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Letters

Laboratory simulations of tensile fracture development in a volcanic conduit via cyclic magma pressurisation

Philip M. Benson a,b,*, Michael J. Heap c, Yan Lavallée d, Asher Flaws d, K.-U. Hess d, A.P.S. Selvadurai e, Donald B. Dingwell d, B. Schillinger f

a Geological Institute, Department of Earth Sciences, Swiss Federal Institute of Technology, Zurich 8092, Switzerland
b Rock Mechanics Laboratory, School of Earth and Environment, University of Portsmouth, Portsmouth PO1 3QL, UK
c École et Observatoire des Sciences de la Terre, Université de Strasbourg (UMR 7516 Centre National de la Recherche Scientifique), France
d Earth and Environment, LMU—University of Munich, Theresienstr. 41, 80333 München, Germany
e Department of Civil Engineering and Applied Mechanics, McGill University, Montreal, Quebec, Canada H3A 2K6
f Forschungszentrum Jülich, Technische Universität München, 85747 Garching, Germany

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A B S T R A C T

During volcanic unrest, high magma pressure induces cracking and faulting of the country rock, providing conduits for the transport of magma and other fluids. These conduits, known as dykes, are fundamental structures for the transport of magma to the surface in volcanically active regions. The mechanics of dyke propagation is not yet fully understood but is crucial to better model dyke emplacement and eruption in volcanoes. Central to this need is a greater understanding of the mechanical properties of the magma/country rock interaction as a function of known magmatic pressure, temperature and stress. Here, we report data from a series of experiments in which we cyclically compress viscoelastic rhyolitic magma (at 828 °C, 892 °C and 918 °C) inside a cylindrical conduit-like shell of basalt (from Mt. Etna, Italy) until fracture occurs. The compression is performed under strain rates cyclically varying between 5 × 10−6 and 5 × 10−5 s−1. The resultant monitored axial loading and relaxation illustrates how the presence of a visco-elastic fluid (magma) controls the stress induced at the conduit margin boundary. This is achieved by analysing the viscoelastic relaxation (through time) to calculate an apparent modulus, which is found to decrease with both increasing stress induced at the conduit margin boundary. This is achieved by analysing the viscoelastic relaxation (through time) to calculate an apparent modulus, which is found to decrease with both increasing stress and time. In the 4 cycles before failure we find that the apparent modulus decreases from 180 to 40 GPa, 80 to 20 GPa and 8 to 1 GPa for imposed stress cycles at 828 °C, 892 °C and 918 °C, respectively. We theoretically estimate a tensile strength at failure of approximately 7–11 MPa, consistent with recent field data and in agreement with a model derived from the sample geometry and basic material parameters. Post-experimental neutron computed tomography and microscopic analyses further reveal the fragmentation of the melt and generation of tuffisite veins inside the conduit due to spontaneous crack nucleation associated with conduit wall fracture. The geometry of the rupture area inside the melt is akin to a Mach cone associated with supershear fractures. We discuss our findings in terms of magma-rock interaction leading to dykes, tuffisite veins and magma fragmentation.

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1. Introduction

The link between magmatism and tectonic structures has long been recognised (e.g. Nakamura, 1977; De Natale et al., 1997; Acocella et al., 2001; Lavallée et al., 2009; Gundmundsson, 2011a). For instance, pressure gradients force magma to ascend through the crust via the process of tensile failure in the country rock at the propagating dyke tip, aided by any existing faults and fractures (Pitcher, 1979). Movement into and through these pathways produces stress fluctuations that act against the host rock and the local/regional tectonic stress field (Hutton, 1996). If the local strength of the rock is exceeded, the resultant failure will modify the stress field (Pertsov et al., 1977; Bonafede and Danesi, 2010), with repercussions on the chemical equilibrium of the magma under the new pressure conditions as well as creating new pathways to divert its course of ascent and to transport exsolved gases. Therefore, dyking exerts a primary control on the integrity of the host rocks whilst simultaneously affecting the physical and chemical evolution of the magma as it attempts to...
reach the surface and erupt. It follows that our assessments of volcanic hazards fundamentally rely on our knowledge of host rock failure, dyke injection and magma transport—processes controlled by the mechanical properties of the rock and the rheological behaviour of the intruding magma (e.g. Gudmundsson, 2011a).

