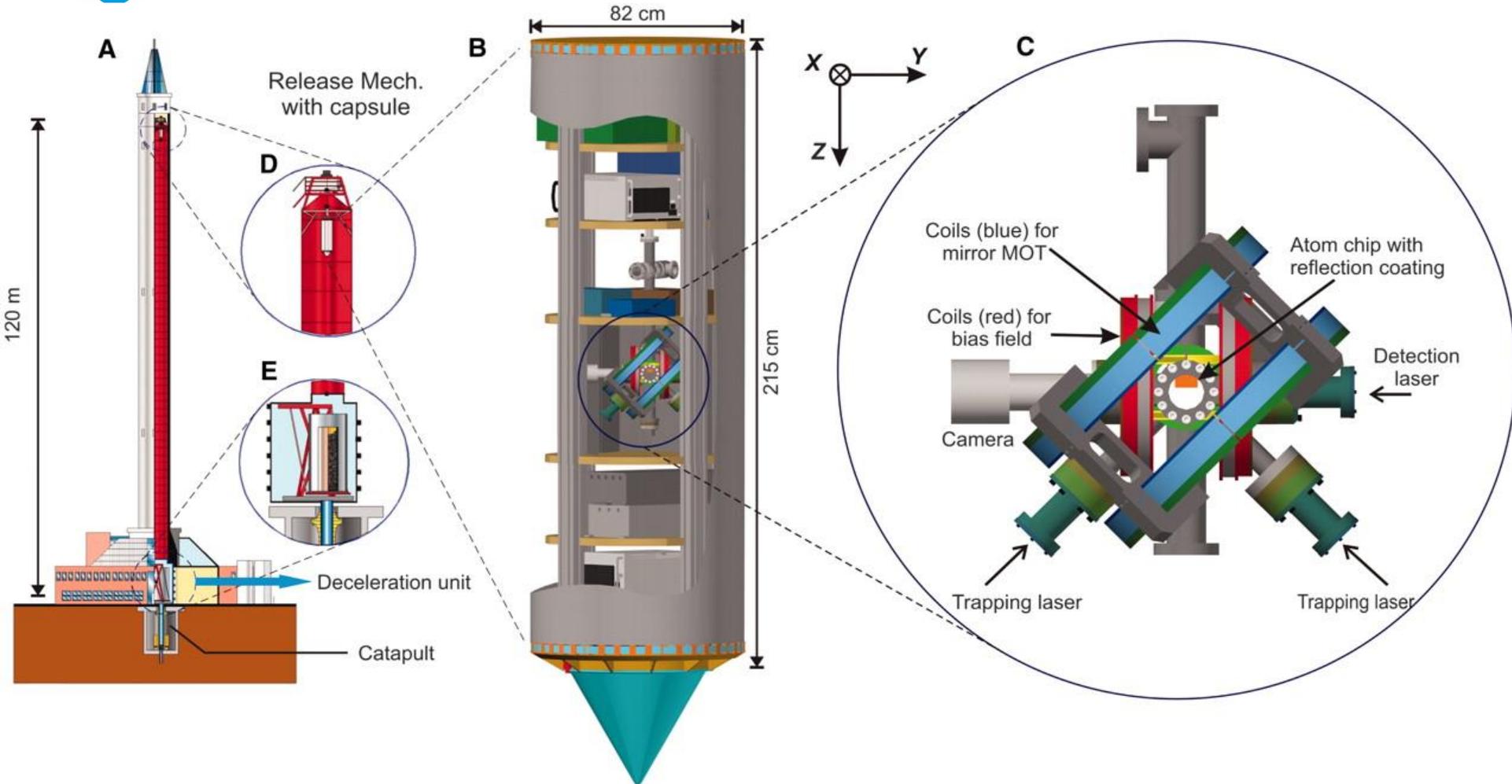


GOCE accelerometer performance using data from:
 Stummer, Claudia S.: PhD Thesis, DGK, Reihe C, Heft 695
 Torsion pendulum measurement data: courtesy of W.J. Weber, Trento

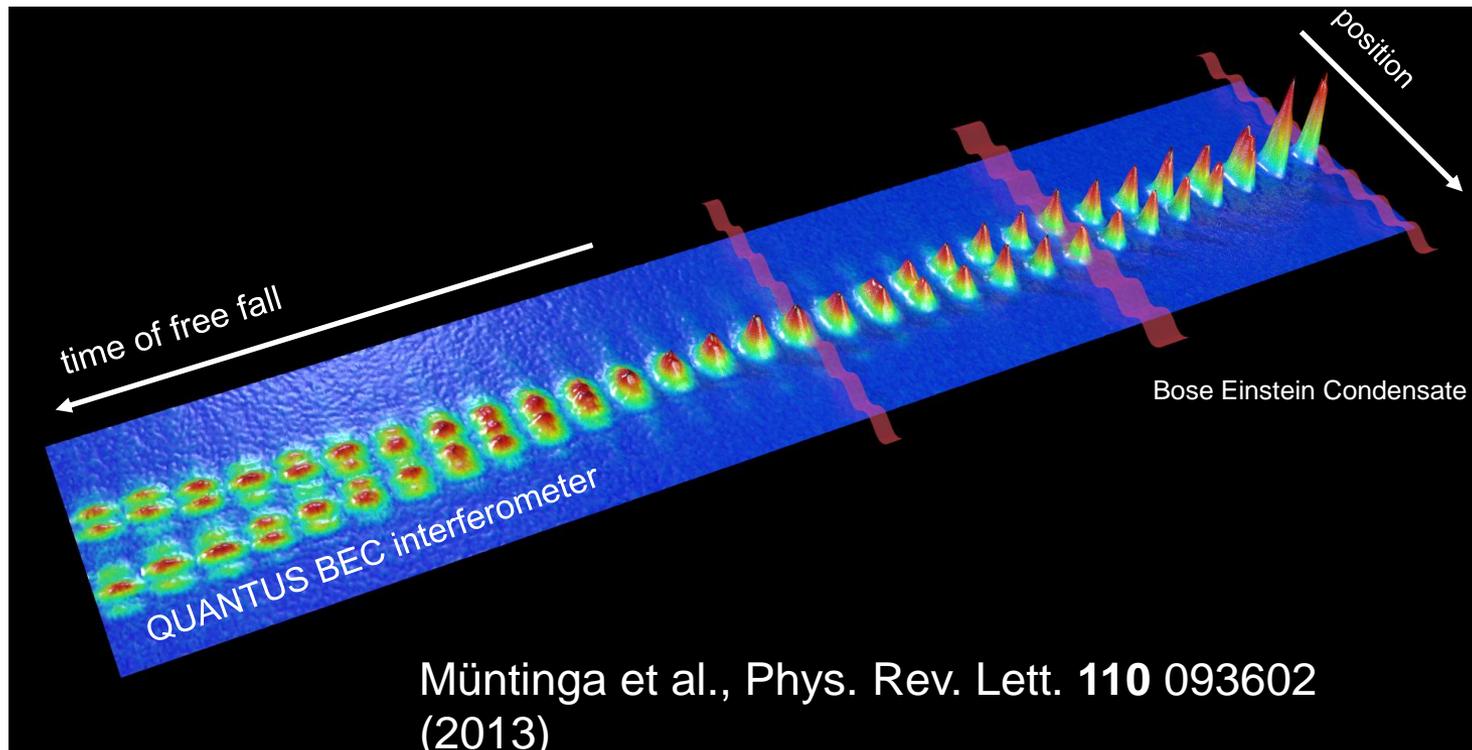
Torsion balance as test environment

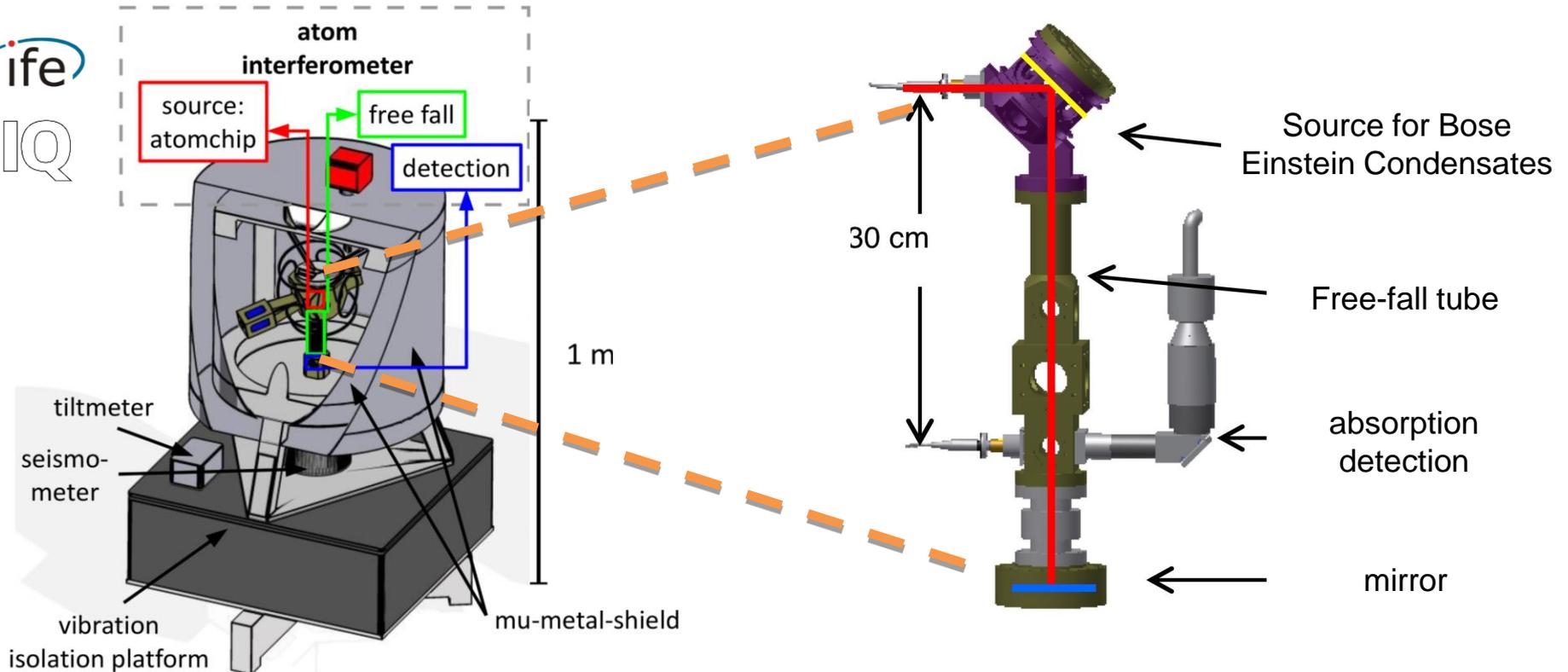


- test sensitivity to spurious forces
- test mass readout
- multi-testmass / multi-channel interferometry (> 20 degrees of freedom)



- QUANTUS experiments for quantum gases in microgravity
- DLR project in Bremen drop tower
- group of Ernst M. Rasel, Wolfgang Ertmer

