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**GRAVIMOB** : a new **gravimetry** and **gradiometry** **mobile** system  
for the subsea domain.

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**Colloque G2 2014 - Strasbourg**

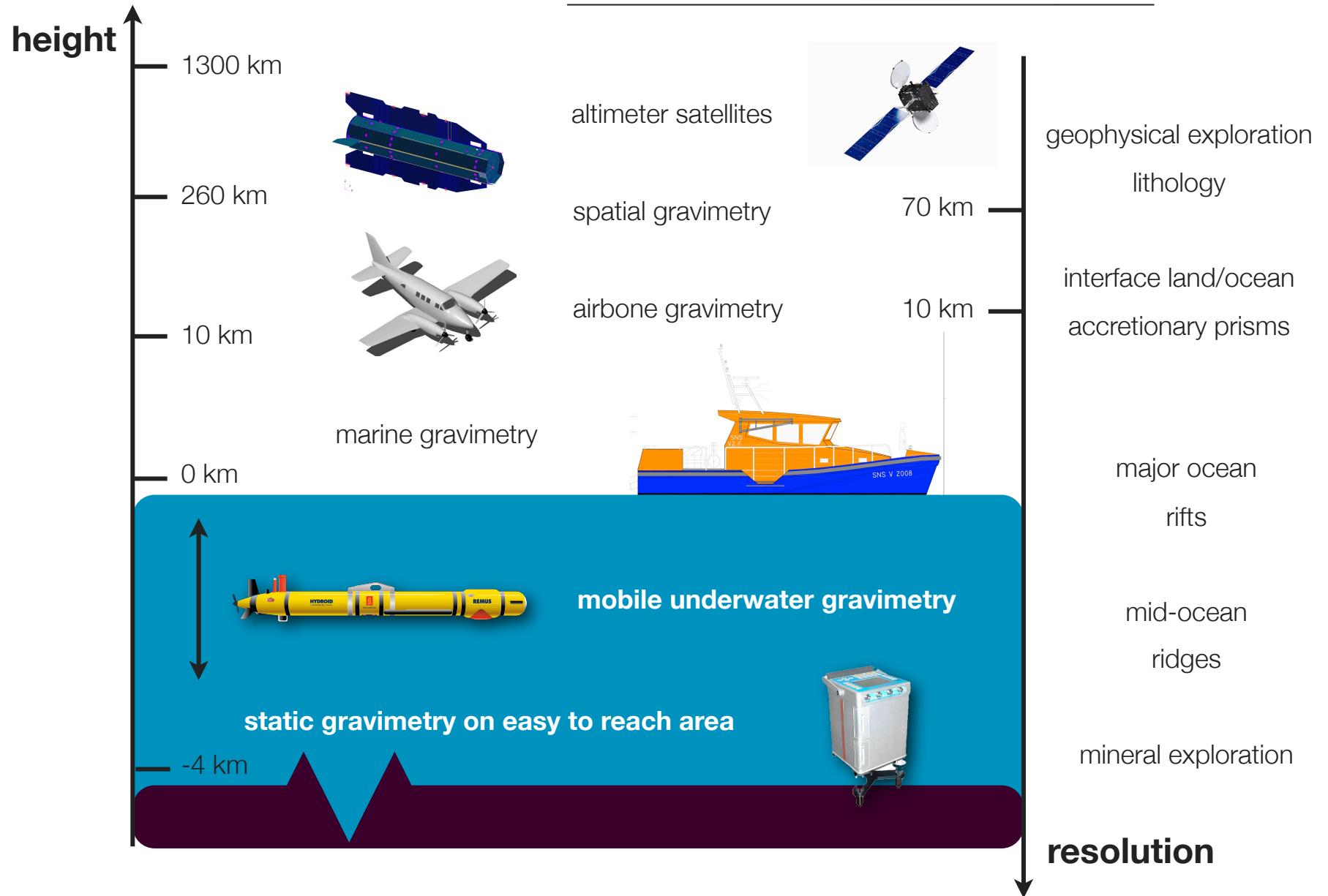
Clément Roussel - PhD Student

Jérôme Verdun - supervisor

Marcia Maïa - co-supervisor

GRAVIMOB : a new gravimetry and gradiometry mobile system for the subsea domain.

# Motivation



GRAVIMOB : a new gravimetry and gradiometry mobile system for the subsea domain.

# Stakes

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source : flotte.ifremer.fr

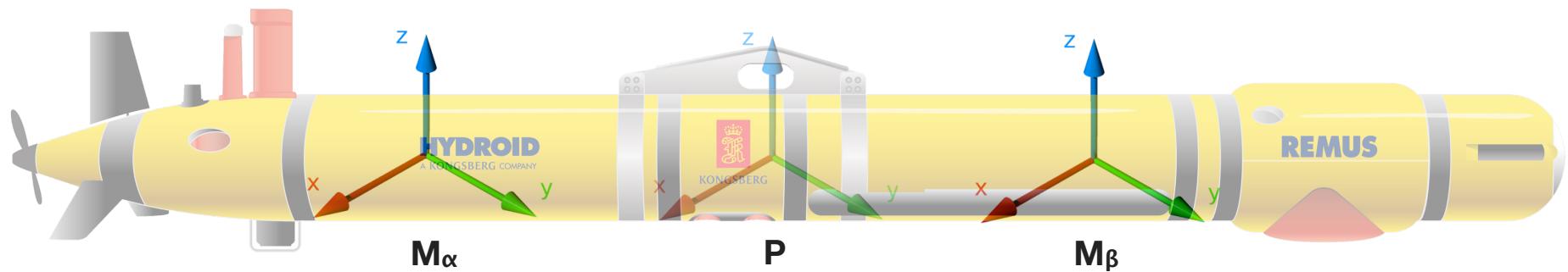
**AUV** AsterX (**A**utonomous **U**nderwater **V**ehicle)

GRAVIMOB : a new gravimetry and gradiometry mobile system for the subsea domain.

# Stakes

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Measuring the components of the gravity field's vector and their spatial variations  
in the subsea environment !