The failure of rocks is initiated largely in tension (Griffith, 1920), owing to the tensile strength of rocks being approximately a tenth of their compressive strength (Jaeger et al., 2007). Shear faulting is essentially a result of the linkage of many smaller tensile cracks (e.g. Paterson and Wong, 2005). Once nucleated, fractures can further propagate due to perturbation of the elastic energy release rate or the stress intensity factor at the crack tips (Inglis, 1913; Broek, 1982). In the case of dyke propagation at high temperatures, the viscoelastic response of the rock, creep (subcritical crack growth) at the dyke tips may accelerate the propagation by one order of magnitude (Chen and Jin, 2011). Experimental studies have mapped out the fracture toughness of volcanic rocks subjected to a range of temperatures and confining pressures (Rocchi et al., 2004; Balme et al., 2004; Smith et al., 2009). These findings therefore suggest that the propagation of tensile fractures would ease as they extend towards the Earth’s surface, a scenario usually favoured in numerical simulations (e.g. Santoni et al., 2011). Although this result can be explained by reference to the classical Griffith energy balance scenario it is important to also acknowledge that, on the other hand, discontinuities are more likely to be open near to the surface leading to the Cook–Gordon analysis of crack arrest (Gudmundsson, 2009).

In the volcanic context, magma can more easily infiltrate tensile fractures as seen in sheet-like dike structures with evidence of elastic wall deformation (e.g. Cuevas et al., 2006). Field and theoretical studies have, however, shown that the majority of dykes are arrested at depth (Gudmundsson and Brenner, 2001, 2004). In the Campi Flegrei caldera (Naples, Italy), for example, very few dykes are exposed at the surface due to the soft overburden (e.g. De Natale et al., 1997), creating stress-release barriers that adversely influence the ability of the dyke tip to propagate further (Gudmundsson, 2011a). The source of these discrepancies may partly reside in the stress imparted by the magma.

During ascent, the physical, chemical and thus rheological properties of magma evolve (Sparks et al., 1997). Changes in pressure and temperature force crystallisation and the exsolution of volatiles which promote an increase in viscosity (Hess and Dingwell, 1996; Lejeune and Richet, 1995) as well as an increase in pore pressure (Massol and Jaupart, 1999). These end effects counteract one another during the magma-driven fracture propagation through the crust (Carrigan, 2000), an increase in viscosity serves to slow magma migration, whereas an increase in pore fluid pressure favours cracking of the host rock. In addition, bubble segregation from the magma followed by accumulation near the fracture tip can amplify the local stress to exceed the fracture toughness. The relationship between the magma rheology, the rock stress and the stress field generated at their interface is thus fundamental to our understanding of fracturing, dyking and magma transport.

Experimental investigations of fracturing, dyking and magma transport are scarce. Work has concentrated either on analogue setups using gelatine and other materials that are fractured by injection of coloured water (Menand and Tailt, 2001; Acocella et al., 2001; Walter and Troll, 2003), or – for simulation of representative rock properties – a simplified experimental setup at room temperatures. In the latter case, hydrofracturing is caused by increasing the water pressure within an axial conduit (cored out of a cylindrical rock shell) flanked by a rubber membrane (to isolate the fluid from the rock) until failure of the rock shell (e.g. Vinciguerra et al., 2004). Although useful for visualising the physical processes occurring during dynamic fracturing, this type of experiment cannot reveal the interaction between the dyke tip and the host rock because the pressurising medium is mechanically coupled to the inner bore by the membrane. In addition, since this type of experiment is conducted at low temperatures, it cannot reproduce the behaviour of magma interacting with the host rock. Here, we experimentally simulate magma–rock interaction by compressing a magma inside a conduit-like cylindrical shell until fracturing of the shell occurs. The experiments provide an estimate of the magma stress relaxation and the tensile strength of the conduit wall rocks at high temperatures, as well as a description of the physics occurring at the onset of dyking.