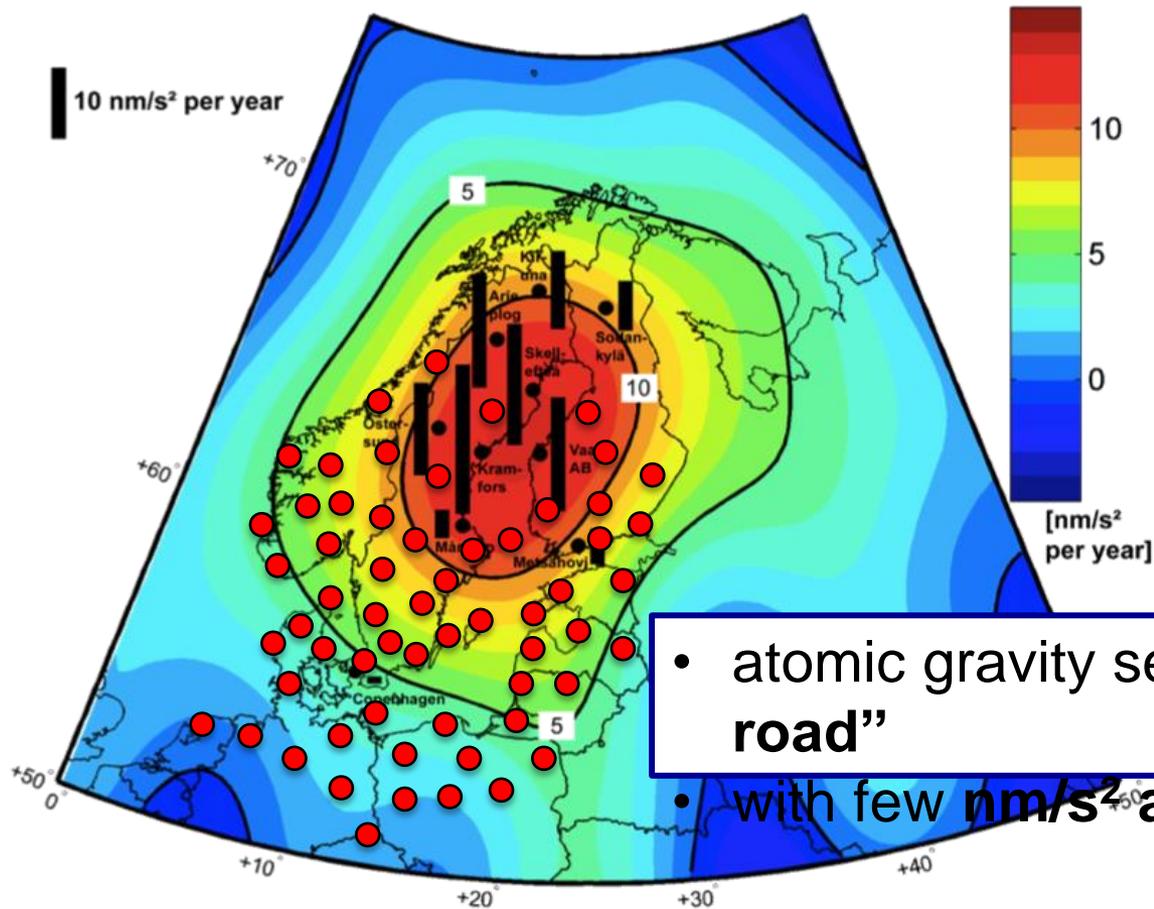




Hannover approach:

- chip atom source
- ultra-cold atoms in transportable setup, Bragg interferometry
- sub- μ Gal perspective for compact field devices

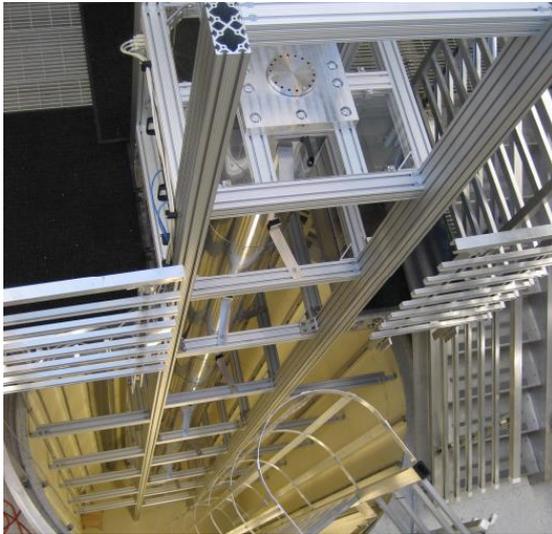
Compact sensors: long term perspective



- atomic gravity sensors “for the road”
- with few nm/s² accuracy

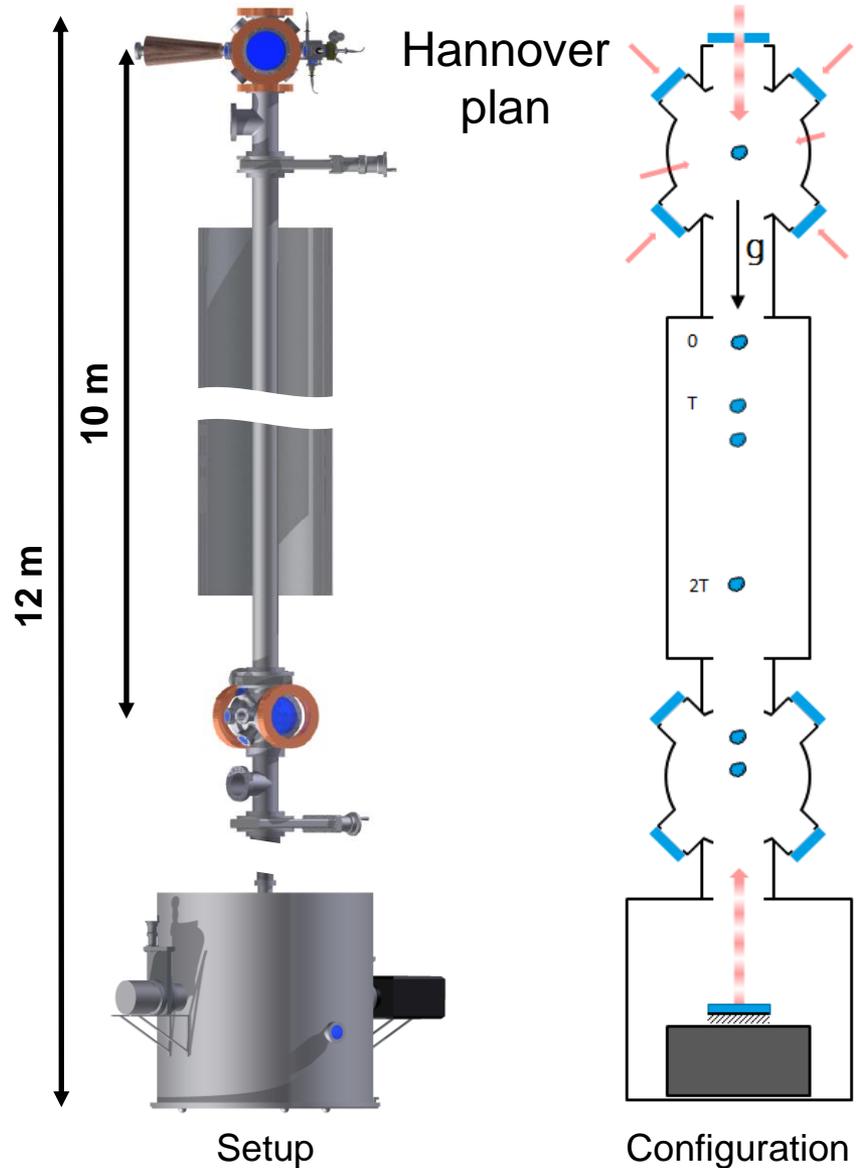


Very long baseline atom interferometry (VLBAI)

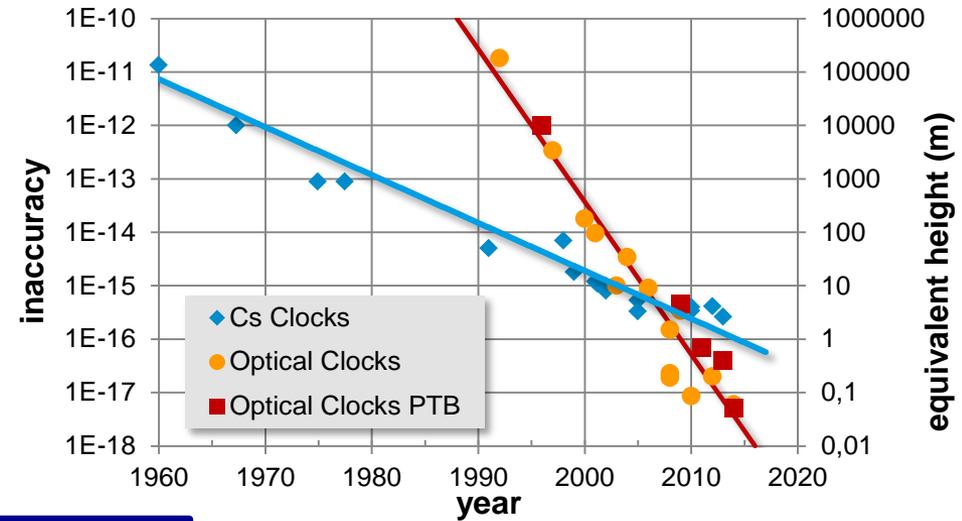
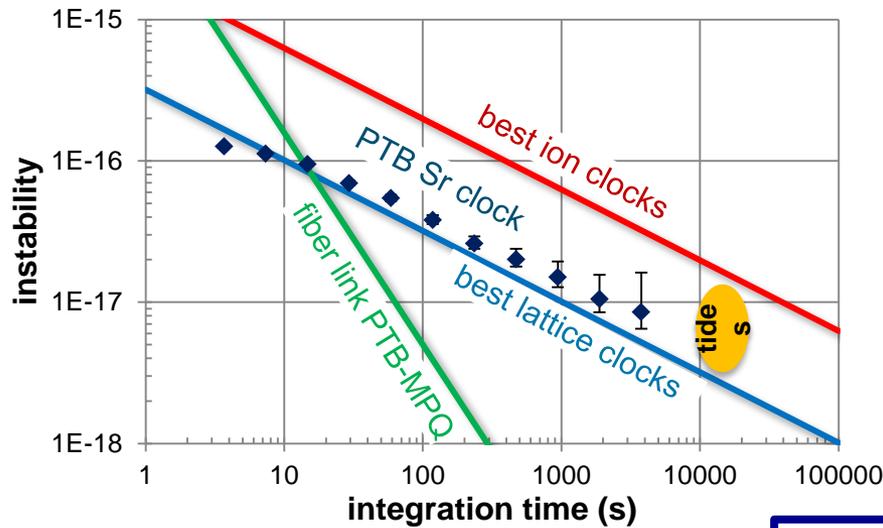


Stanford
10 m atom
fountain

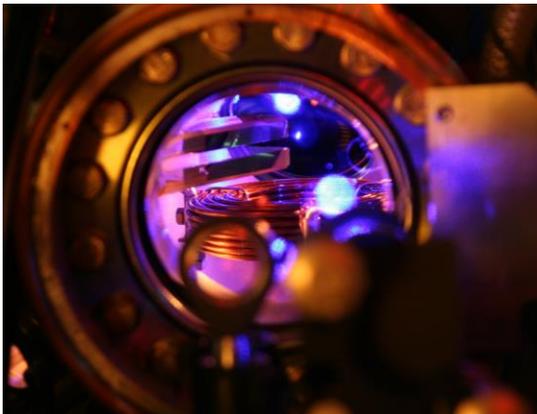
- Stanford, MIGA
- sensitivity $\sim T^2$
- 1 sec $\sim 10^{-13}$ m/s²
- challenges: VLBAI
gravimetry, gradiometry
and fundamental physics