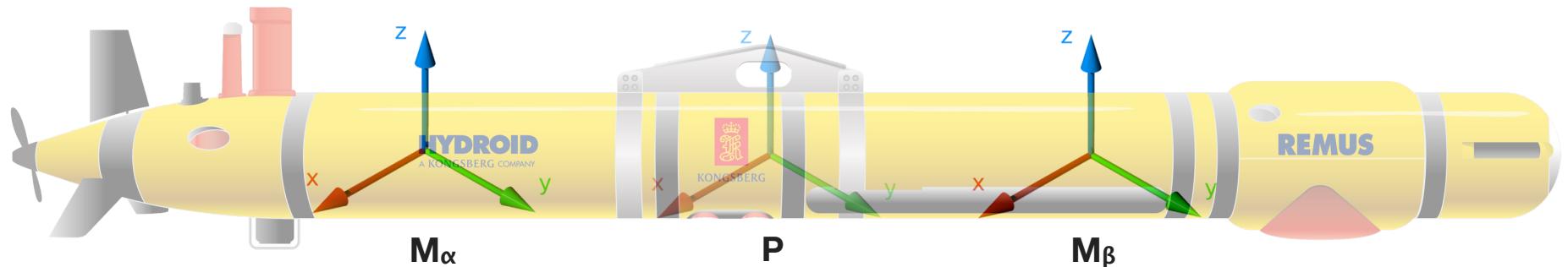
$$g_\alpha^b = \left[ (\Omega_{ib}^b \Omega_{ib}^b + \dot{\Omega}_{ib}^b) X_P^b + 2\Omega_{ib}^b \dot{X}_P^b + \ddot{X}_P^b \right] + \left[ (\Omega_{ib}^b \Omega_{ib}^b + \dot{\Omega}_{ib}^b) L_\alpha^b \right] - a_\alpha^b$$

$$g_\beta^b = \left[ (\Omega_{ib}^b \Omega_{ib}^b + \dot{\Omega}_{ib}^b) X_P^b + 2\Omega_{ib}^b \dot{X}_P^b + \ddot{X}_P^b \right] + \left[ (\Omega_{ib}^b \Omega_{ib}^b + \dot{\Omega}_{ib}^b) L_\beta^b \right] - a_\beta^b$$

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# Equations

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$$g_{\alpha}^b = \left[ (\Omega_{ib}^b \Omega_{ib}^b + \dot{\Omega}_{ib}^b) X_P^b + 2\Omega_{ib}^b \dot{X}_P^b + \ddot{X}_P^b \right] + \left[ (\Omega_{ib}^b \Omega_{ib}^b + \dot{\Omega}_{ib}^b) L_{\alpha}^b \right] - a_{\alpha}^b$$

$$g_{\beta}^b = \left[ (\Omega_{ib}^b \Omega_{ib}^b + \dot{\Omega}_{ib}^b) X_P^b + 2\Omega_{ib}^b \dot{X}_P^b + \ddot{X}_P^b \right] + \left[ (\Omega_{ib}^b \Omega_{ib}^b + \dot{\Omega}_{ib}^b) L_{\beta}^b \right] - a_{\beta}^b$$

$$g_{\alpha}^b \approx g_P^b + \nabla g_P \cdot P M_{\alpha}$$

$$g_{\alpha}^b \approx g_P^b + \nabla g_P \cdot P M_{\alpha}$$

$$g_{\beta}^b \approx g_P^b + \nabla g_P \cdot P M_{\beta}$$

+

-

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$$g_{\alpha}^b + g_{\beta}^b \approx 2g_P^b$$

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$$g_{\alpha}^b - g_{\beta}^b \approx \nabla g_P \cdot M_{\beta} M_{\alpha}$$

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## Current Work

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What are the resolutions and accuracies reachable with such a system ?



### **Study of the gravity field's restitution by numerical simulation (Monte Carlo)**

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# Numerical simulation

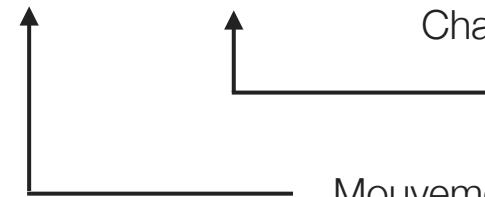
Principle

$$a_M^{ref} = \ddot{X}_M^{ref} - g_M^{ref}$$

Accélérations de rappel de référence  
**déduites**



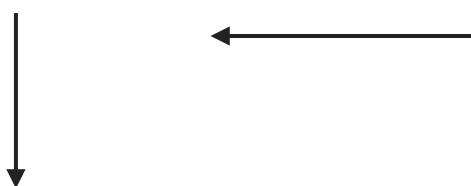
Champ de gravité de référence  
**choisi**



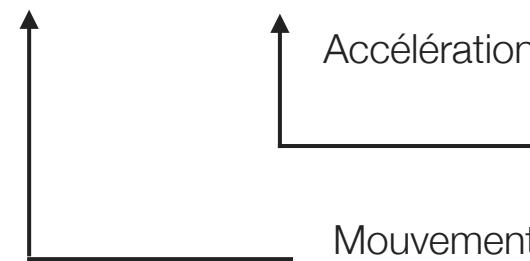
Mouvement de référence du porteur  
**choisi**