2. Methods

Magma–rock failure tests were performed by combining Cougar Creek obsidian, CO, (from the Cougar Creek lava flow, Yellowstone National Park, USA; see Christiansen, 2001), and Etna basalt, EB, (from Mt. Etna volcano, Italy) in an experimental setup analogous to hydraulic fracture experiments (see below for details). The selected obsidian is a dense (porosity of <0.1%), aphyric rhyolite, simulating flow of a single-phase silicate melt at high temperature. The basalt is a porphyritic, alkali basalt of approximately 3.8% porosity. It comprises millimetre-size phenocrysts of pyroxene, olivine and feldspar within a fully crystallised, fine-grained groundmass. The basalt was chosen because it has been extensively studied (Stanchits et al., 2006; Benson et al., 2007, 2010; Heap et al., 2009, 2011) and because its properties are nearly isotropic (e.g. ultrasonic wave velocities) and temperature independent (the mechanical strength was found to be independent of temperature up to 900 °C). Furthermore, this basalt contains no glass, so it should not undergo softening at the investigated temperatures. Thus, these materials were selected since the rhyolite can deform viscously while the basalt will remain brittle under the given experimental temperatures. Our study was carried out in three phases.

Firstly, we characterised the viscosity–temperature relationship of the rhyolitic melt to be used as a guide for our experimental temperatures. We employed the standard micropenetration technique using a Baehr vertical dilatometer, which involved monitoring the penetration rate of an indenter (of known geometrical end shape) into a disc of melt (Hess and Dingwell, 1996). The rate of indentation of a small melt disc (6 mm in diameter and 3 mm in thickness) was used to compute the viscosity as a function of temperature, according to:

\[ \eta_{\text{shear}} = \frac{0.1875F}{a^2/2} \cdot \frac{t}{1.5} \]

where \( F \) is the force applied by the indenter, \( t \) the time of indentation, \( r \) the indenter radius, and \( z \) the indented depth. This method resolves the viscosity to within \( +/−0.05 \) log unit of viscosity (Hess and Dingwell, 1996).

Secondly, the uniaxial compressive strength of the basalt was investigated at a range of temperatures (25, 200, 500, 750, 900 and 950 °C) on cylindrical cores (25 mm in diameter and 75 mm in length) in a high-temperature uniaxial press (a full description of the uniaxial press can be found in Hess et al., 2007). The strength tests were performed under the same variable strain rates as used in the magma–rock failure tests (see below).

Finally, magma–rock failure tests were performed in the high-temperature uniaxial press by pressing a plug of basalt (a disc 10 mm in diameter and 10 mm in length) onto a central core of rhyolitic melt (10 mm in diameter and 85 mm in length) encased by an outer shell of basalt (60 mm in diameter and 90 mm in
length; Fig. 1). The plug of basalt ensured that the inner conduit could be loaded without the loss of melt. Pressurisation of the inner melt was achieved by cyclically changing the imposed axial strain rate between $3.2 \times 10^{-5} \text{ s}^{-1}$ for 30 s and $1.3 \times 10^{-6} \text{ s}^{-1}$ for 300 s, thus yielding an average of $6.5 \times 10^{-6} \text{ s}^{-1}$. This cyclicity was applied in an attempt to best simulate the cyclic pressurisation inferred from volcanic conduits (Vinciguerra et al., 2005).

The uniaxial compressive strength of the basalt was investigated at three temperatures (25, 200, 500, 750, 900 and 950 °C) in order to probe potential changes in the mechanical behaviour. Brittle failure was observed in all samples (Fig. 3). Below 950 °C the strength remained approximately 150 MPa and did not vary systematically with temperature. At 950 °C the sample demonstrated mild changes in the mechanical behaviour, resulting in an increase in the peak stress and total strain at failure. Altogether, the data yielded values comparable to complementary studies (e.g., Heap et al., 2010).

3. Results and analysis

3.1. Conduit melt viscosity

The temperature dependence of viscosity investigated through micropenetration shows that the Cougar Creek rhyolitic melt is a strong melt (low fragility index), with a near Arrhenian behaviour (Fig. 2). The viscosity data shows a standard deviation below 0.05 log unit of viscosity. Application of the Vogel–Fulcher–Tammann (VFT) equation resolves the viscosity ($\eta$) to:

$$\log \eta = A + \frac{B}{T - C}$$

where $T$ is the temperature in Celsius, valid between the investigated temperature range of 750 and 920 °C, and $A = -0.6505$, $B = 7342$, and $C = -132$.