State of the art optical clocks

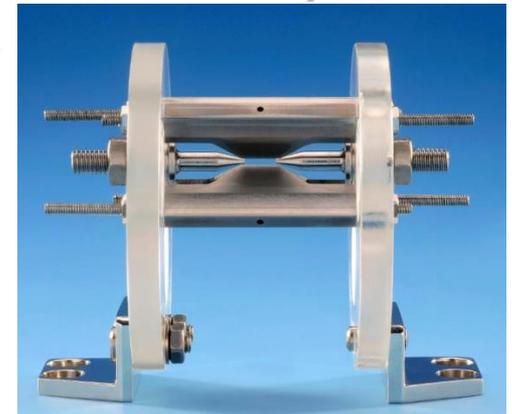


Sr lattice clock: **stable**



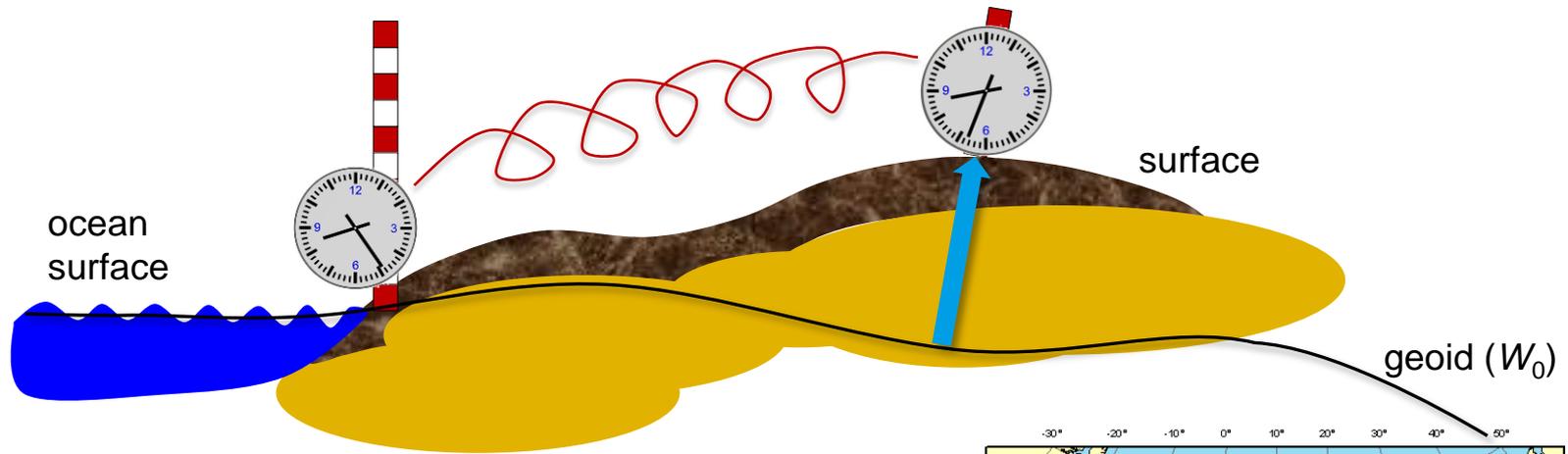
$$DW = \frac{Df}{f} c^2$$

Al⁺ clock: **reproducible**

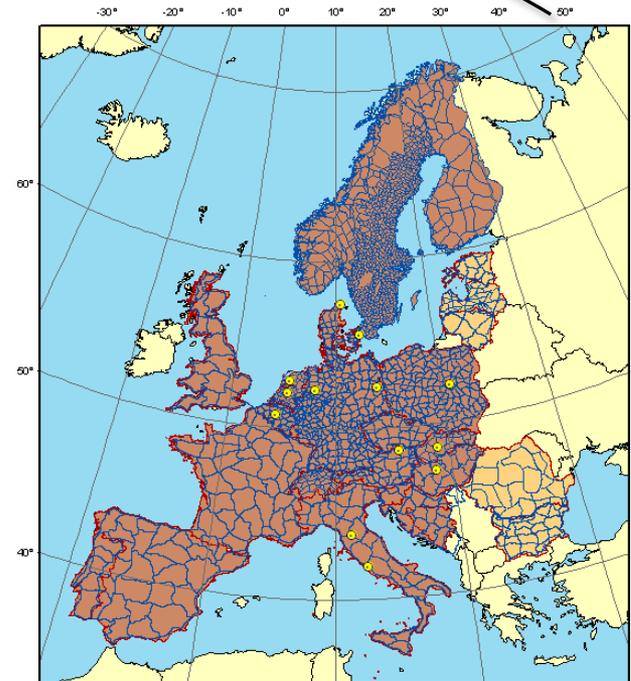


Hybrid Clock:
stable & reproducible

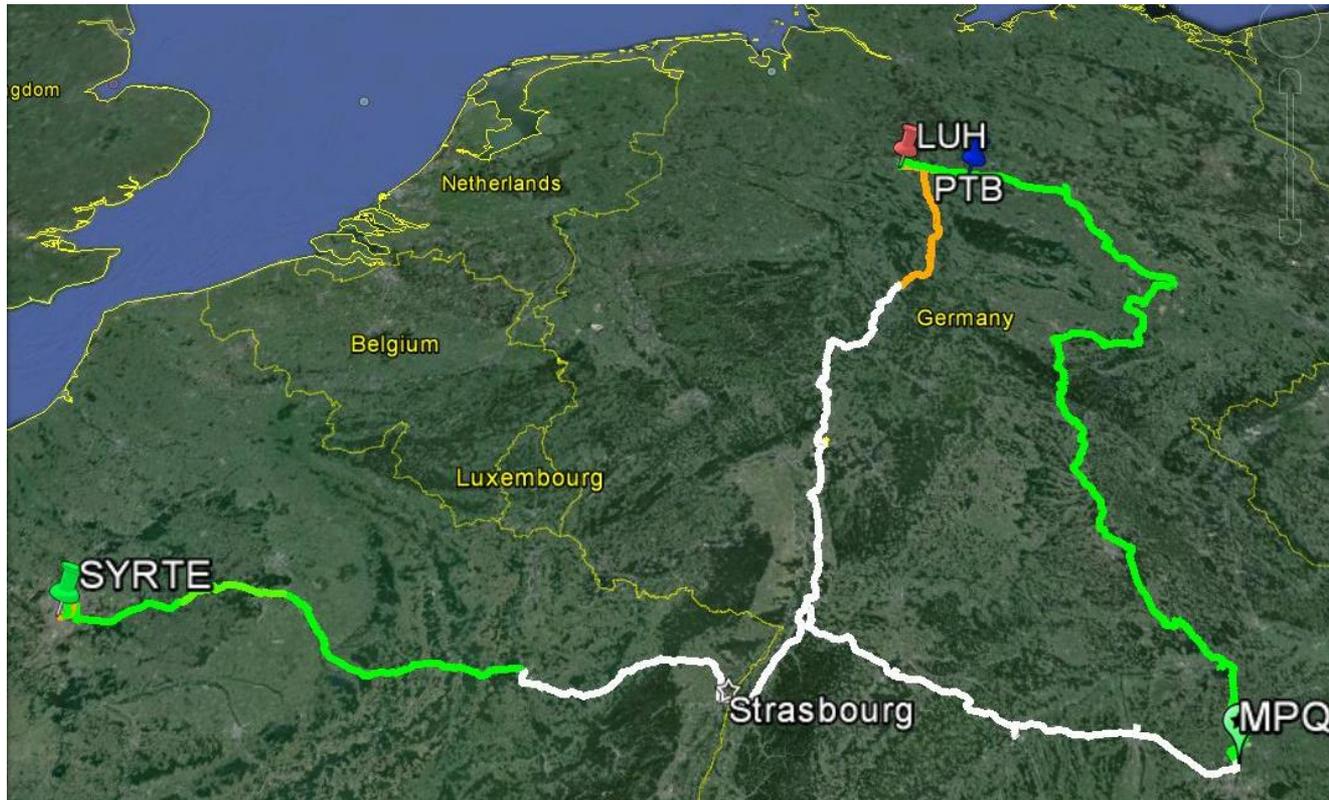
group of Piet Schmidt and Christian Lisdat



- frequency transfer through **optical fiber**
- frequency difference between remote clocks
- provides directly **potential differences** and **height differences** over very **large distances**



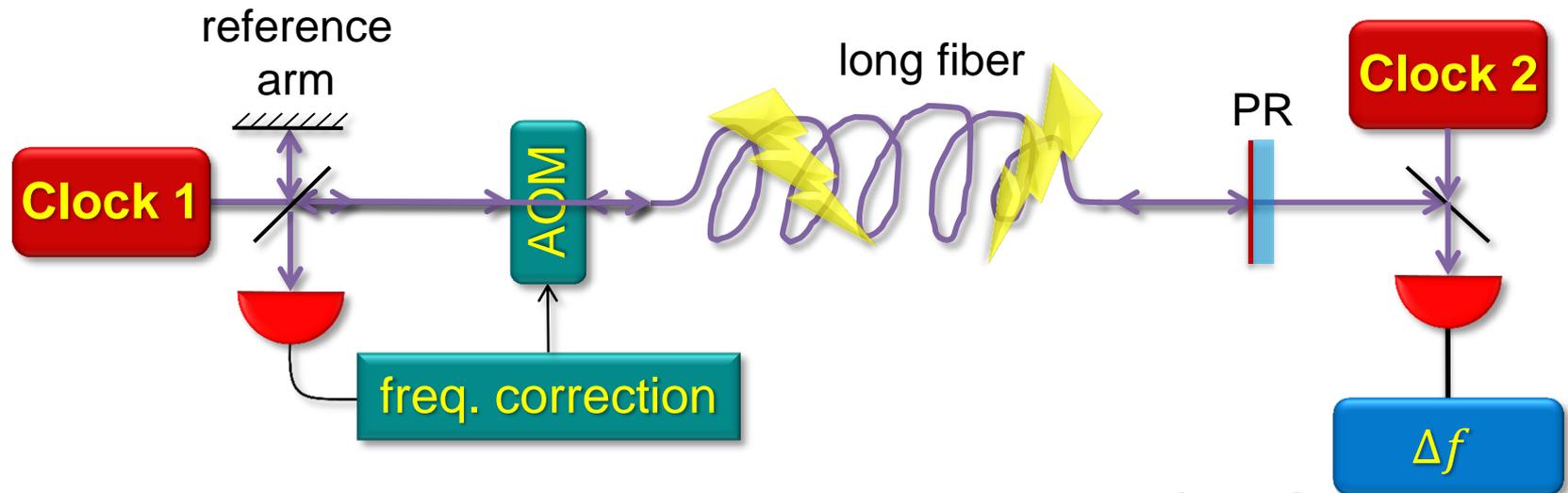
Steps towards chronometric leveling



existing and prospective fiber links

Clock comparison: phase-stabilized fibers

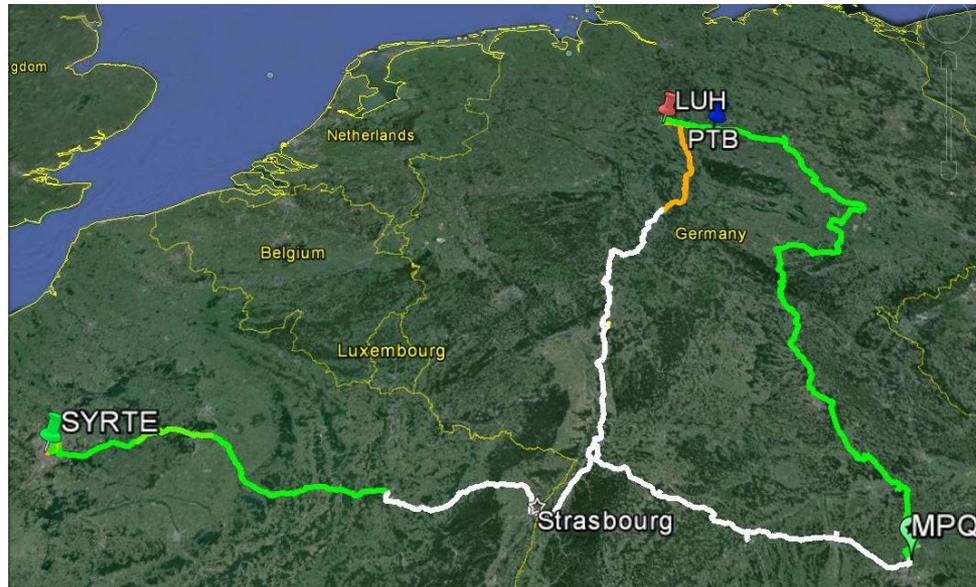
- Acoustic and thermal perturbations affect length of fiber
- frequency of transmitted light is Doppler-shifted
 → active length stabilization of fiber required