$$g_M = \ddot{X}_M - a_M$$

Champ de gravité **déduit**



Accélérations de rappel de référence  
**+ bruit**

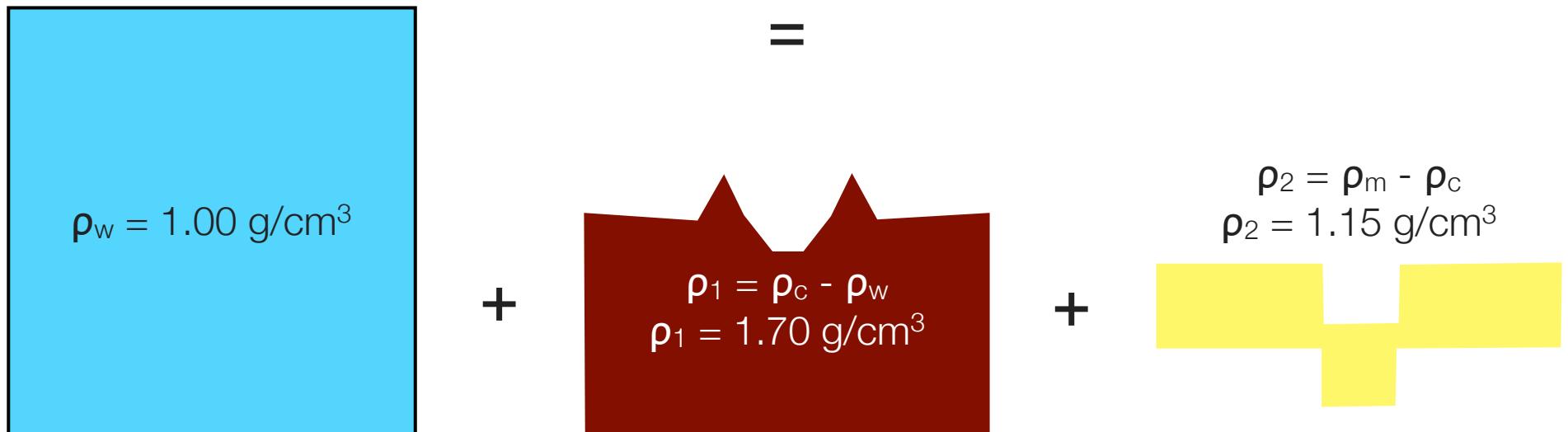
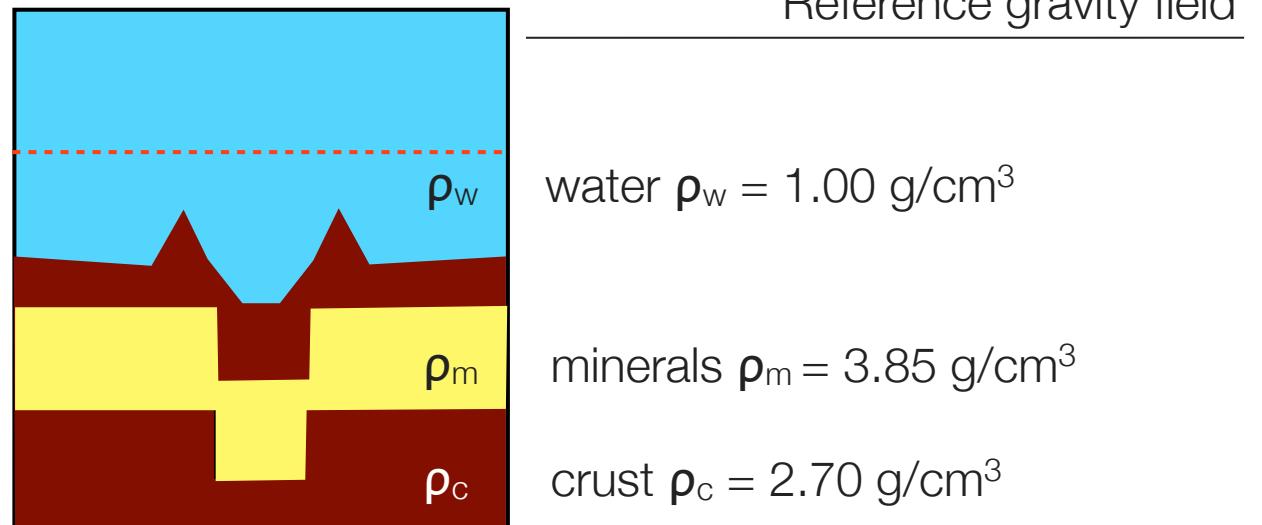


Mouvement de référence du porteur  
**+ bruit**

$$\epsilon = g_M - g_M^{ref} \quad \left\{ \begin{array}{l} E(\epsilon) = \frac{1}{n} \sum_0^n \epsilon \\ VAR(\epsilon) = E((\epsilon - E(\epsilon))^2) \end{array} \right.$$