3.2. Uniaxial compressive strength of the basalt

The uniaxial compressive strength of the basalt was investigated at a range of temperatures (25, 200, 500, 750, 900 and 950 °C) in order to probe potential changes in the mechanical behaviour. Brittle failure was observed in all samples (Fig. 3). Below 950 °C the strength remained approximately 150 MPa and did not vary systematically with temperature. At 950 °C the sample demonstrated mild changes in the mechanical behaviour, resulting in an increase in the peak stress and total strain at failure. Altogether, the data yielded values comparable to complementary studies (e.g., Heap et al., 2010).

3.3. Magma–rock failure test

The mechanical behaviour of conduit failure due to magma pressurisation was investigated at three temperatures. Fig. 4 shows the evolution of stress (axially generated on the cylindrical end of the inner melt core) with strain of the magma. During the experiment at 828 °C (Fig. 4A), the first detection of accumulated stress occurred at approximately 2570 s, with a subsequent stress...
drop noted as the strain rate entered its deceleration phase. The next cycle of strain rate acceleration/deceleration was also accompanied by a stress concentration/drop. The character of the third, fourth and fifth cycles of strain rate acceleration/deceleration were, however, significantly different in that a much higher stress accumulation was measured, of 25, 38 and 45 MPa respectively, and in each case an exponential stress drop occurred that did not fully recover to zero before the onset of the subsequent strain acceleration. The onset of pressure accumulation further coincided with the continuous release in acoustic emissions. The fifth and final cycle induced a stress drop to a low value (6–7 MPa) as a result of the complete failure of the outer shell. Failure was accompanied by a momentary increase in acoustic emissions. The two subsequent cycles of strain rate acceleration/deceleration showed that stress was incapable of accumulating and that acoustic emissions were fluctuating. The data show a clear dependence of the conduit pressure on the strain rate, since the peak stress increases in subsequent cycles, and the stress is released during the strain deceleration phases.

The general observations of stress concentration and relaxation as well as the accompanying acoustic emissions remain similar for all magma-conduit pressurisation tests, irrespective of the temperature. Temperature, which according to our investigation lowers the melt viscosity more than it affects the elastic properties of the temperature. Temperature, which according to our investigation lowers the melt viscosity more than it affects the elastic properties of the melt, affects both the axial stress and the relaxation rate. A complementary analysis of the criterion for failure at approximately (A) 3550 s, (B) 10475 s, and (C) 10560 s. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Fig. 3. Uniaxial compressive strength (UCS) of the basalt as a function of temperature. The UCS is largely independent of temperature up to 900 °C.

4. Analysis

4.1. Structural analysis

Optical observation of the samples after the experiments clearly illustrates the tensile nature of the cracks that developed (Fig. 5). In plan view, the samples display two or three tensile cracks separated by angles of 180° or 120°, respectively, which illustrate the axisymmetric nature of the setup. Axially, these cracks extend the entire length of each shell. The aperture of each fracture varies between each experiment; in some cases (Fig. 5, YE3), the sample fractured violently resulting in the presence of large glass fragments in the tensile cracks (Lavallée et al., 2012).

Post-test neutron computed tomography images of the sample revealed the continuity of each tensile fracture developed, from the outer to the inner margin of the shell (Fig. 6). An in-depth examination of the cracks clearly shows that they extend further into the rhyolite conduit. Microscopic analysis provides further details of the geometry of the cracks in the glass, which was a melt as it underwent brittle deformation. In detail, we observe a fragmented area hosting multiple micrometric cracks, converging towards the rupture tips, some 600 μm inside the glass (melt). The ability of a melt to fracture requires a strain rate faster than its relaxation rate. A complementary analysis of the criterion for failure of the melt during conduit fracturing is presented in
By examining the time-scale of stress release, it is possible to extract a quantitative relationship between the dynamic modulus of the melt in the conduit and the stress decay rate prior to shell failure. The analysis makes use of the known viscosity of the central rhyolitic melt at the temperatures of interest (Fig. 2), in order to derive an apparent modulus for the melt. Four cycles of strain-hold are considered prior to shell failure, and the Maxwell model adapted by Richter (2006) is used. This application is possible because the viscosity of a Newtonian melt remains constant at the tested strain rates:

$$\sigma(t) = \sigma_0 \exp \left[ - \frac{(t - t_0) M_0}{\eta_0} \right]$$

This analysis delivers the Young’s modulus of the inner conduit (melt); however, for the purposes of our study, we adopt a generalised ‘apparent’ modulus ($M_a$). Other variables include time $t$, loading time $t_L$, peak stress $\sigma_0$, stress at time $t$, and tensile viscosity $\eta_t$ (Eq. (3)). Fig. 7 illustrates the first 100 s immediately after the commencement of the deceleration segments of the four cycles preceding shell failure (for each of the three experiments shown in Fig. 3). Application of Eq. (3) using measured viscosities of 8.3, 9.6 and 10 log unit (in Pa s), thus permits the calculation of the conduit stiffness with each cycle and temperature (Fig. 8). For all experiments, the stress decay exponent decreases (i.e. becomes flatter) moving from cycle 1 to 4. In terms of material stiffness, this result shows a decrease in modulus $M_a$ from 180 to 30 MPa at 828 °C, from 80 MPa to 10 MPa at 892 °C and from 8 MPa to nearly zero MPa in the case of 918 °C. This suggests that the apparent modulus decreases as stress accumulates on the outer shell, leading to failure, as the temperature increases.

### 4.3. Peak stress at failure

The outer shell is most likely to fail when the hoop stress at its boundary exceeds the limiting tensile strength of the basalt. It is possible to estimate the tensile strength of the basalt shell using a combination of setup geometry and knowledge of the Young’s modulus, the Poisson’s ratio, and the material stiffness (as provided by Rocchi et al., 2004; Heap et al., 2011; Selvadurai and Benson, 2012). This analysis provides a direct measure of the stress accumulated in the magma at failure, and thus the resistance of magma to dyking.

In a recent study, Selvadurai and Benson (2012) theoretically examined the problem of the internal pressurisation of a hollow elastic cylinder of internal radius $a$ and external radius $b$ by a
Young's modulus of the basaltic shell with isotropic stress fields. The objective of their study was to use the smoothly embedded cylindrical elastic inclusion as a device for exerting a radial stress at the interface, which in turn would induce a tensile stress field in the hollow elastic cylinder. The use of an elastic cylindrical inclusion or plug to induce the hoop stress state in the annular cylinder is considered to be a more convenient and controllable loading configuration as opposed to the application of fluid pressures, which would entail abrupt rupture of the outer cylinder, particularly if the aspect ratio \( b/a = 1 \) is marginally in excess of unity. The provision of a smooth interface between the cylindrical inclusion and the annular cylinder lends itself to the development of a relatively convenient closed form analytical solution based on the classical theory of elasticity. In an experiment, this interface has to be smooth to ensure the applicability of the theoretical results. [Note: the alternative to account for axial friction between the inner core and the external annular cylinder is much more difficult and the stress analysis of the resulting problem can only be performed through a computational approach (Selvadurai and Boulon, 1995).]

In the context of the application of the theoretical derivation to the present magma pressurisation problem, the outer annular cylinder can be regarded as the basaltic shell with isotropic Young's modulus \( E_b \) and Poisson's ratio \( \nu_b \) and the inner closely fitting elastic inclusion can be regarded as the conduit core of rhyolitic melt of isotropic Young's modulus \( E_c \) and Poisson's ratio \( \nu_c \). The inner core is subjected to a uniform axial compressive stress \( \sigma_a \) and the outer boundary of the annular basalt cylinder is maintained traction free. The analysis of the resulting elasticity problem is straightforward and the assumption of complete contact at the interface between the inner core and the external cylinder ensures that the radial displacement and the radial tractions exhibit continuity (Timoshenko and Goodier, 1970; Davis and Selvadurai, 1996; Selvadurai, 2000). The specifics of the analysis of the elastic plug compression problem are given in Selvadurai and Benson (2012), who also use the elastic inclusion compression approach to estimate the tensile strength of annular cylinders of Stanstead Granite. These studies also present an approach for estimating the Mode I fracture toughness of the geomaterial. The result of primary interest to the present paper relates to the tensile hoop stress that is generated at the boundary of the annular rock cylinder during compression of the central cylindrical elastic core by the axial compressive stress \( \sigma_a \), which can be evaluated in exact closed form. For example, the tensile hoop stress at the inner boundary of the outer cylindrical rock can be evaluated using:

\[
\sigma_{bh}(t) = |\sigma_a| \frac{\nu_c(t^2 + 1)}{(E_c/\nu_b)(t^2) + (1-\nu_c) + (1-\nu_c)(t^2 - 1)}
\]