→ proof of principle experiments PTB–LUH/MPQ
 1840 km loop link with $\delta f/f \sim 4 \times 10^{-19}$ @ 100 s

group of Harald Schnatz

Steps towards chronometric leveling



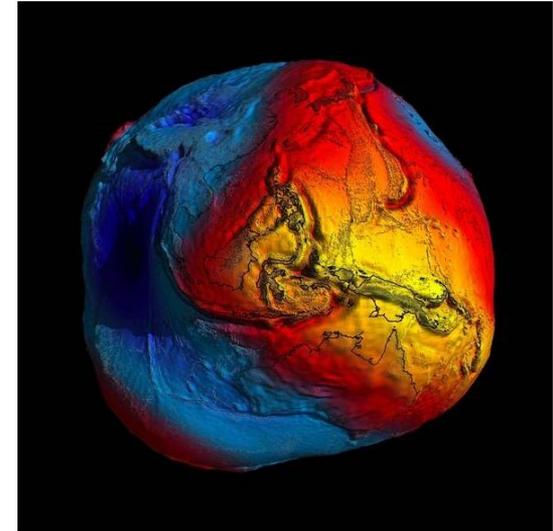
- transportable clocks for side-by-side calibration
- to eliminate residual systematic errors
- connection F – D at University of Strasbourg Computing Centre

- relativistic **geoid definition**: surface where clocks run with the same speed
- clock network: geoid **accessible** within continents

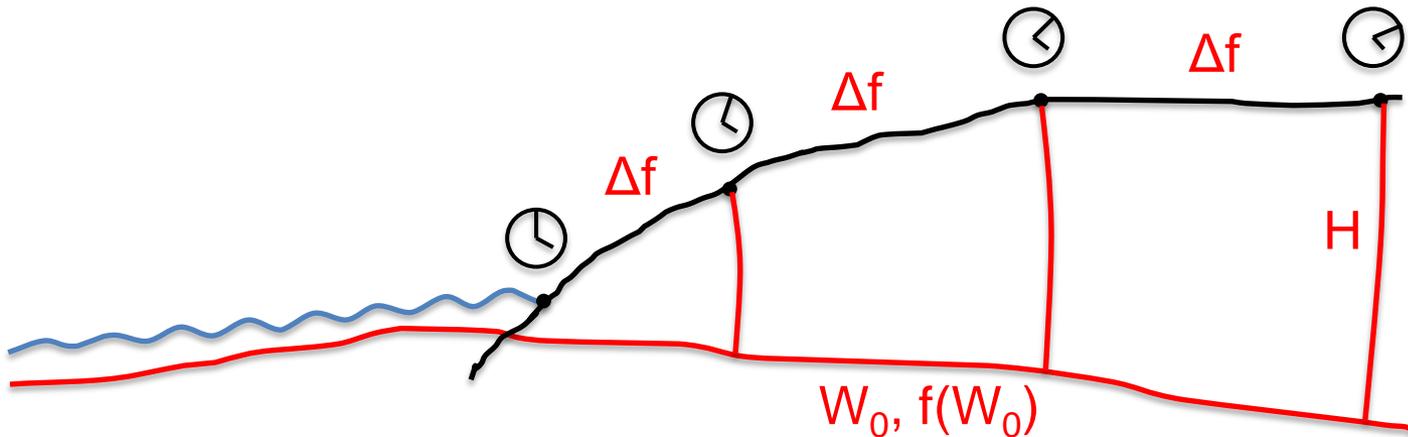
$$H = (W_0 - W_p) / \bar{g}$$

- well defined height reference
- very different from conventional height determination

- **challenge: develop the foundations for chronometric leveling and relativistic geoid**