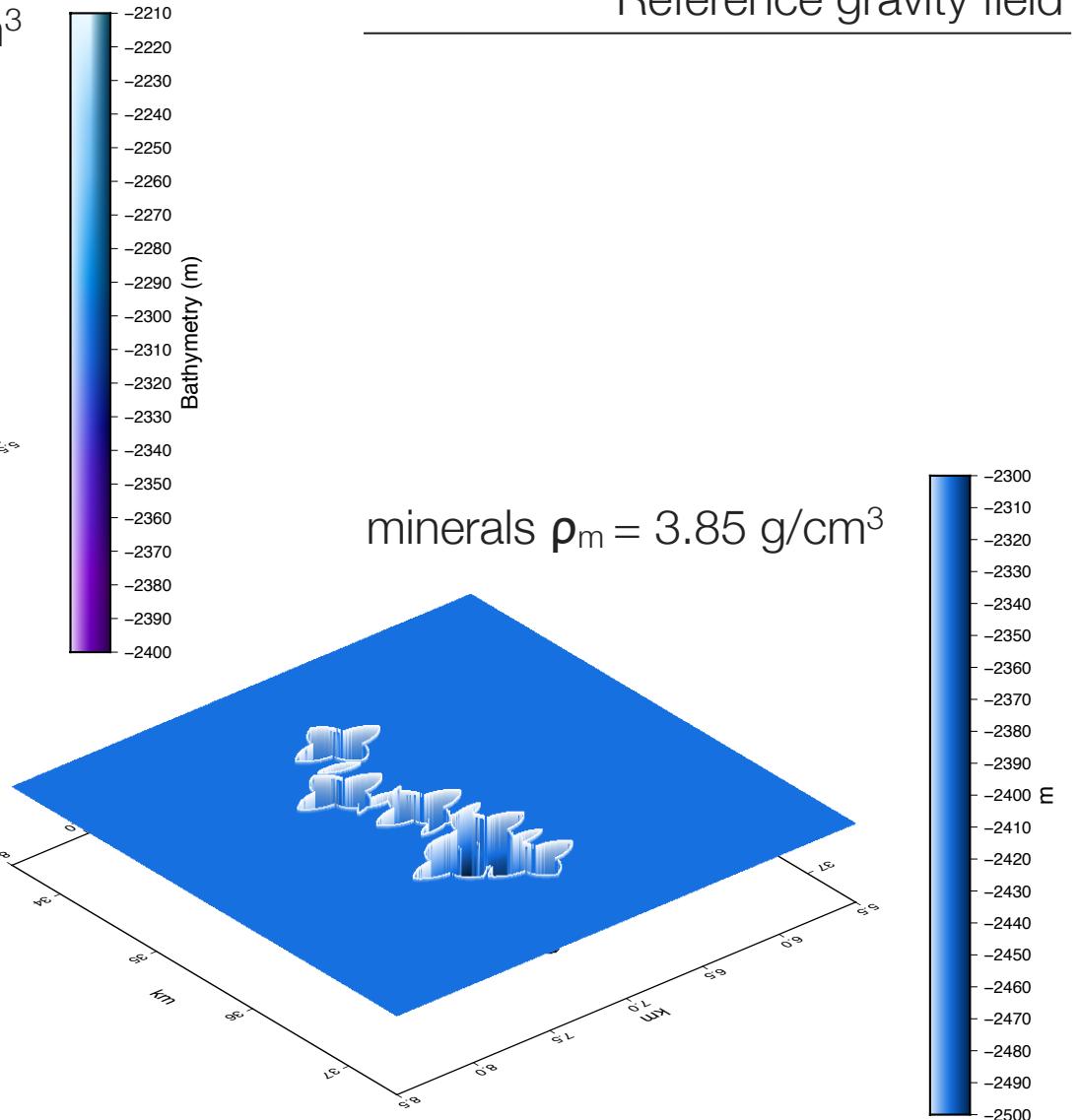
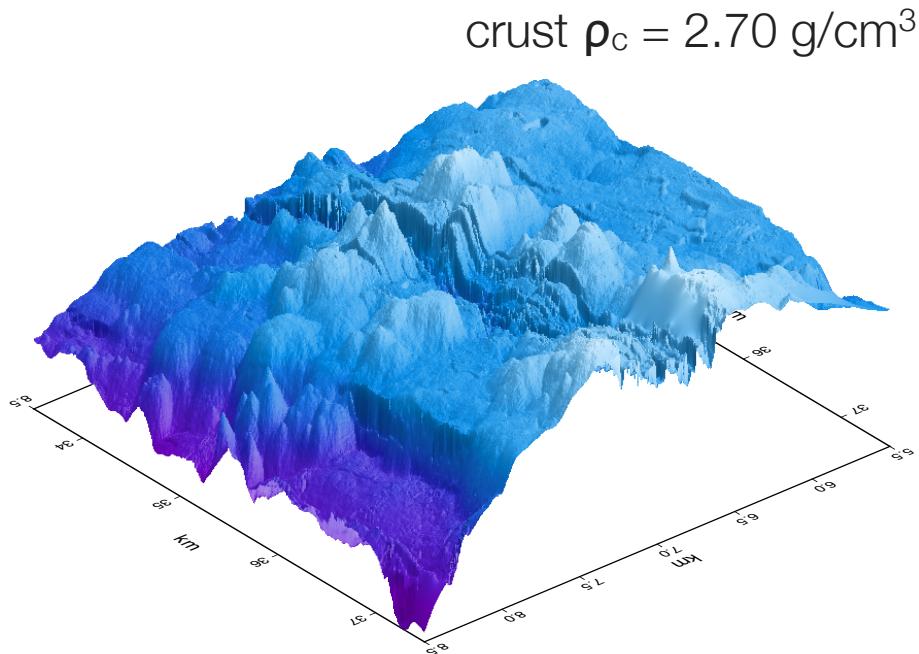
GRAVIMOB : a new gravimetry and gradiometry mobile system for the subsea domain.