(4)

It is clear that in order for these stresses to develop, \( \nu_c \neq 0 \) and the analysis (Selvadurai and Benson, 2012) shows that the interface compressive stress is identical to the tensile hoop stress generated at the boundary of the rock. Of specific interest are the results applicable to the limiting case where the outer boundary of the core extends to infinity (i.e. \( t \to \infty \)). In this case the above results yield:

\[
|\sigma_{bh}(0)| \to \infty = |\sigma_a| \frac{\nu_c}{(E_c(1+\nu_b)/(1+\nu_c))}
\]

(5)

Known parameters in Eqs. (4) and (5) include the applied stress \( \sigma_a \) the ratio of conduit to shell diameter \( \Gamma \), the Poisson's ratios and Young's moduli for the outer shell and the core \((\nu_c, E_c)\) and \((\nu_b, E_b)\) respectively. The modulus of the conduit is calculated from the stress relaxation stage of the experiment discussed previously, leaving only the Poisson's ratio of the melt (0.35 ± 0.05) that is taken from previously published model data (Lister and Kerr, 1991). This permits the tensile stress to be calculated as a function of the applied stress. If this stress at the boundary of the country rock reaches the limiting tensile strength, fracture will occur.

To compare the theoretical fracture criteria with the laboratory data, Fig. 9 shows the theoretical (hoop) stress (given by Eq. (4)) as a function of the applied stress and a ‘family’ of representative Poisson’s ratios (0.3–0.35–0.4) for the conduit, superimposed with the actual stress at which the samples failed (arrows). A clear relationship is seen whereby higher temperatures require a lower...
the state of the host rocks at depth (e.g. Nakamura, 1977; stability/integrity of a volcanic conduit, strongly relies on probing volcanic hazards posed by the propagation of dykes, as well as the Collinson and Neuberg, 2011). Indeed, the accuracy of forecasting through dykes is central to our understanding of mass transport.

5. Discussion and conclusions

The dynamics of fracturing and associated magma movement through dykes is central to our understanding of mass transport and ultimately to our descriptions of volcanic eruptions (McNutt, 1996; Carracedo, 1999; Gudmundsson and Brenner, 2004; Collinson and Neuberg, 2011). Indeed, the accuracy of forecasting volcanic hazards posed by the propagation of dykes, as well as the stability/integrity of a volcanic conduit, strongly relies on probing the state of the host rocks at depth (e.g. Nakamura, 1977; Gudmundsson and Loetveit, 2005) – a task that cannot be achieved with current state of knowledge regarding monitored geophysical signals alone (McNutt, 1996; Smith et al., 2009). Models require the input of the path leading to various conduit fracture properties at depth and in volcanic edifices (e.g. Gudmundsson and Brenner, 2001; Vinciguerra et al., 2004). The present experimental and analytical investigation of magma–rock coupling to the problem of dyke initiation demonstrates the strong relationship between magma rheology and host rock elasticity. A decrease in the apparent Young’s modulus of the magma precedes the tensile fracture of the host rock, which generates a local strain rate capable of fragmenting the magma.

Material stiffness is a key parameter of volcanic melts, and in many cases it is intimately linked to the explosivity of magma (e.g. Dingwell, 1996). The ability to estimate an apparent modulus of magma at depth would be helpful; since direct measurements are impractical, complimentary means must be employed to obtain such data. Our analysis suggests that it is possible to do so by incorporating measured viscous and elastic parameters (e.g. Table 1) in Eq. (4). For the case of the competent outer basalt shell, the Young’s modulus and Poisson’s ratio were measured directly and found to be essentially temperature invariant within our investigated temperature range (Heap et al., 2009), which is in broad agreement with the work of Rocchi et al. (2004).