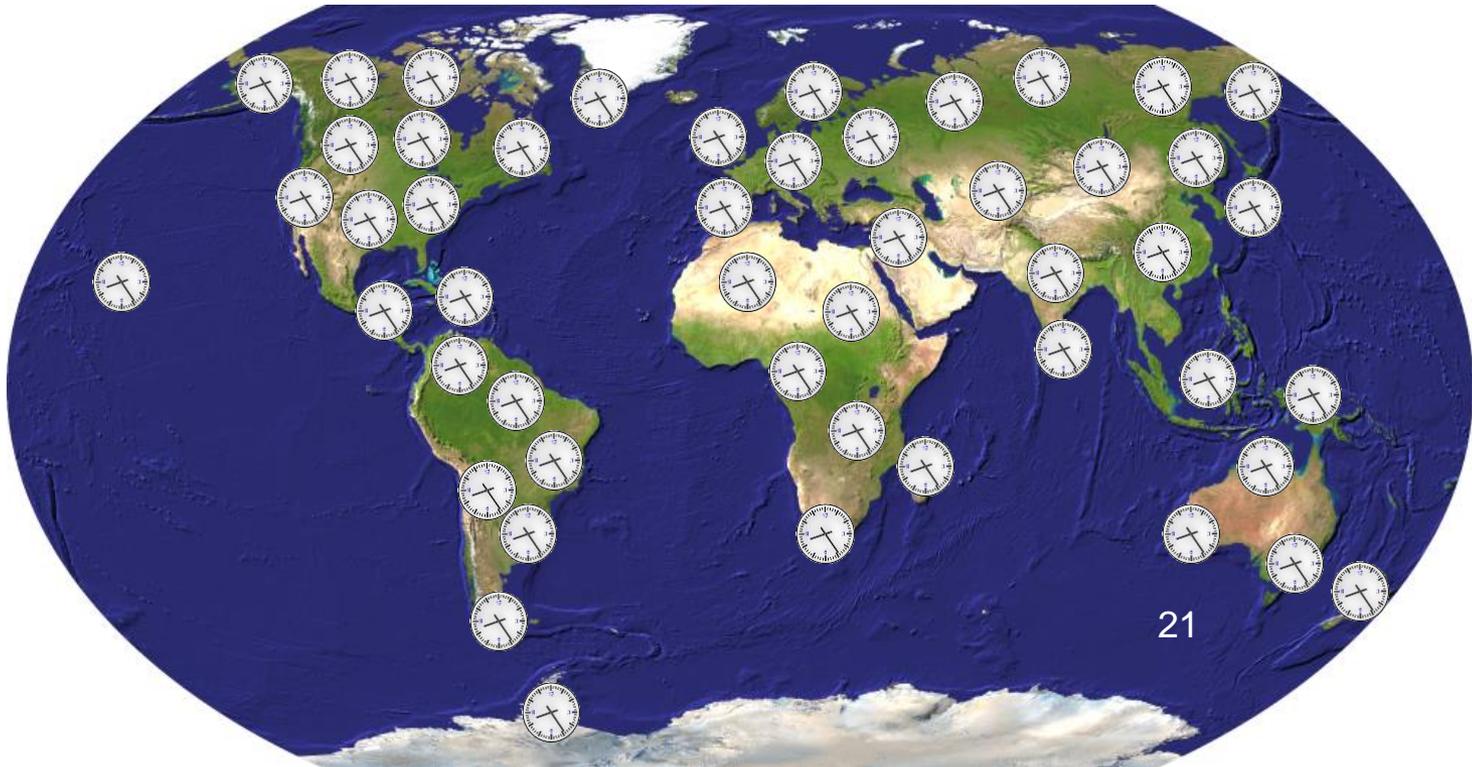


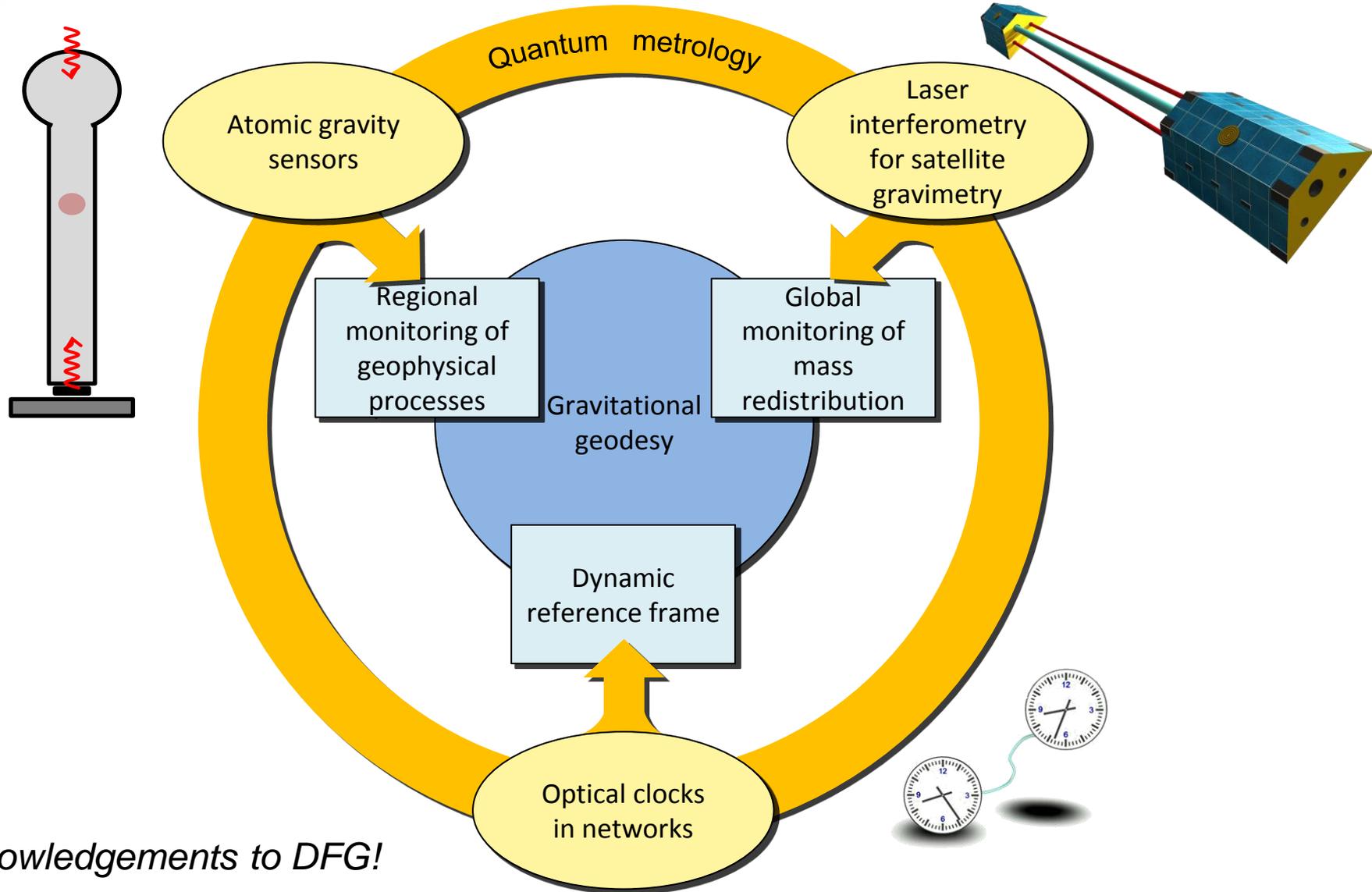
ESA





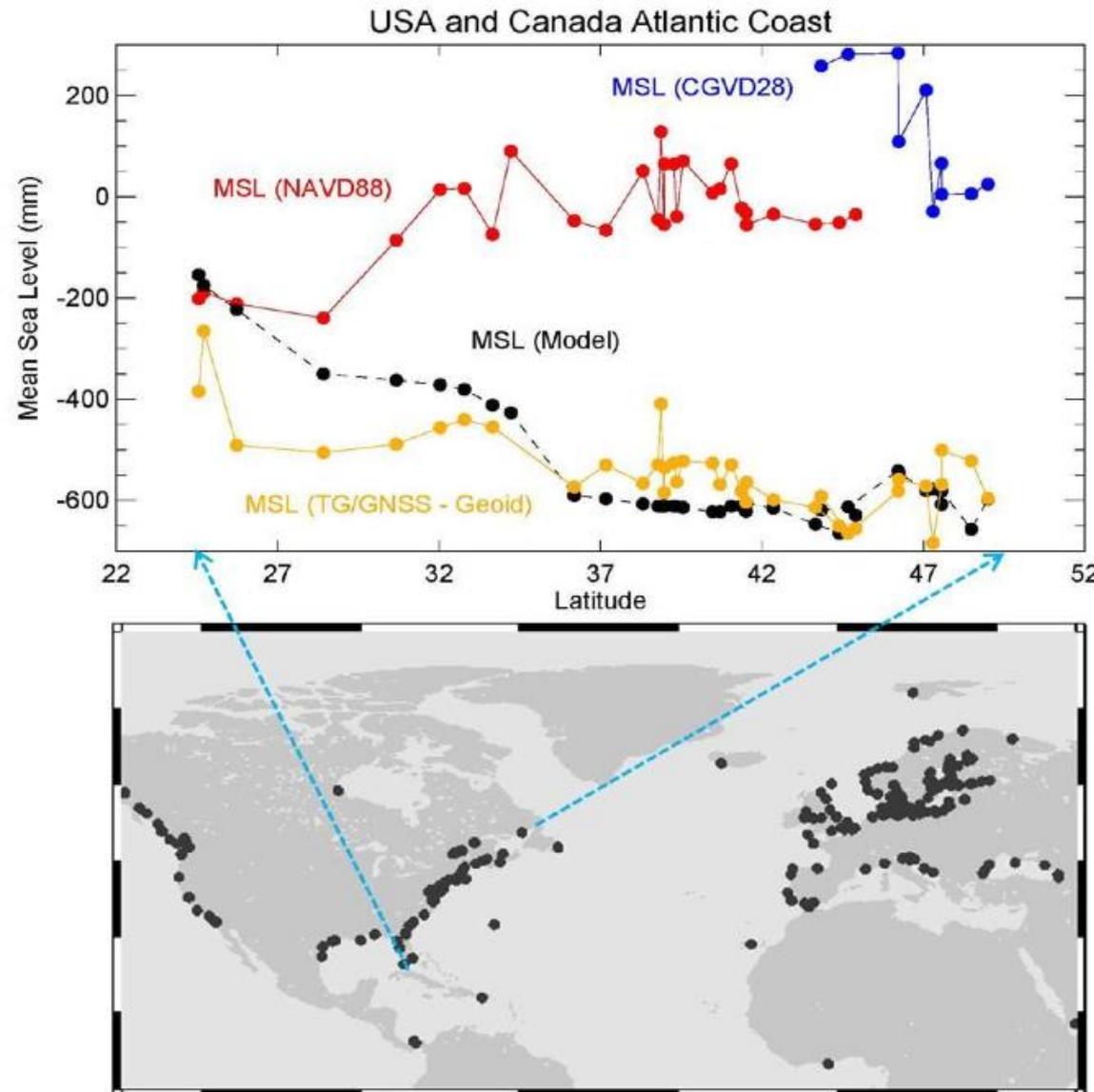
towards clock based gravity reference...





Acknowledgements to DFG!

Height inconsistencies

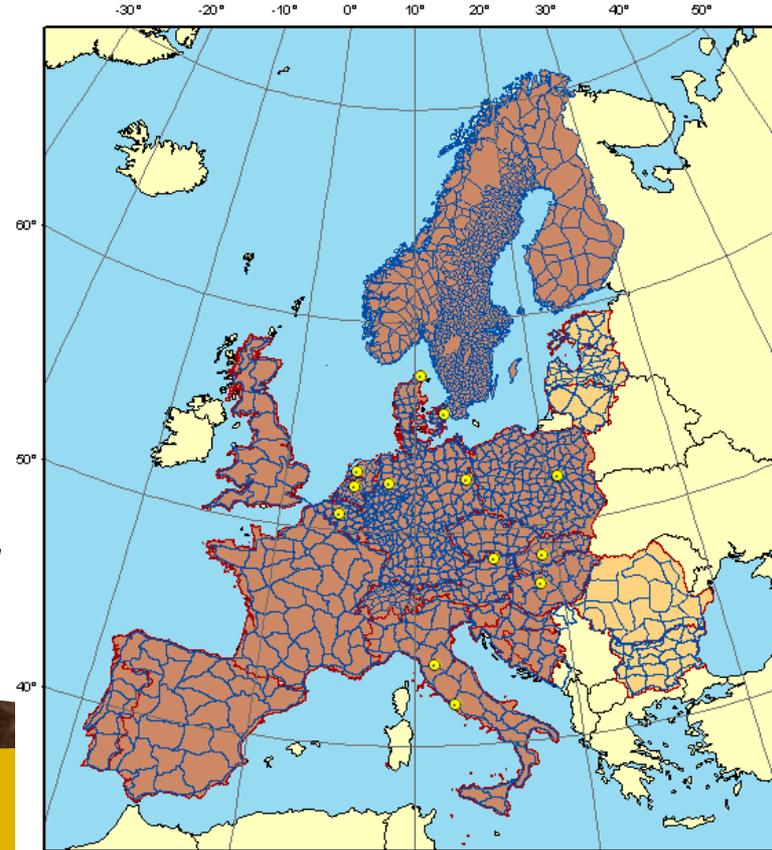
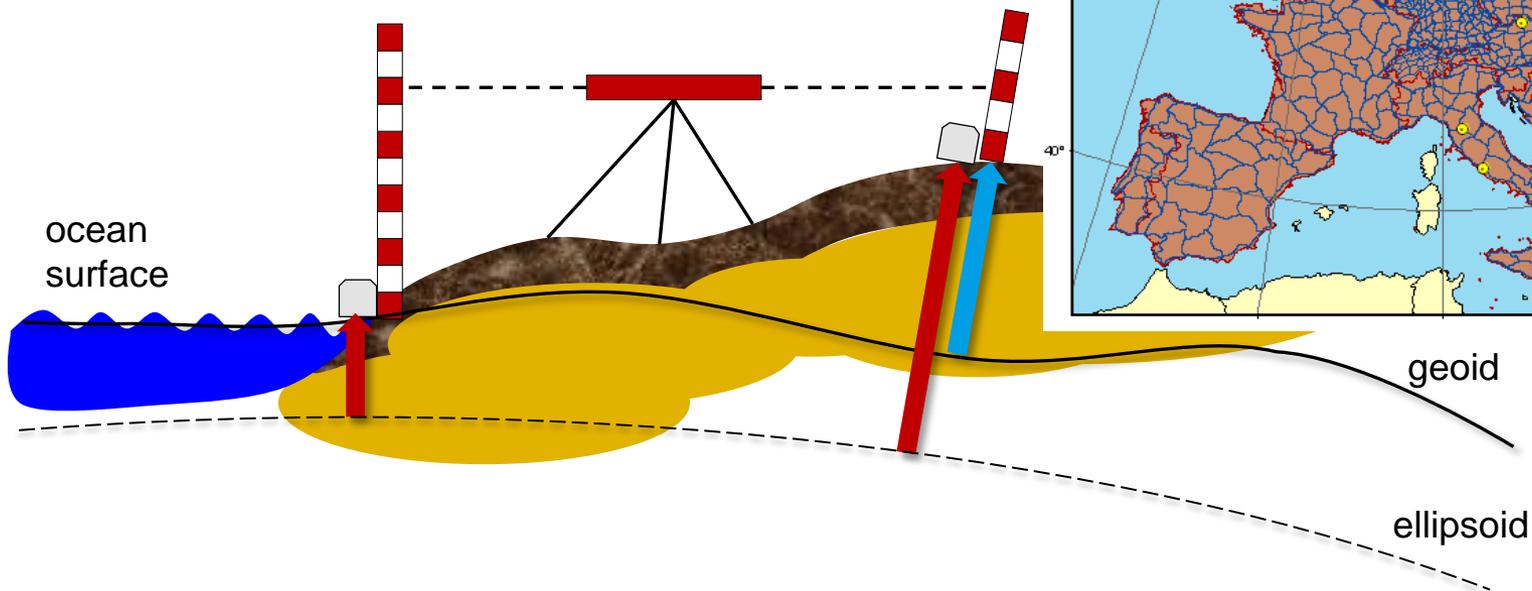


- decimeter inconsistencies
- hamper combination of tide gauges
- efforts for **height system modernization**
- **clocks** could provide **in-situ cm** accuracy referred to **well-defined W_0**

Sideris et al 2013 (GOCEplus study)

Classical leveling

- spirit leveling
- large effort
- **accumulation of errors** over large distances
- **tide gauges** as rather **arbitrary** reference