## Numerical simulation



GRAVIMOB : a new gravimetry and gradiometry mobile system for the subsea domain.

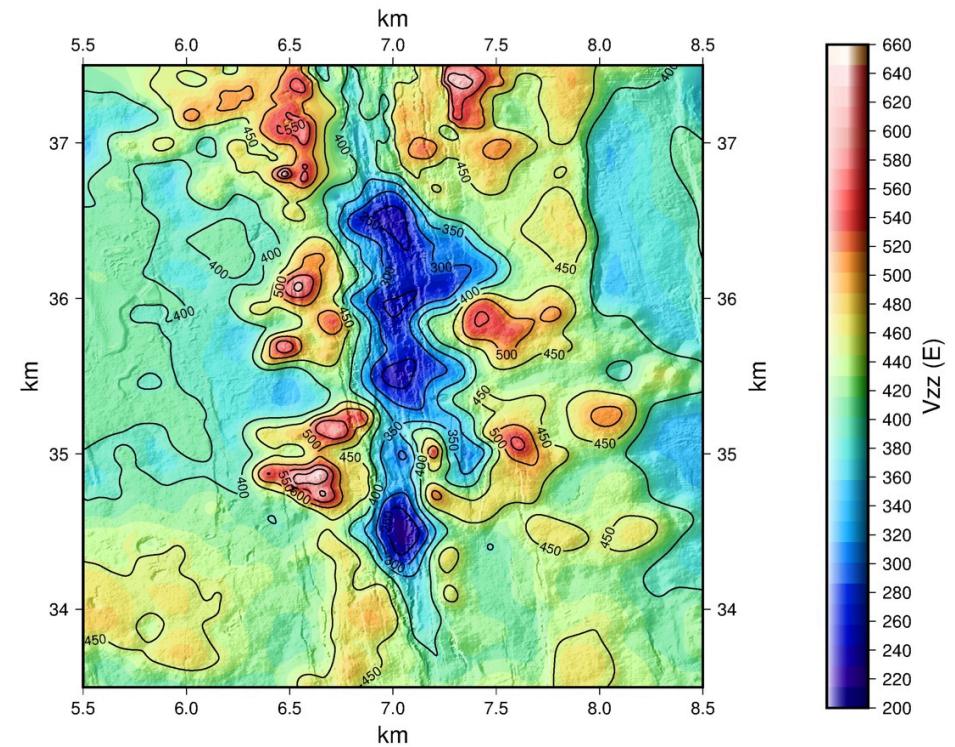
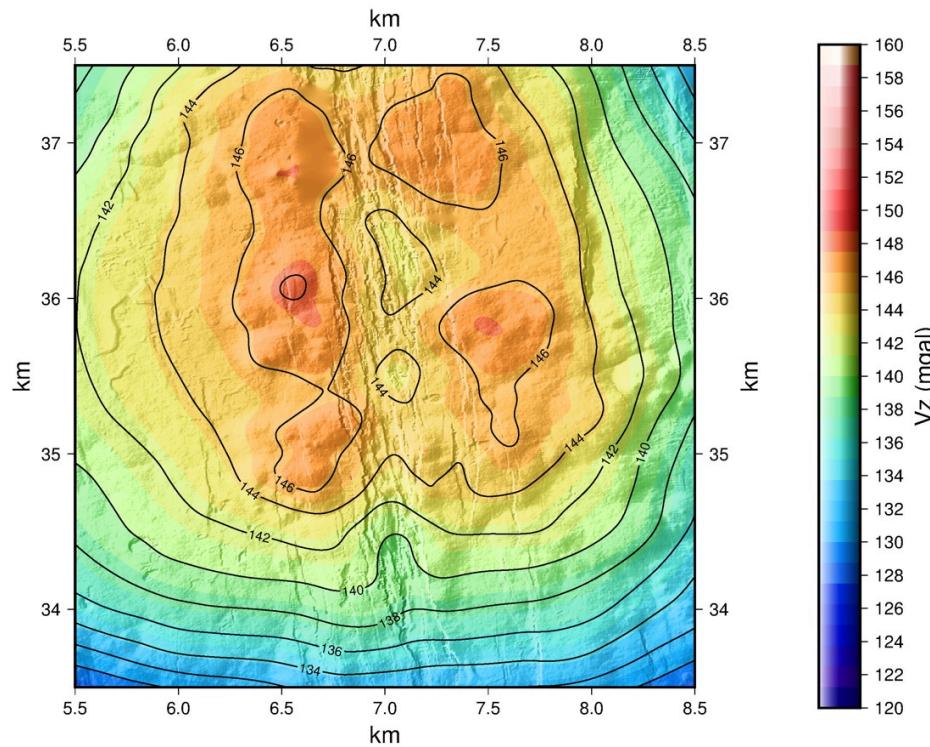
## Numerical simulation