Likewise, the viscosity of the rhyolite melt is also known as a function of temperature. The least constrained parameter, the Poisson’s ratio of the melt, was given a central value of 0.35 with a spread of 0.05 to calculate the tensile fracturing. The lower and centre estimates for Poisson’s ratio within this range have been suggested in the small number of studies done to date (Gudmundsson, 1988; Rubin, 1995; Carpenter and Cash, 1988; Chu et al., 2010), with the upper end data measured at room temperature. Our analysis resolves the tensile (hoop) stress required to fracture the outer shell to be approximately 7 to 11 MPa, irrespective of the viscosity of the conduit. This agrees with field estimates for the tensile strength of rocks important in dyke propagation of approximately 6–9 MPa (Gudmundsson, 2011a, 2011b).

The stress relaxation is analysed using the Maxwell–Zener model (Richter, 2006). Specifically, our experiments suggest that a noticeable decrease in the apparent modulus $M_s$ precedes failure. Although this is counterintuitive, such an effect could be produced if, as the cycles proceeded, an increase in shear stresses is present on the boundary of both the conduit and the inner shell surface. This is definitely a possibility since, in our experiment, pressurisation of the magma against the conduit wall is accompanied by an increased surface area of contact (i.e., initially, there is a narrow $< 0.1$ mm gap between the melt and the shell due to abrasion during sample preparation). Additionally, there may be rheological changes taking place due to melt pressurisation. Whether thixotropy of the melt comes into play in our investigation is rather unlikely since pressurisation of the low-viscosity melt was performed at strain rates far slower than the onset of non-Newtonian behaviour calculated via Maxwell relaxation time scale (e.g., Dingwell and Webb, 1989; see Lavallée et al., 2012). As to the likelihood that the visco-elastic behaviour of the melt is modified with increasing pressurisation, magmas are generally regarded as visco-elastic liquids with very restricted influence of pressure on the viscosity (Dingwell, 1998). It thus seems most likely that the observed apparent modulus decrease results from a combination of viscous relaxation and release of the elastic stress of the shell accumulated at the inner margin. The ability to probe for this apparent modulus in nature would thus offer a window for both the magma viscosity and the conduit wall elastic response.

Finally, it should be emphasised that the post-failure observations revealed fracturing of the melt inside the conduit. Rheological and acoustic analysis of the criterion for failure of the melt during conduit fracturing is presented in Lavallée et al. (2012), suggesting that at the high strain rates inherent in these processes, even low-viscosity melts will deform in a brittle manner (e.g., Dingwell and Webb, 1989). A close analysis of the fracture tip and surrounding crack geometry reveals a remarkable similarity to a Mach cone. Such ‘shock cone’ features generally form in spontaneously nucleated supershear ruptures, propagating faster than the local speed of sound (e.g. Xia et al., 2004), fossilised here in the (formerly molten) rhyolite at an angle $\theta$ to the fracture. Whether the cone formed as a result of sub-Rayleigh tensinal cracking of the melt during conduit shell failure or due to spontaneous supershear rupture cannot be ascertained through

![Fig. 9. Theoretical tensile failure strength as a function of internal magma pressure, inclusion modulus and temperatures. The magma pressurises until the shell fails in tension, denoted by arrows according to the maximum recorded conduit stress. Although the temperature of the experiments varies, a very similar hoop (tensile) stress at failure (i.e., 7–11 MPa) is calculated using Eq. (5).](image-url)
our post-experiment analysis; it nonetheless remains evident that magma can fragment during wall rock failure. This observation alone is important to our understanding of dyke nucleation and propagation, because not only does magma failure instigate the generation of tuffisite veins (Lavallée et al., 2012), it also contributes to the seismic record (Lavallée et al., 2008; Tuffen et al., 2003, 2008), masking the precursor signal for dyke propagation and, potentially, explosive eruptions.

In summary, the combined experimental (mechanical and AE) and analytical simulations of conduit failure induced by the inner compression of magma show that:

(a) The coupling of stress, strain and seismic data through time can be used to infer the stability of volcanic conduits and/or the state of the magma during periods of unrest via the calculation of viscoelastic relaxation parameters and hence the modulus (or viscosity) of the melt.

(b) Dyke nucleation initiates when the tensile strength of the host rocks is overcome by the magmatic pressure. In the case of the investigated basalt from Mt. Etna, the calculated tensile strength is temperature invariant and approximates 7–11 MPa.

(c) Conduit wall rock failure generates an energetic strain wave, with some evidence of this being a supershear feature, capable of locally fragmenting magma, thereby promoting the production of tuffisite veins and, potentially, episodes of explosive activity.

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