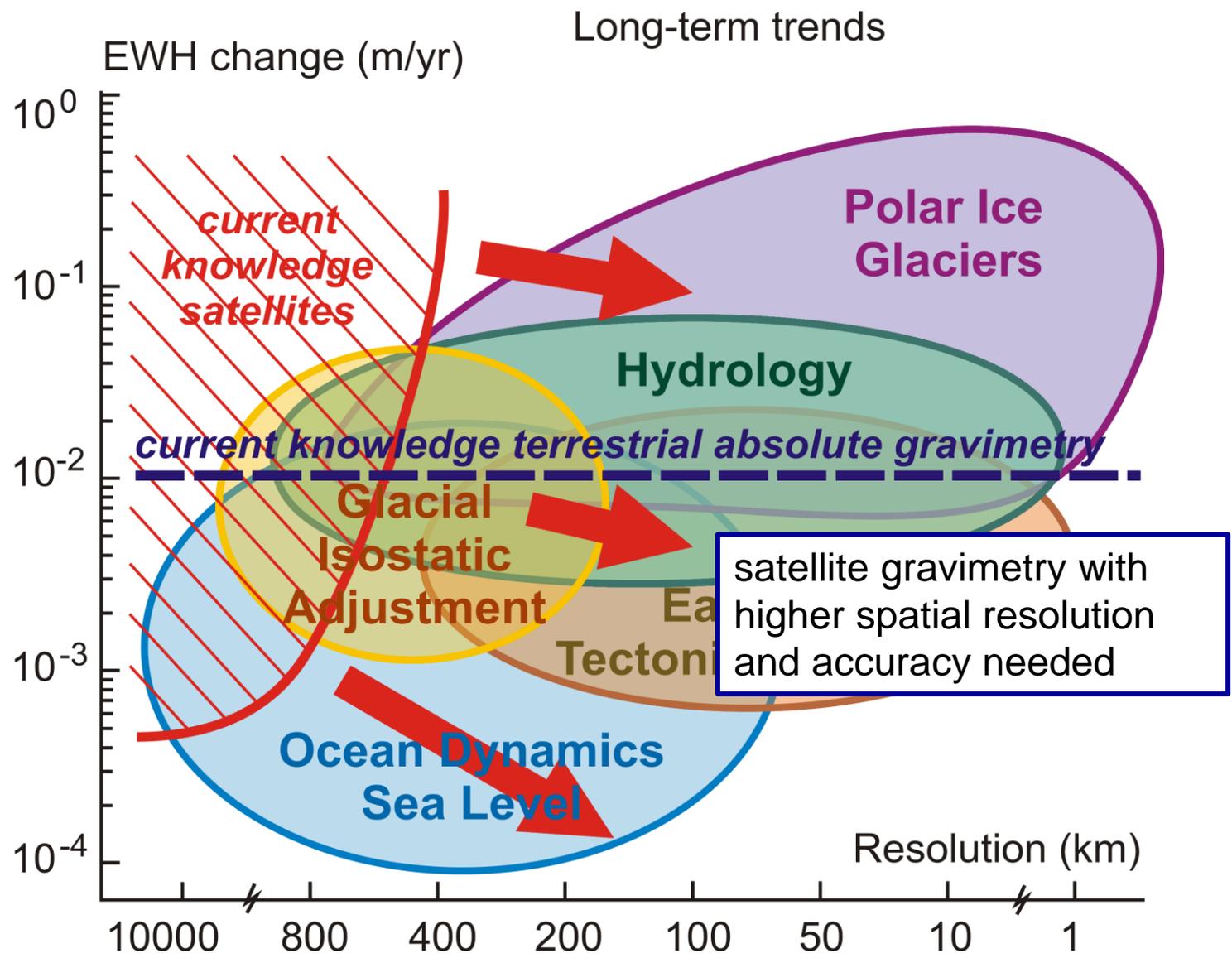
- Global change monitoring based on quantum measurement science
 - Multi-testmass interferometry in space as standard technique for sensing global mass variations
 - Quantum gravimeters rapidly and reliably monitoring sub-surface mass changes
 - Relativistic geodesy with clock networks establishing and distributing vertical reference
 - New class of gravity models integrating quantum sensor data with spatio-temporal zoom-in
- For everyday geo-applications & fundamental physics breakthroughs