GRAVIMOB : a new gravimetry and gradiometry mobile system for the subsea domain.

# Numerical simulation

## Reference gravity field



Logiciel **Tesseroid** - Leonardo Uieda

Leonardo Uieda, Everton P. Bomfim, C. B. E. M. (2011). Optimal forward calculation method of the marussi tensor due to a geologic structure at goce height

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# Numerical simulation

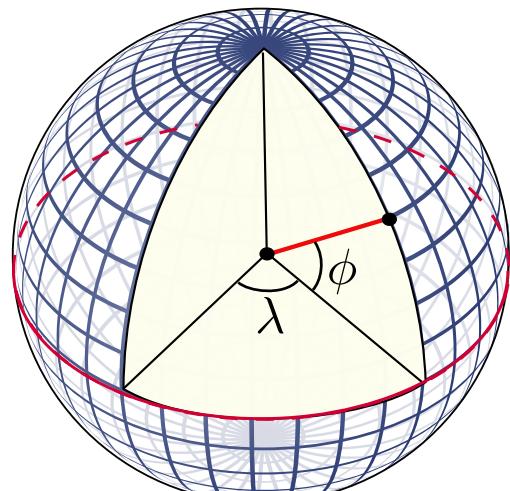
Reference motion of the carrier

## Position

$\lambda$  : longitude

$\Phi$  : latitude

h : height

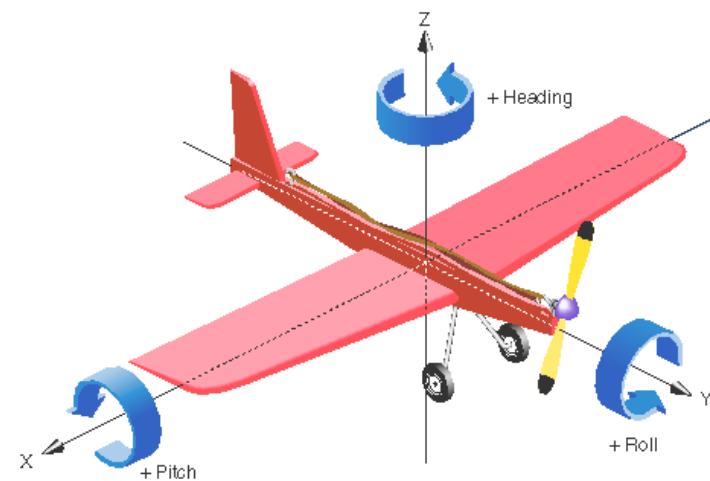


## Attitude

$\alpha$  : heading

x : pitch

$\eta$  : roll



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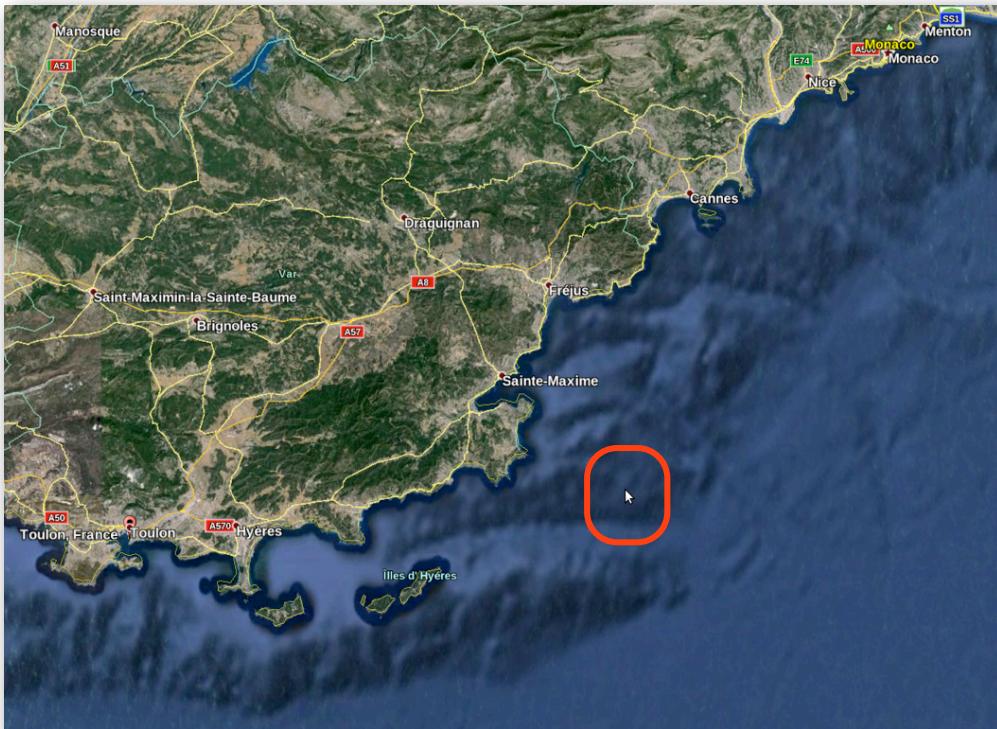
# Numerical simulation