J. Fraunhofer

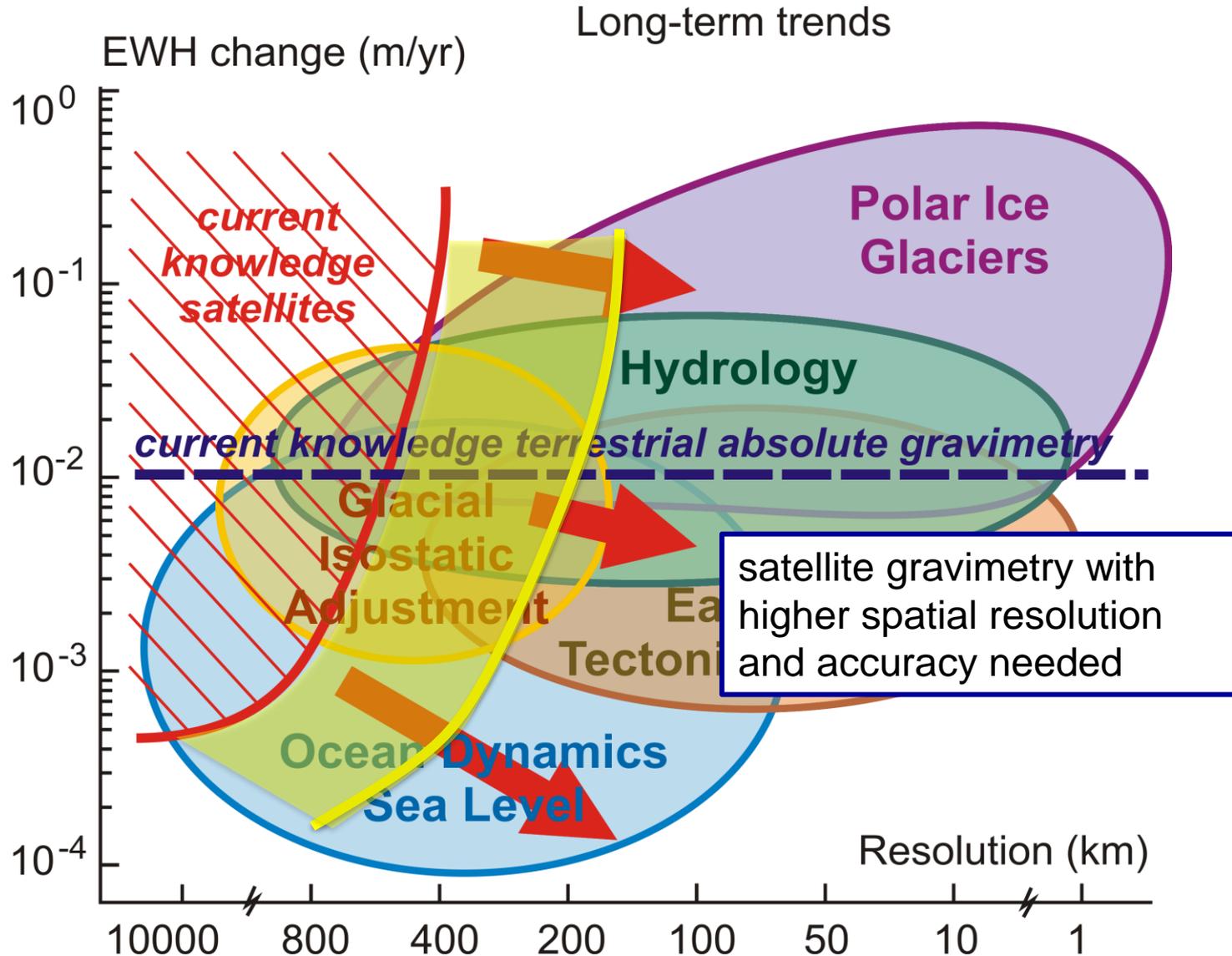


Towards new geophysics



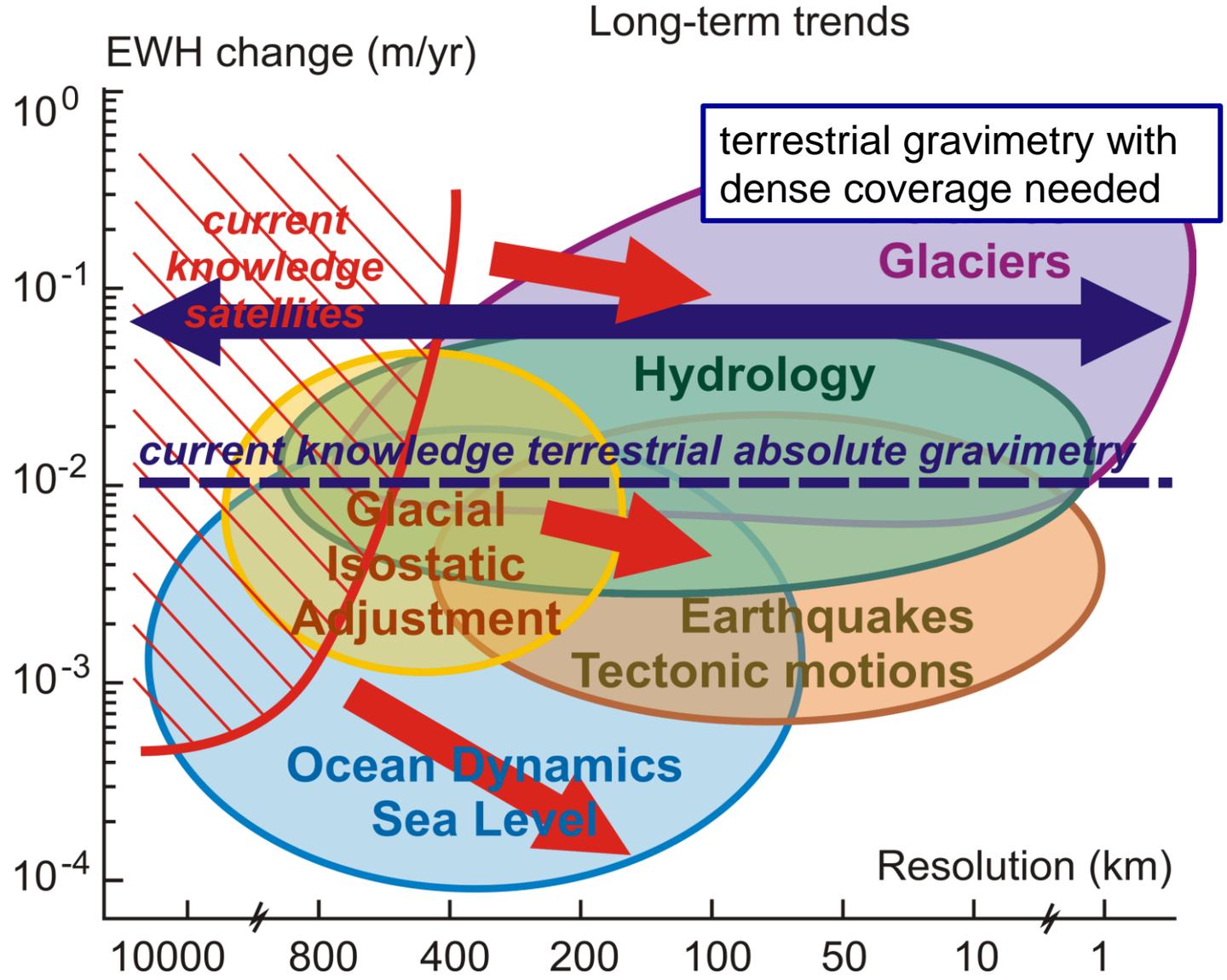


Towards new geophysics

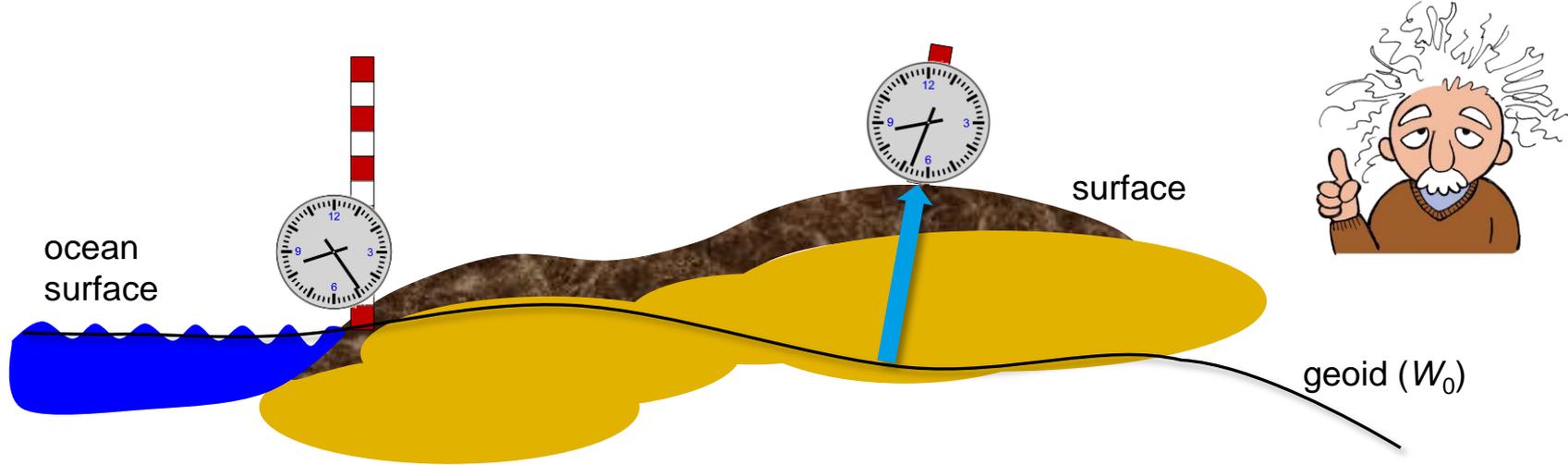




Towards new geophysics



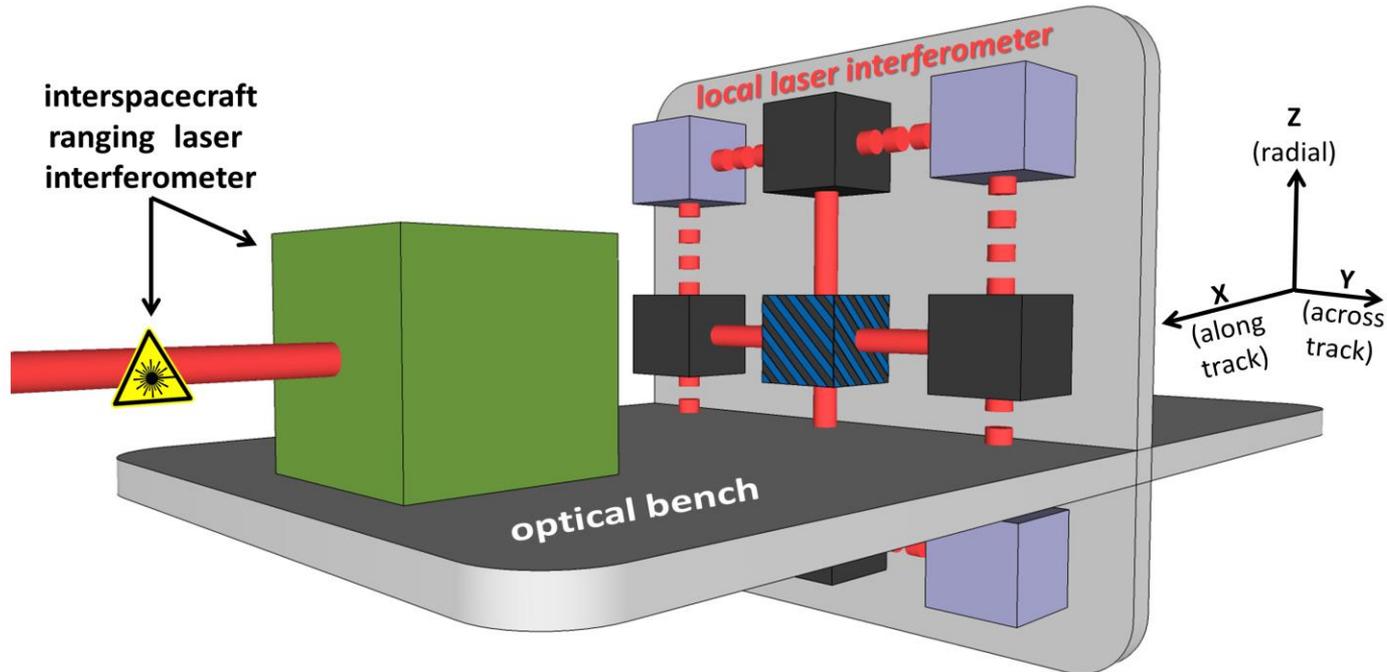
Relativistic geodesy with clocks



- fundamental relation **time / frequency – gravitation / height**

$$DW = \frac{Df}{f} c^2$$

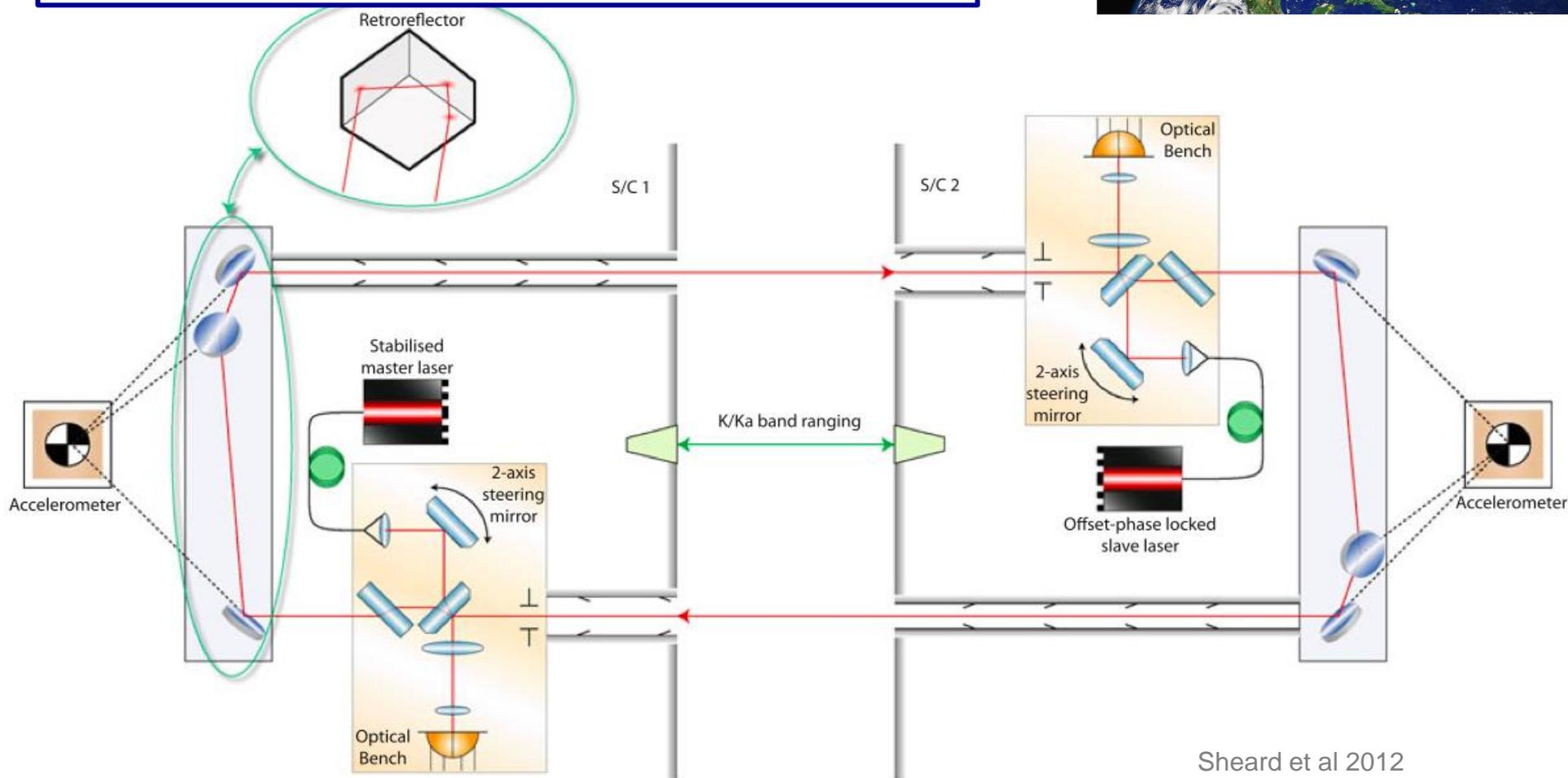
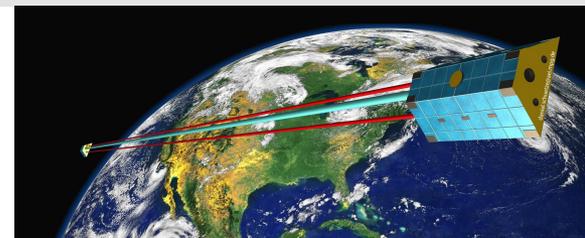
- optical atomic clocks now approaching $10^{-18} \Leftrightarrow 0.1 \text{ m}^2/\text{s}^2 \Leftrightarrow 1 \text{ cm}$
- the **most accurate** physical measurement!
- towards cm precision height determination with frequency measurements
- curvature of **space-time** now relevant at the **cm level** on Earth surface!



- **challenge: exploring the metrology of optical multi-testmass systems**
- pm/ $\sqrt{\text{Hz}}$ ranging
- multichannel optics, phasemeters, testmass control, ...

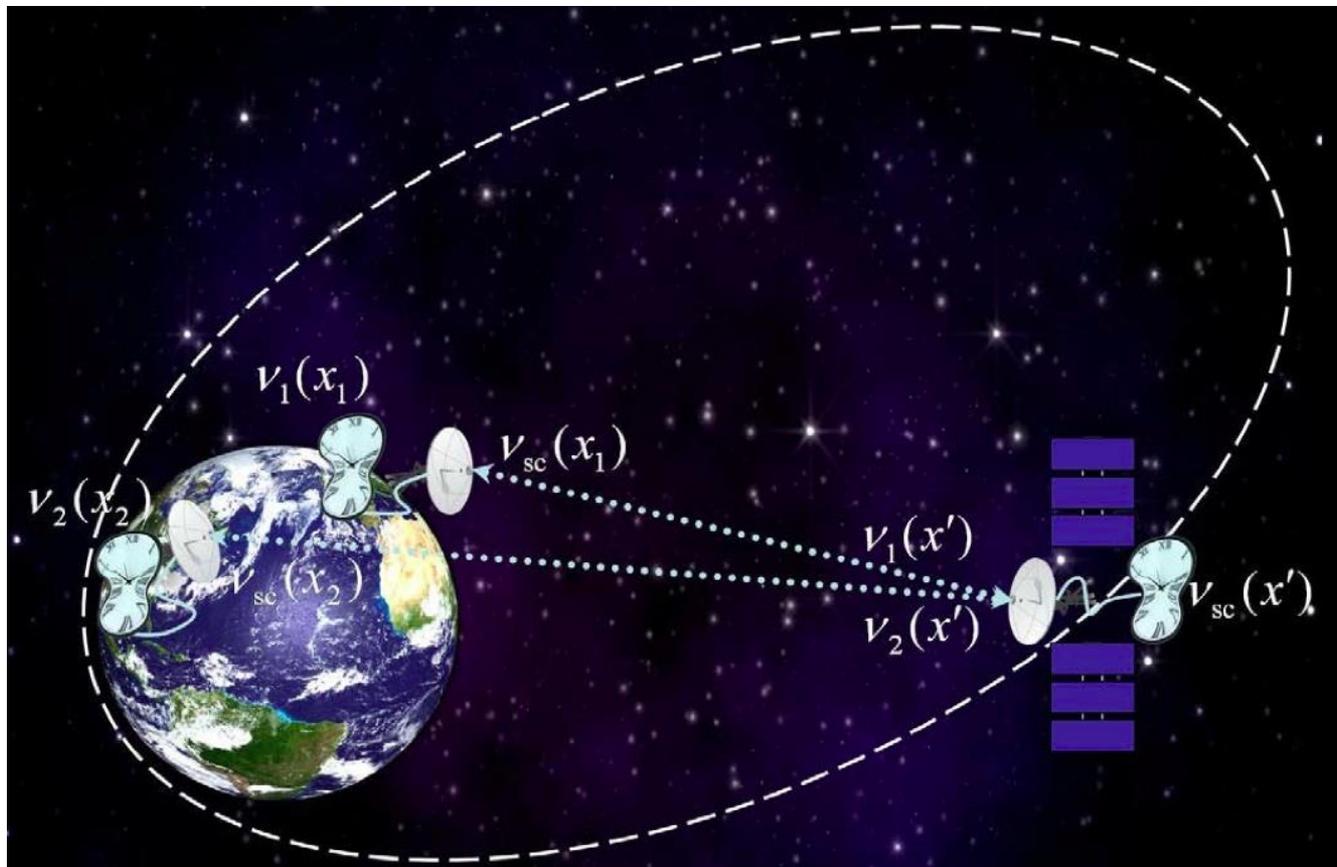
First laser interferometer between Earth orbiters