Reference motion of the carrier

## Mission ESSAUV12

Plongée du

1 décembre 2012

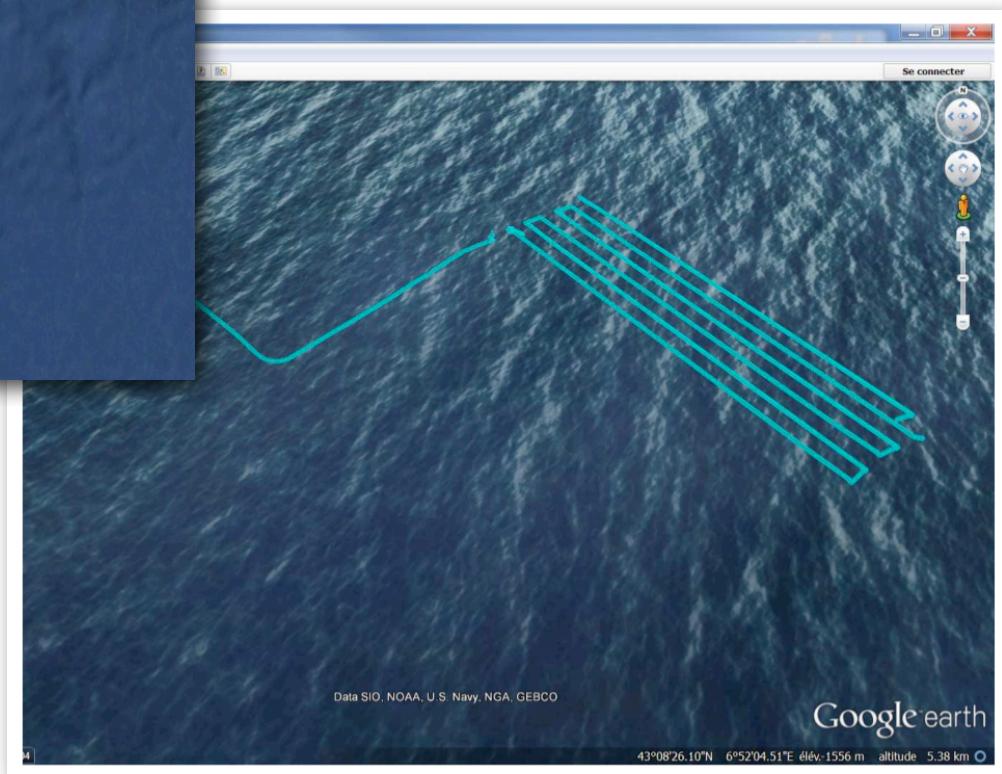


Données fournies par l'**IFREMER**

Marie-Edith BOUHIER

Données échantillonnées

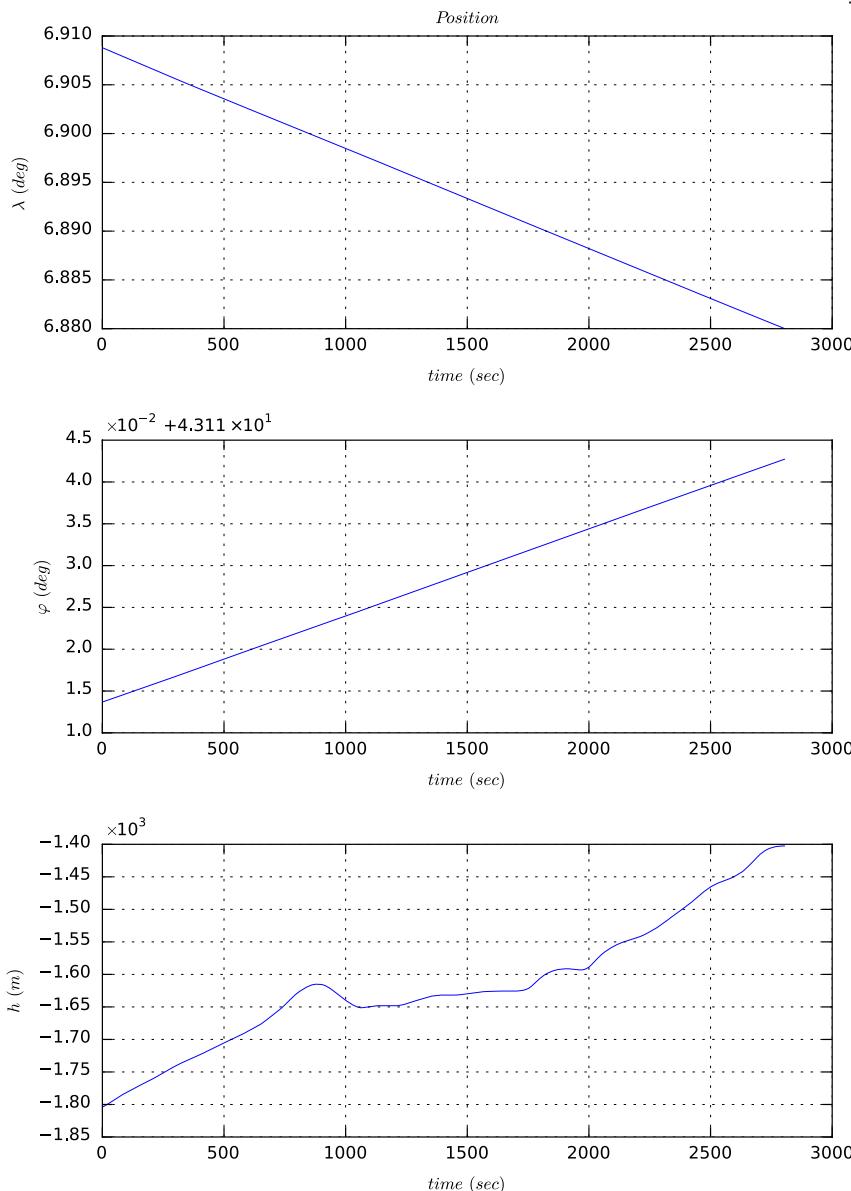
$$T_e = 1 \text{ s}$$



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# Numerical simulation

Reference motion of the carrier



$$\lambda(t) = \lambda^{\text{ref}}(t) + b_\lambda(t)$$

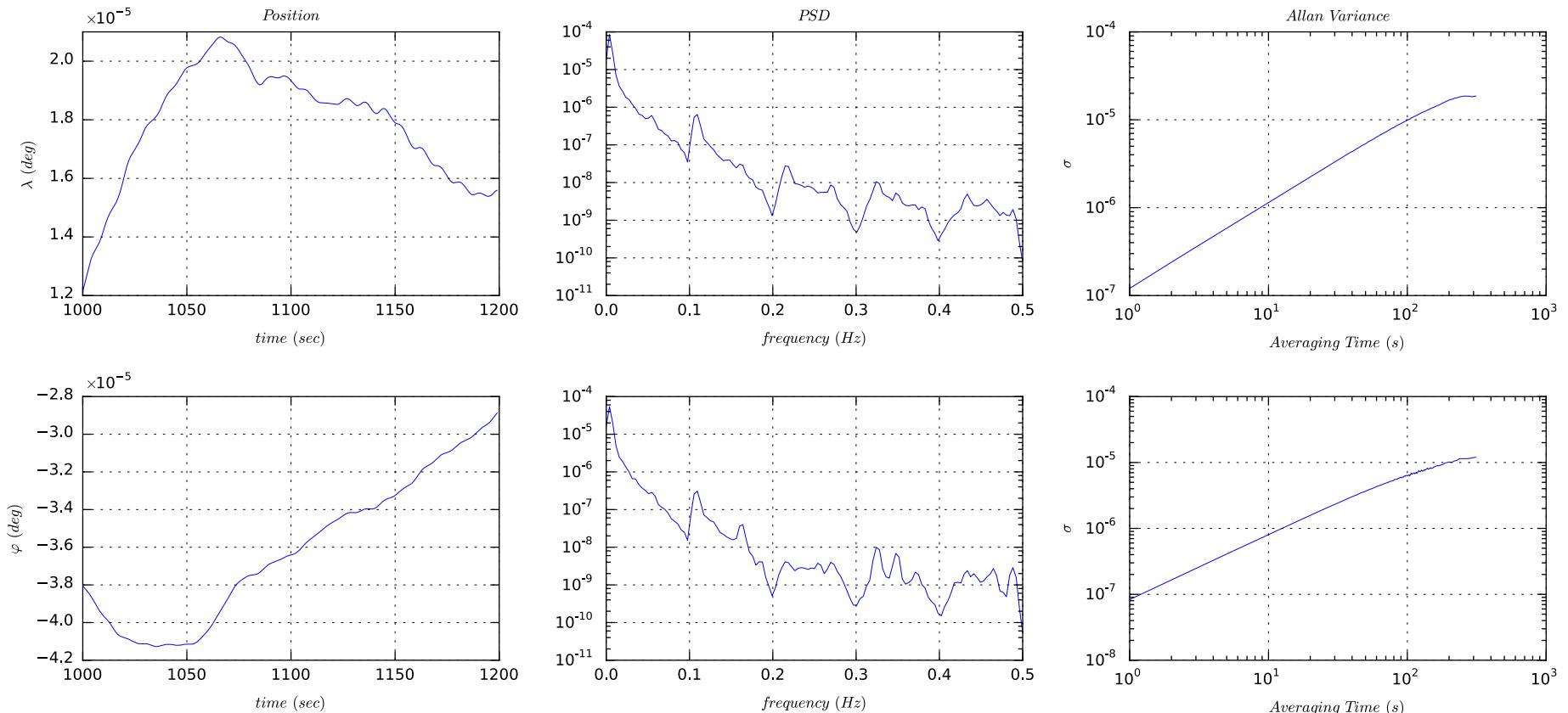
$$\varphi(t) = \varphi^{\text{ref}}(t) + b_\varphi(t)$$

$$h(t) = h^{\text{ref}}(t) + b_h(t)$$

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# Numerical simulation

## Reference motion of the carrier



GRAVIMOB : a new gravimetry and gradiometry mobile system for the subsea domain.