- “racetrack” interferometer configuration
- beam steering for better pointing control
- nm ranging for better gravity resolution



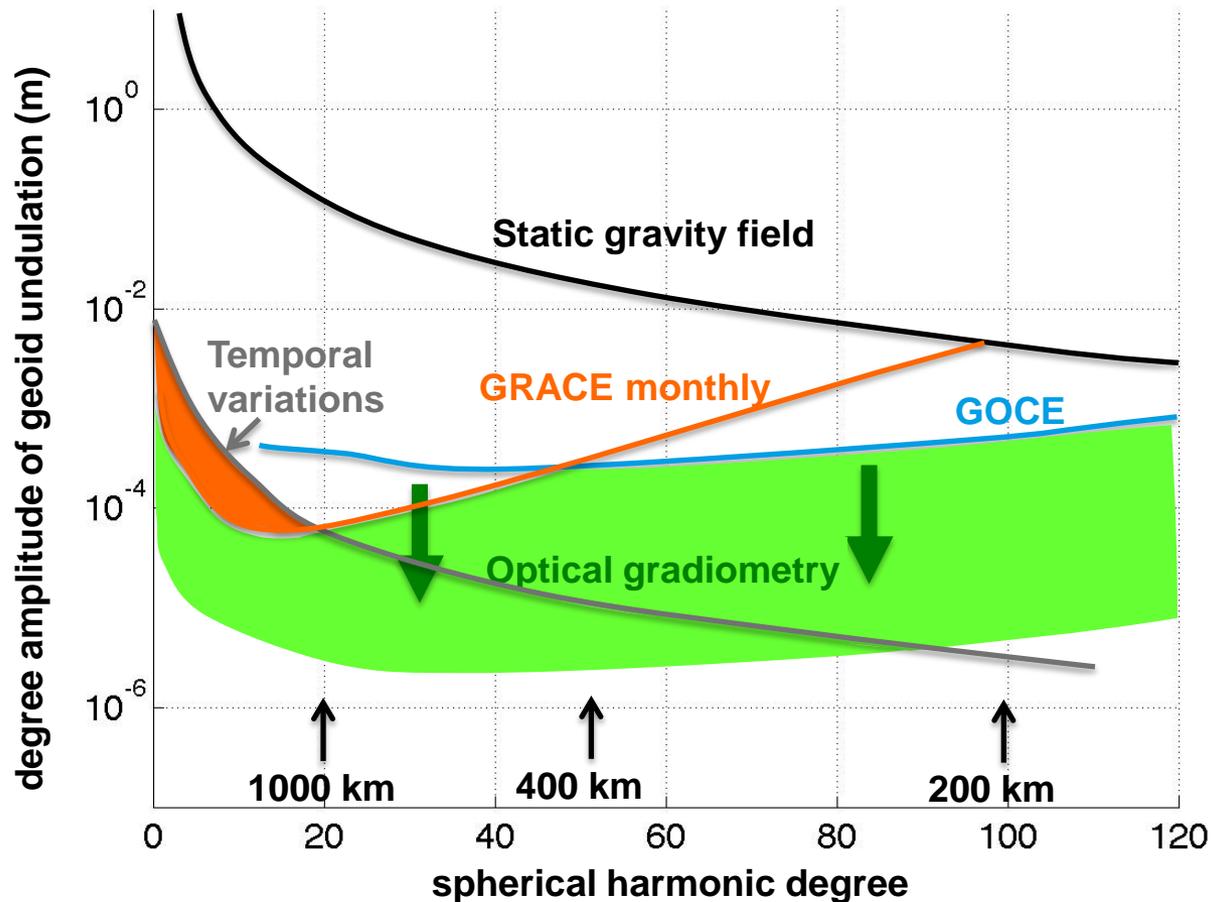
Sheard et al 2012

- laser interferometric length measurements
- gravity gradiometry with atomic interferometry (ESA, NASA, ...)
- gravitational redshift, clock network in space (STE-QUEST)

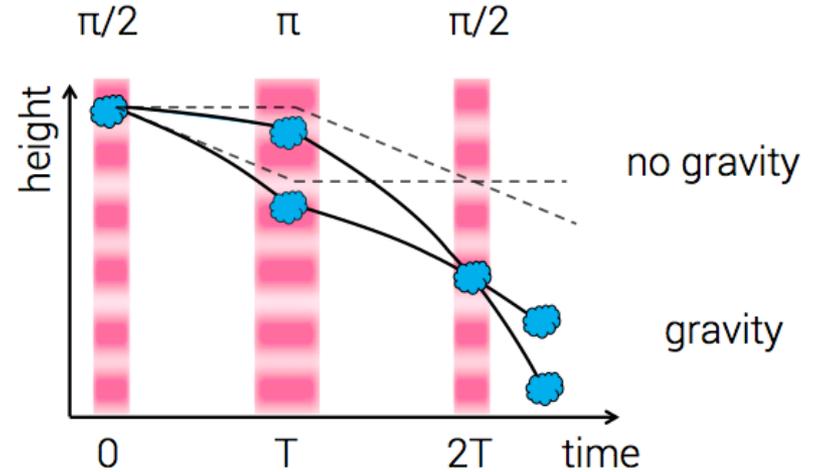
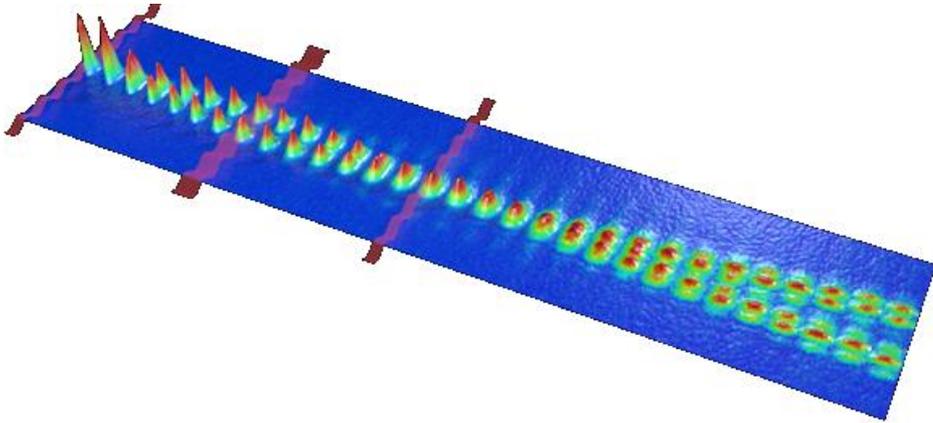


Enhanced resolution in gravity modeling

- future **gradiometry** in combination with ranging is very **promising for satellite gravimetry**



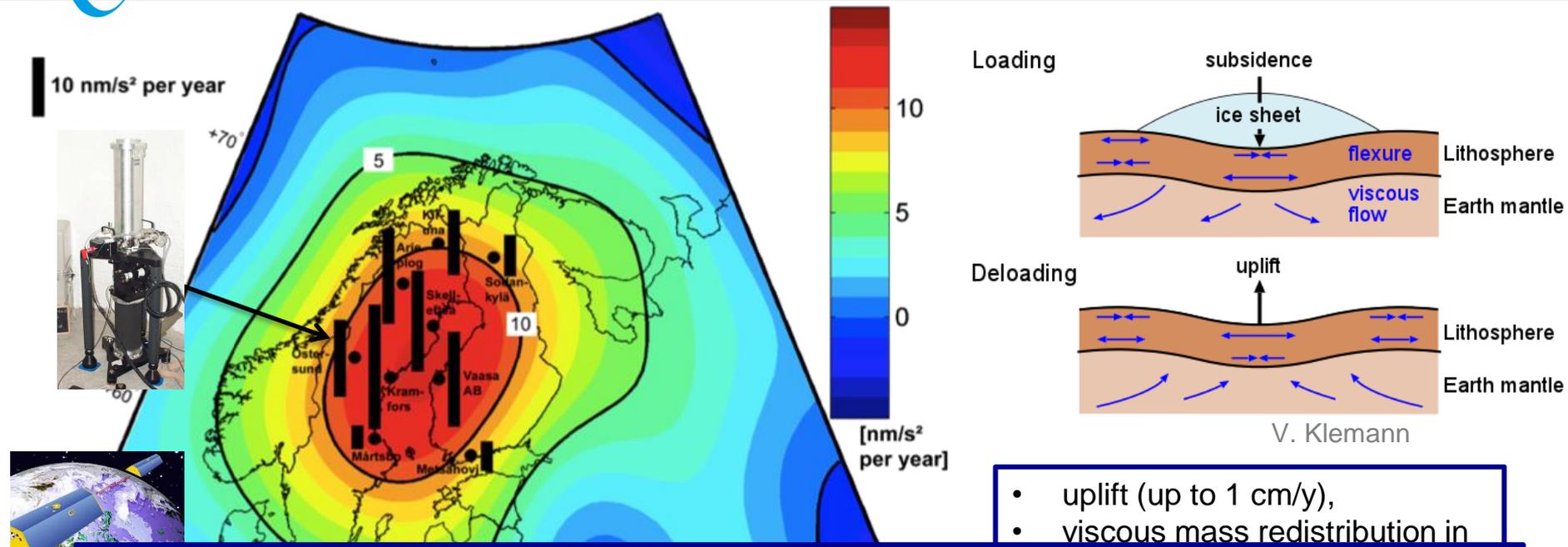
Gravity sensing with atom interferometry



- **matter waves** of a **free-falling atom cloud** are coherently split, redirected and recombined with a pulsed light grating
- position information imprinted onto matter wave phase in each atom-light interaction
- measured through matter wave interferometer **phase readout**



Gravity signals: Glacial Isostatic Adjustment



- uplift (up to 1 cm/y),
- viscous mass redistribution in

Glacial Isostatic Adjustment (GIA) is

- revealing **mass flux in Earth mantle** and mantle properties
- affecting whole Earth (mm/y-level), sea level change estimates
- affecting geodetic networks
- **measurement challenge, faster absolute gravimeters** needed to understand regional patterns