# Numerical simulation

Principle

$$a_M^{ref} = \ddot{X}_M^{ref} - g_M^{ref}$$

Accélérations de rappel de référence  
**déduites**

Champ de gravité de référence  
**choisi**

Mouvement de référence du porteur  
**choisi**

$$g_M = \ddot{X}_M - a_M$$

Champ de gravité **déduit**

Accélérations de rappel de référence  
**+ bruit**

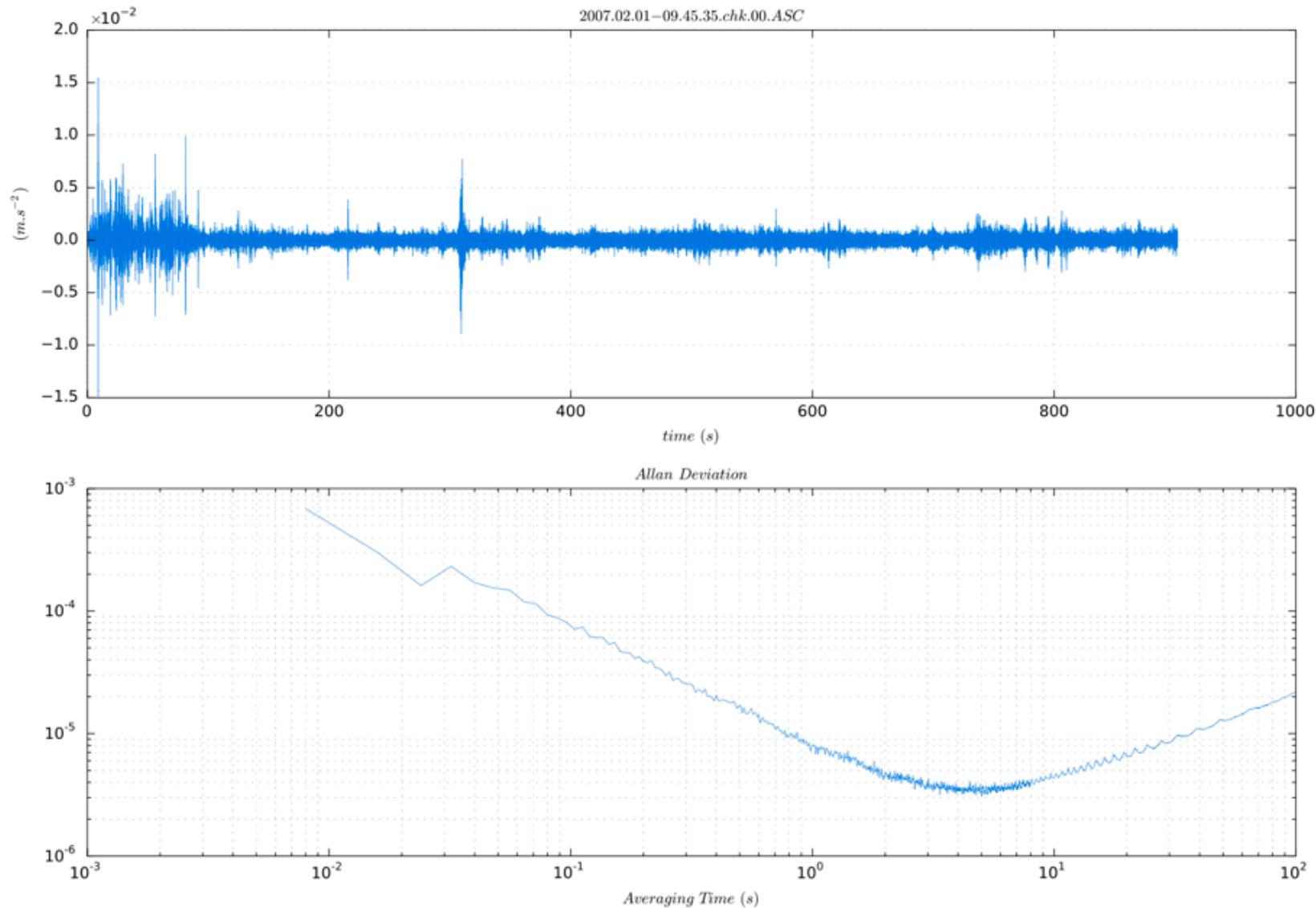
Mouvement de référence du porteur  
**+ bruit**

$$\epsilon = g_M - g_M^{ref} \quad \left\{ \begin{array}{l} E(\epsilon) = \frac{1}{n} \sum_0^n \epsilon \\ VAR(\epsilon) = E((\epsilon - E(\epsilon))^2) \end{array} \right.$$

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# Numerical simulation

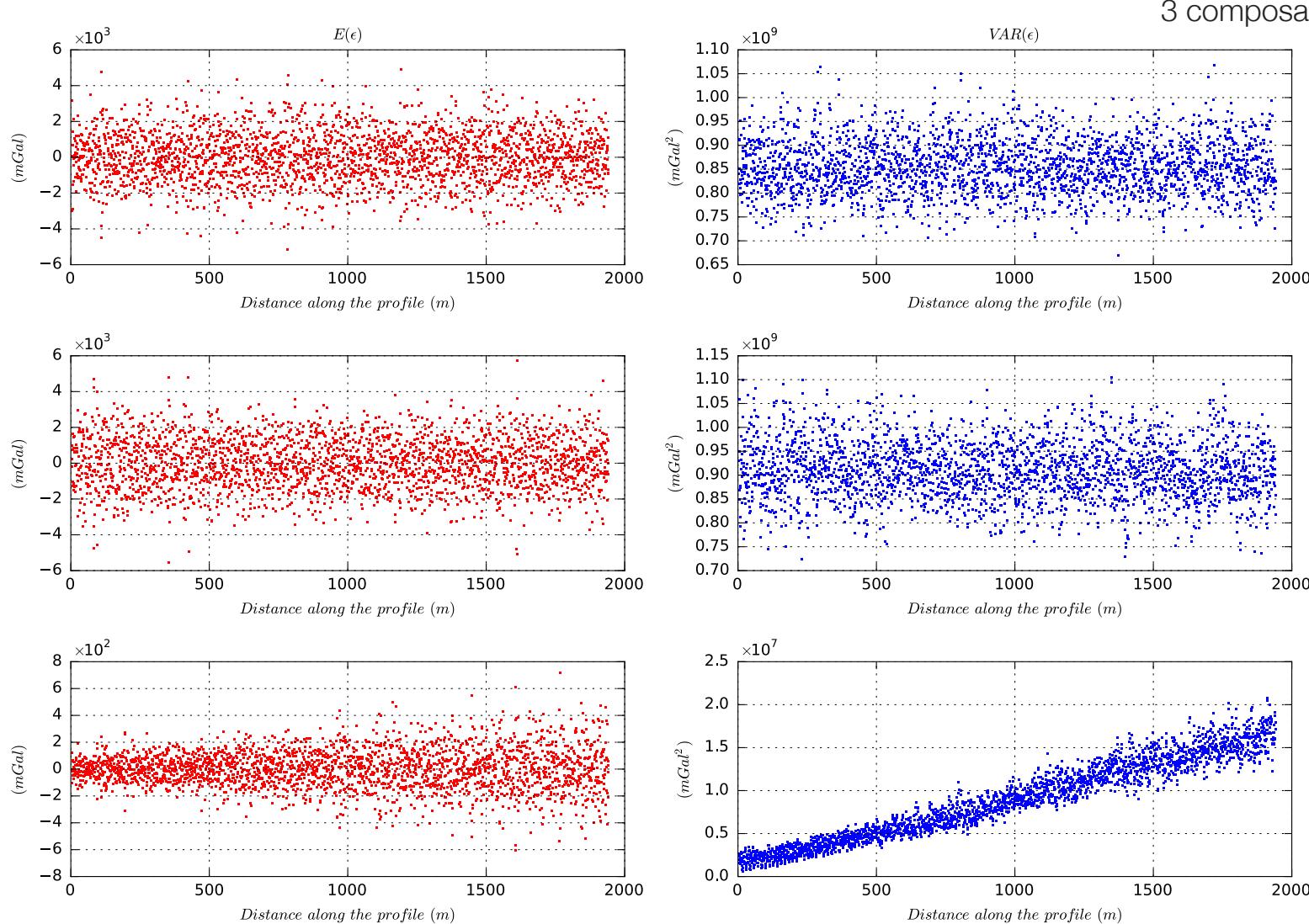
Specific force



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# Numerical simulation

Espérance et Variance de l'erreur



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